

# **Analysis and Optimization of Distributed Real-Time Embedded Systems**

**Paul Pop, Traian Pop, Sorin Manolache,  
Petru Eles, Zebo Peng**

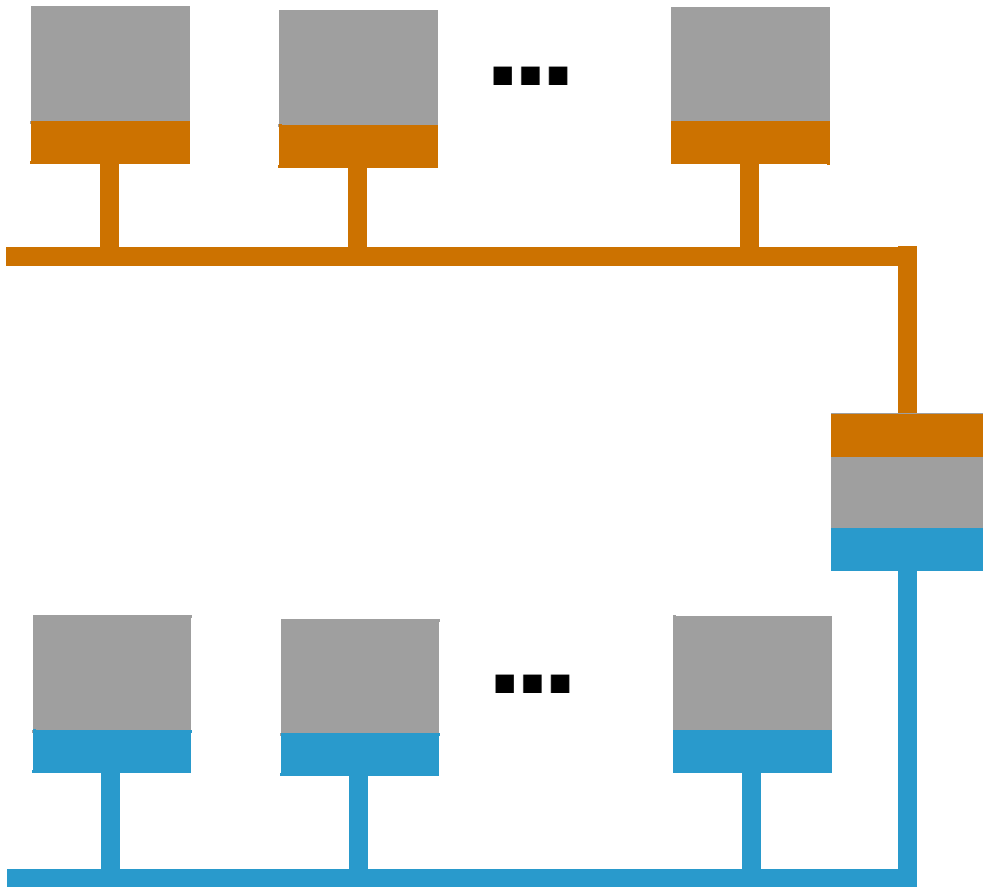
**Department of Computer and Information Science (IDA)  
Linköping University  
<http://www.ida.liu.se/~eslab/>**



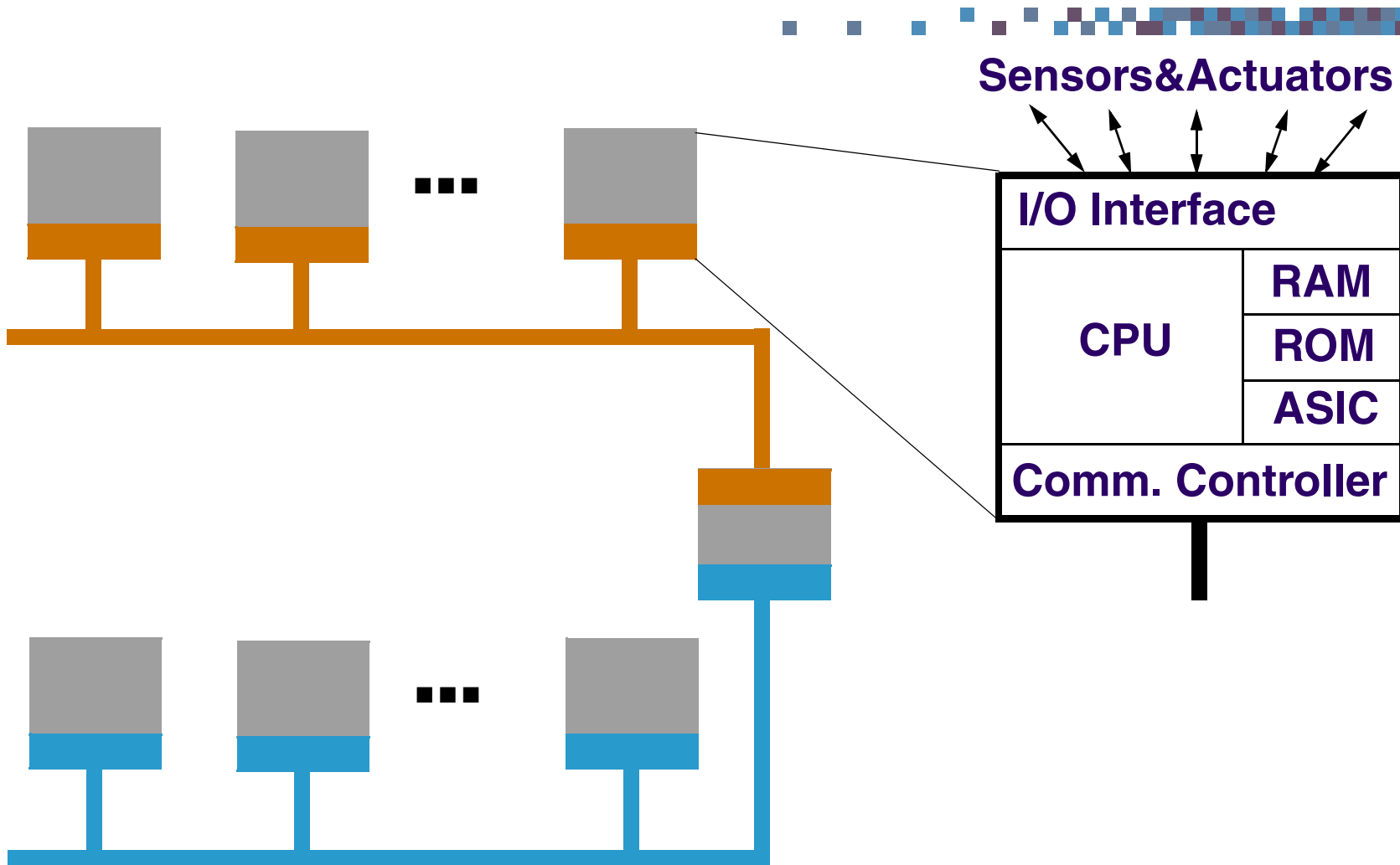
- **Distributed Embedded Systems**
- **System-level Design Flow**
- **Application Model**
- **Distributed Hard Real-Time Systems**
  - **Heterogeneous Distributed Systems**
  - **Static and Dynamic Communication**
  - **Analysis & Optimization**
  - **Fault Tolerance**
- **Distributed Soft Real-Time Systems**
  - **Analysis Approaches and Optimization**
  - **Optimization**



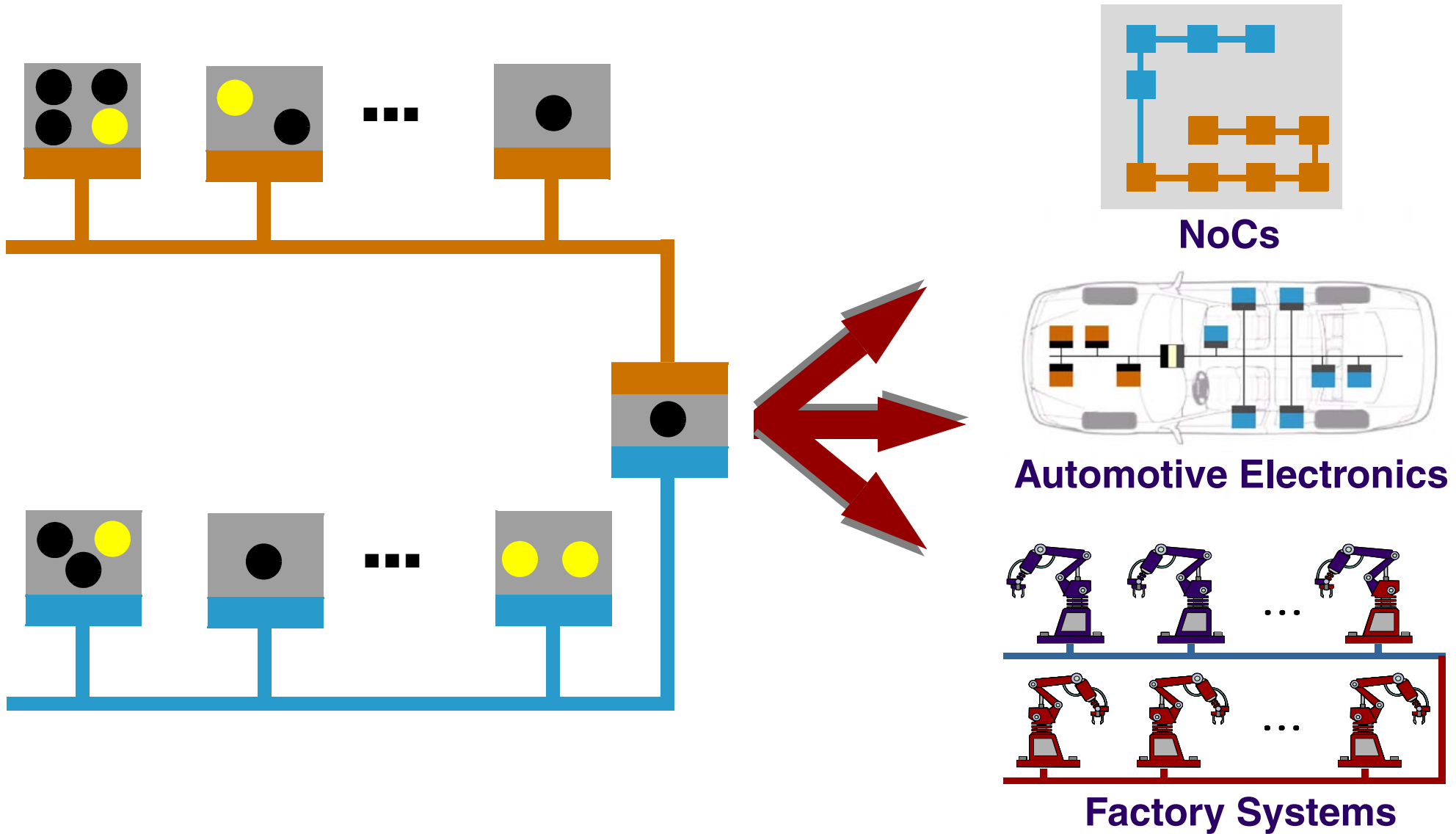
# Distributed Embedded Systems



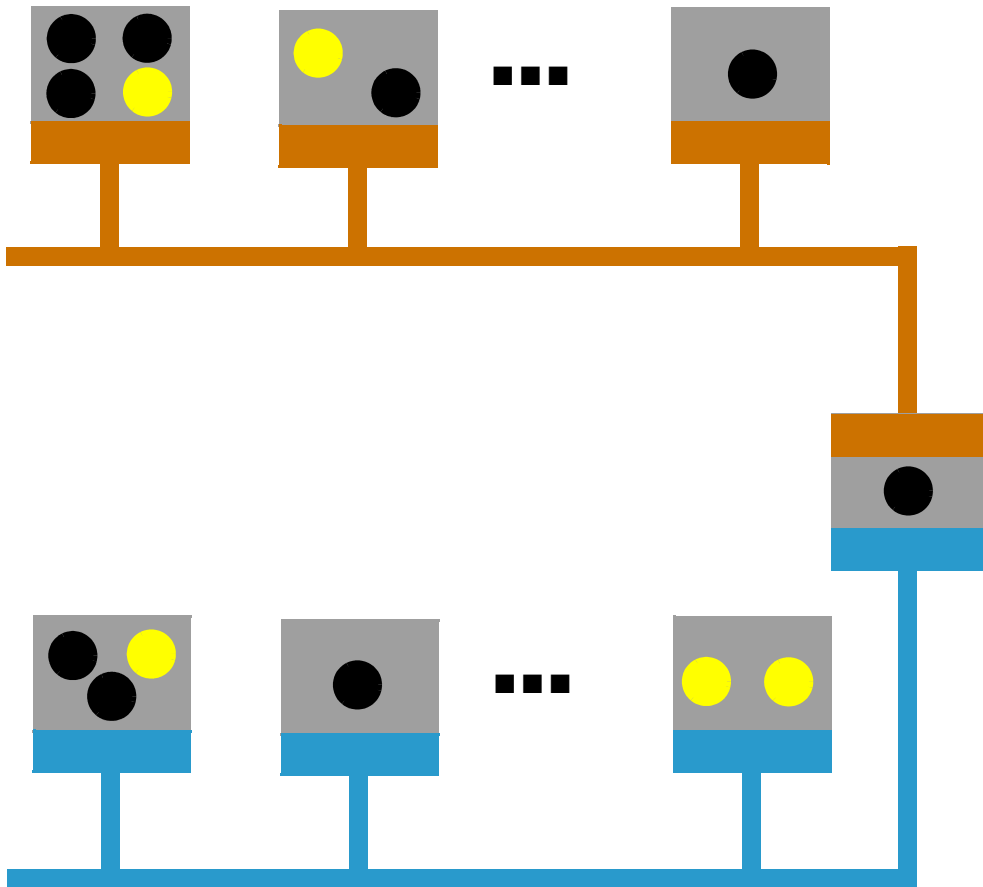
# Distributed Embedded Systems



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# Distributed Embedded Systems

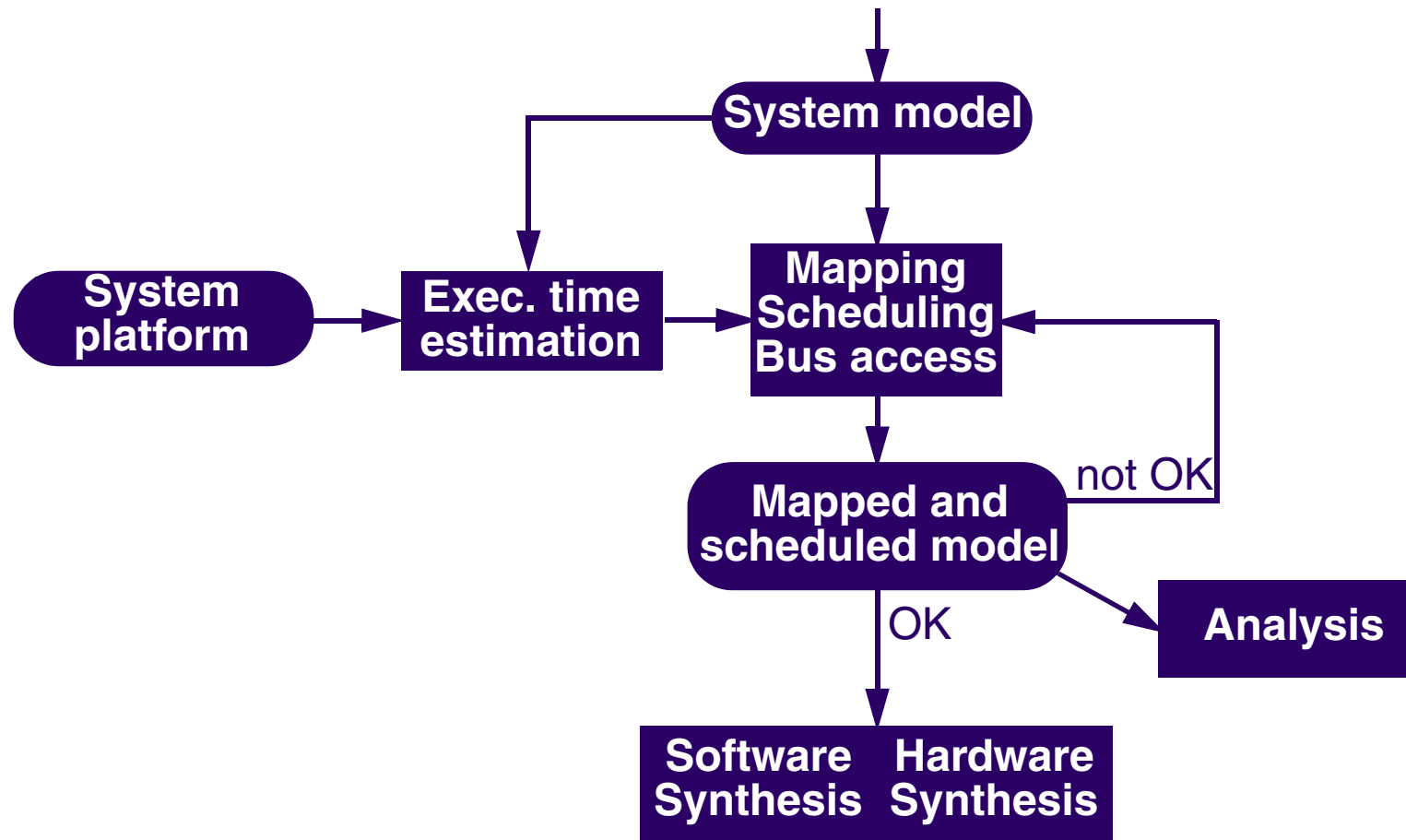


Why?

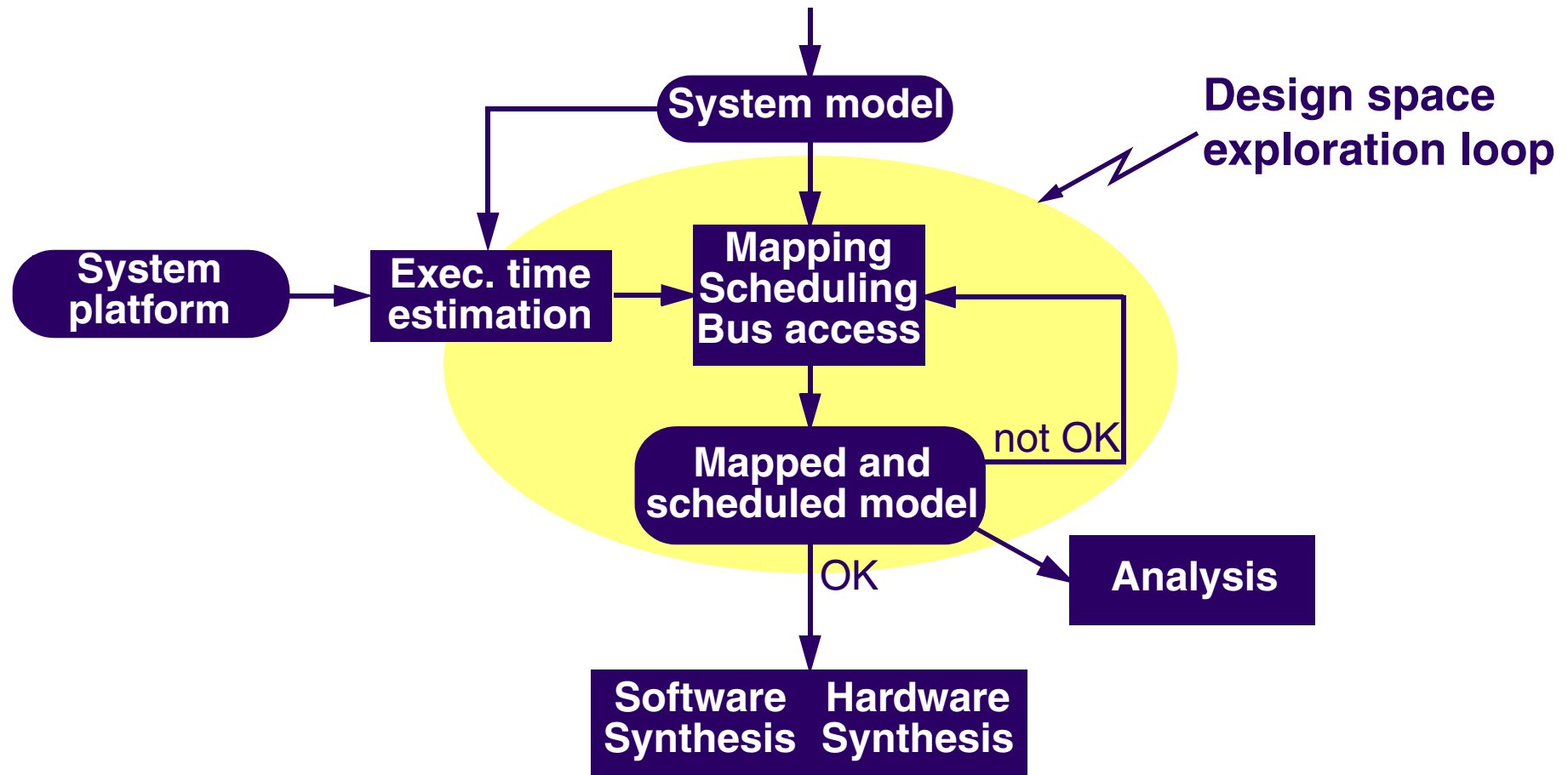
- Physical constraints
  - Operation close to sensor;
- Modularity constraints
- Safety Constraints
- Performance



# System Level Design Flow

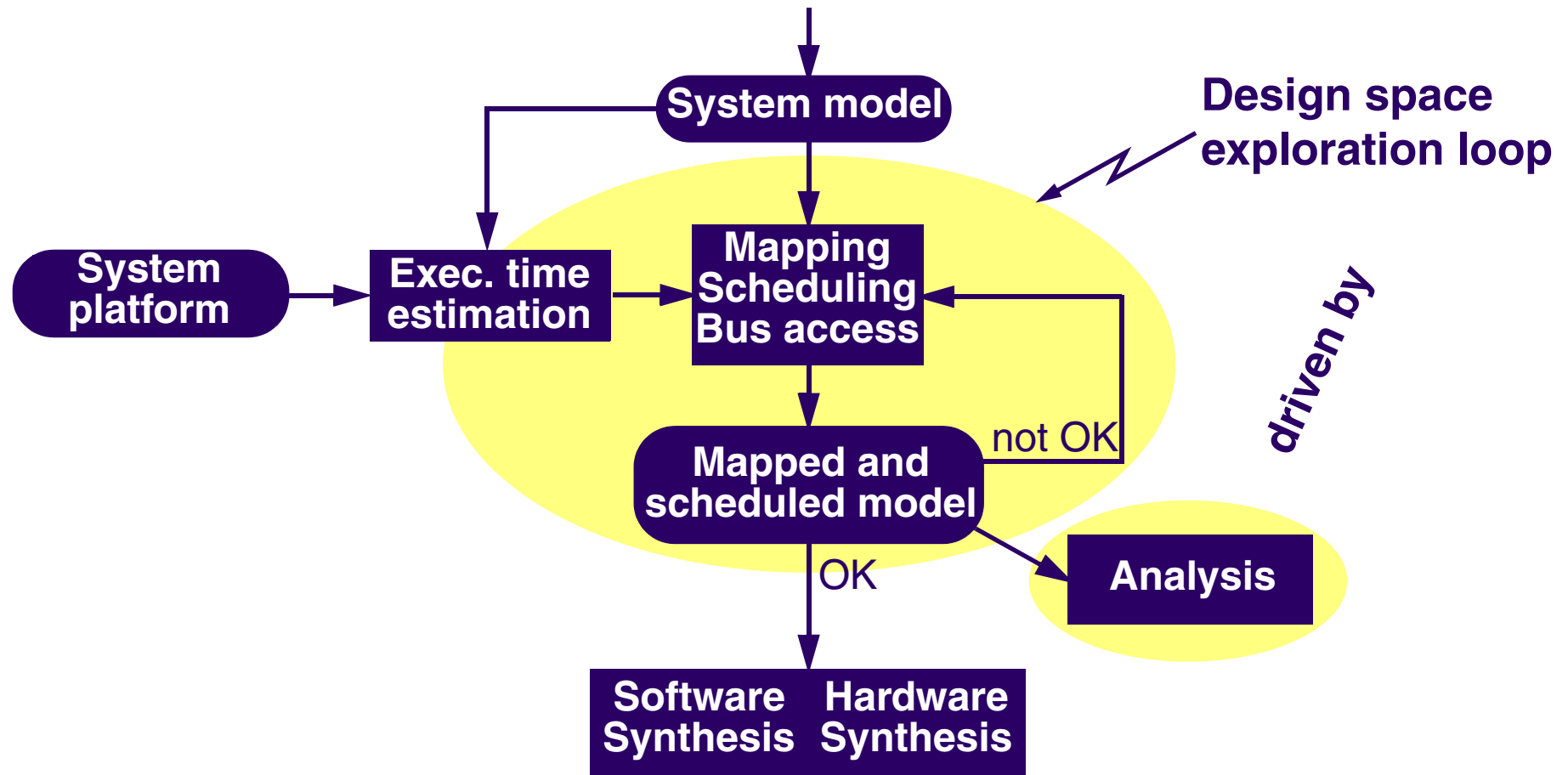


# System Level Design Flow





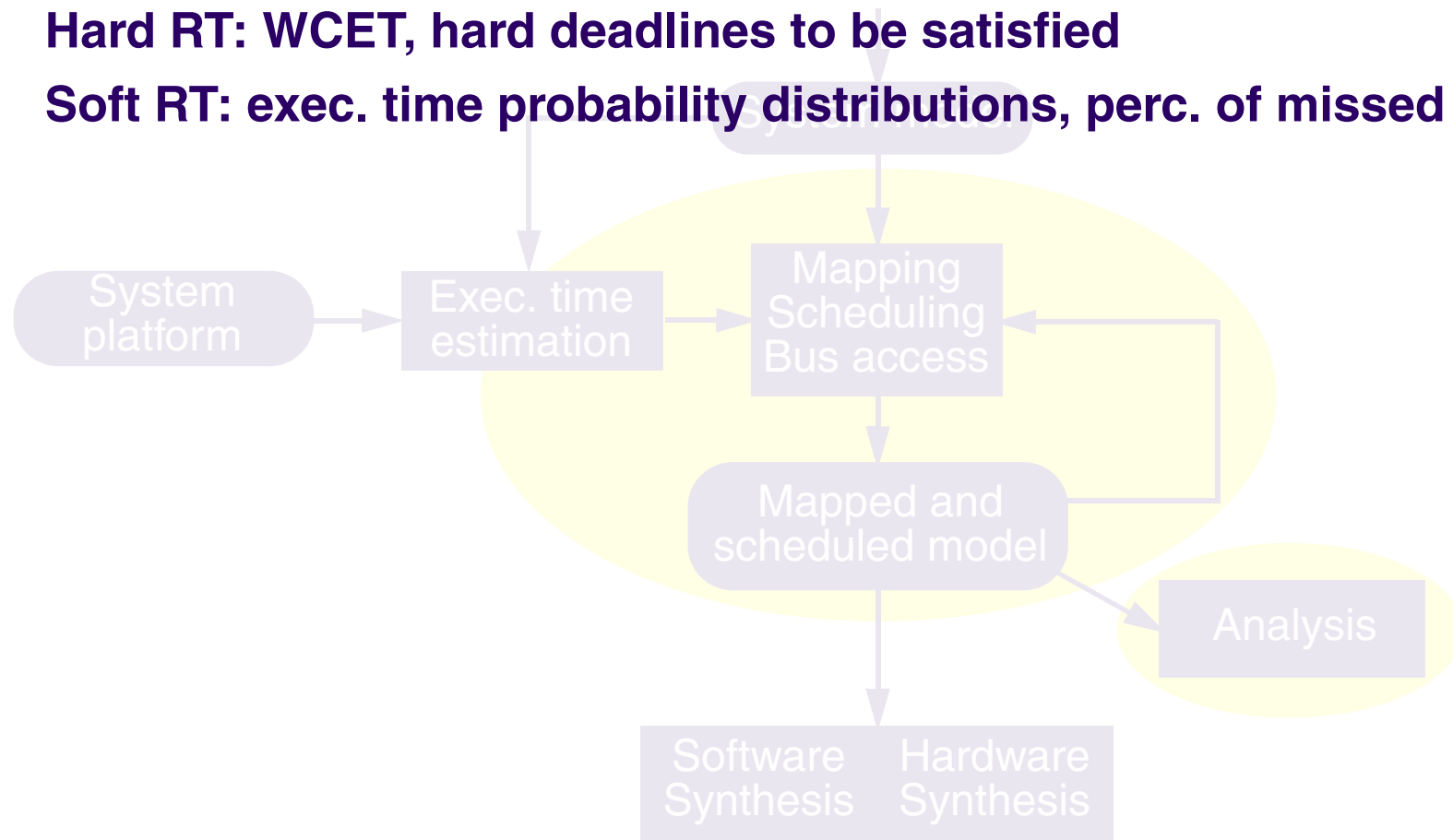
# System Level Design Flow



# System Level Design Flow

## ■ Category of applications:

- **Hard RT: WCET, hard deadlines to be satisfied**
- **Soft RT: exec. time probability distributions, perc. of missed deadlines**



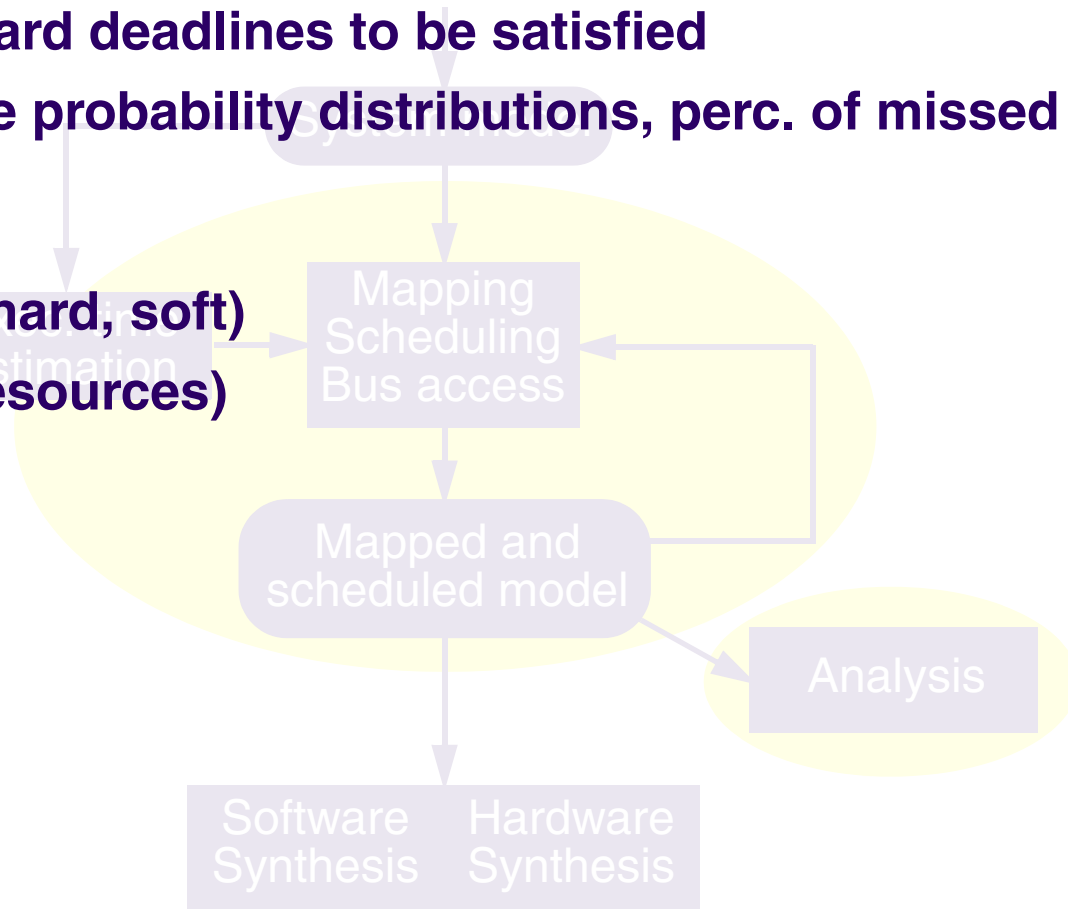
# System Level Design Flow

## ■ Category of applications:

- Hard RT: WCET, hard deadlines to be satisfied
- Soft RT: exec. time probability distributions, perc. of missed deadlines

## ■ Constraints:

- time constraints (hard, soft)
- cost (amount of resources)
- fault tolerance



# System Level Design Flow

## ■ Category of applications:

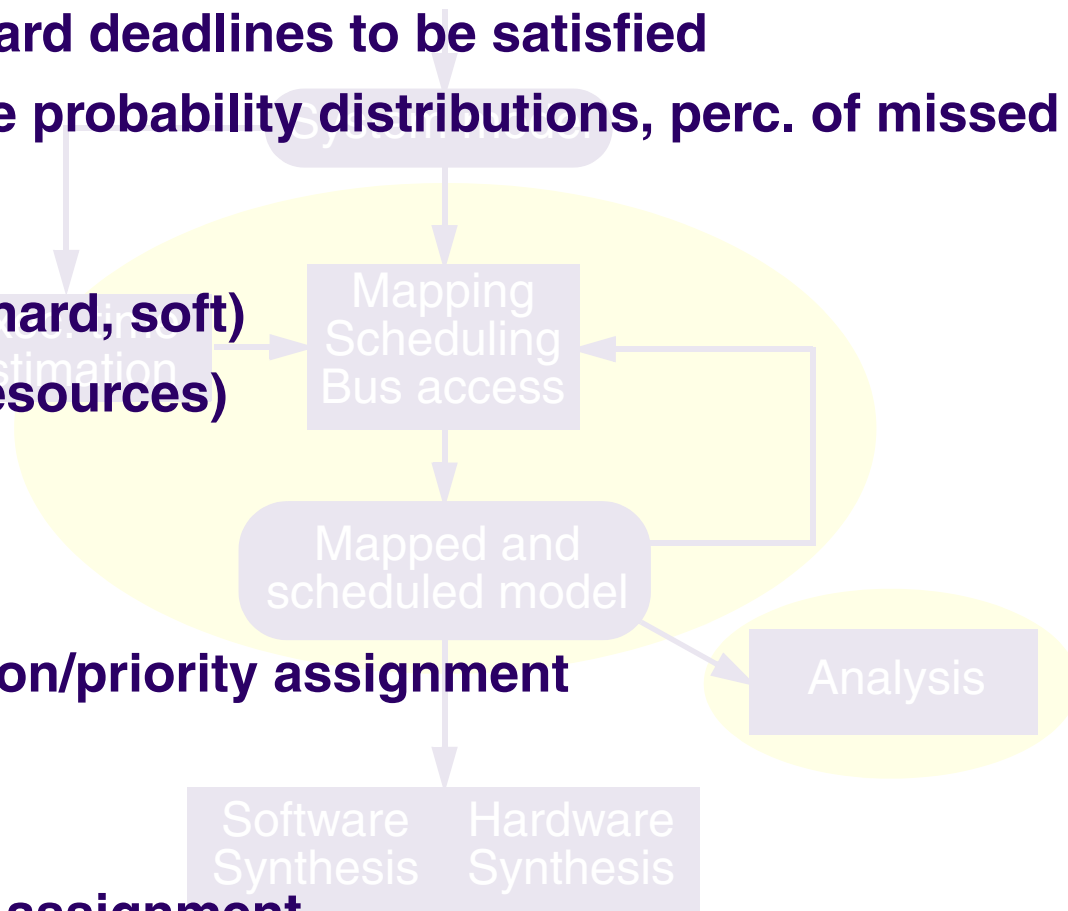
- Hard RT: WCET, hard deadlines to be satisfied
- Soft RT: exec. time probability distributions, perc. of missed deadlines

## ■ Constraints:

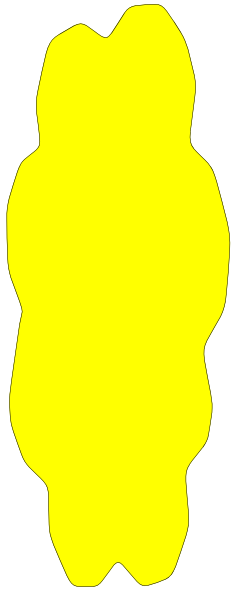
- time constraints (hard, soft)
- cost (amount of resources)
- fault tolerance

## ■ Optimization problems:

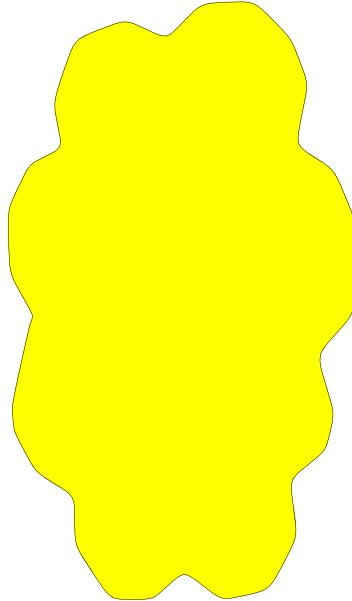
- schedule generation/priority assignment
- task mapping
- bus configuration
- scheduling policy assignment
- fault tolerance policy assignment



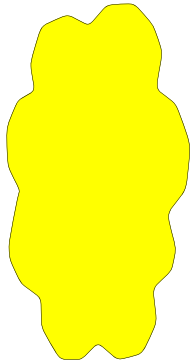
- ➡ An application is modelled as a set of task graphs:



$\Gamma_1$   
**Period:  $T_{\Gamma_1}$**   
**Deadline:  $D_{\Gamma_1}$**



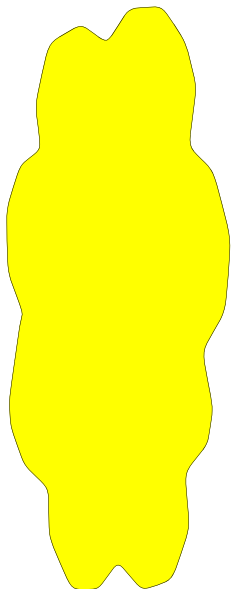
$\Gamma_2$   
**Period:  $T_{\Gamma_2}$**   
**Deadline:  $D_{\Gamma_2}$**



$\Gamma_3$   
**Period:  $T_{\Gamma_3}$**   
**Deadline:  $D_{\Gamma_3}$**



- 

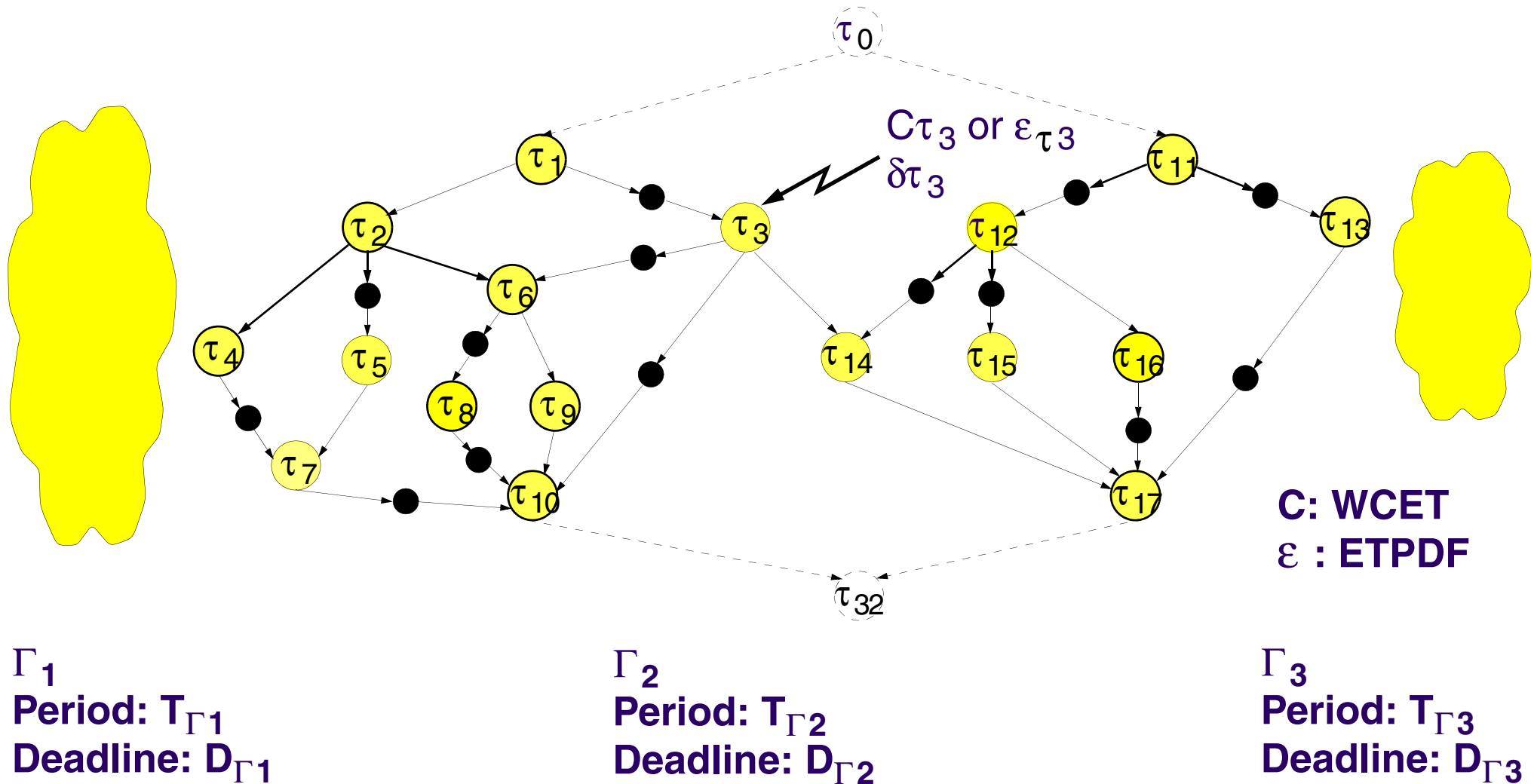
 $\Gamma_1$  $\Gamma_2$ 

**Г3**



# Application Model

- ☞ An application is modelled as a set of task graphs:



- **Distributed Embedded Systems**
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- **Application Model**
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  - **Heterogeneous Distributed Systems**
  - **Static and Dynamic Communication**
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# Distributed Hard Real-Time Systems



## ■ Given:

- WCET and BCET of each task
- Dimension of messages
- Deadlines for tasks/task graphs

☞ All deadlines have to be satisfied!



# Distributed Hard Real-Time Systems



## ■ Given:

- WCET and BCET of each task
- Dimension of messages
- Deadlines for tasks/task graphs

☞ All deadlines have to be satisfied!

## ■ Particular issues taken into consideration

- Heterogeneous nature of the system
- Various communication protocols

☞ Try to satisfy constraints at low cost!

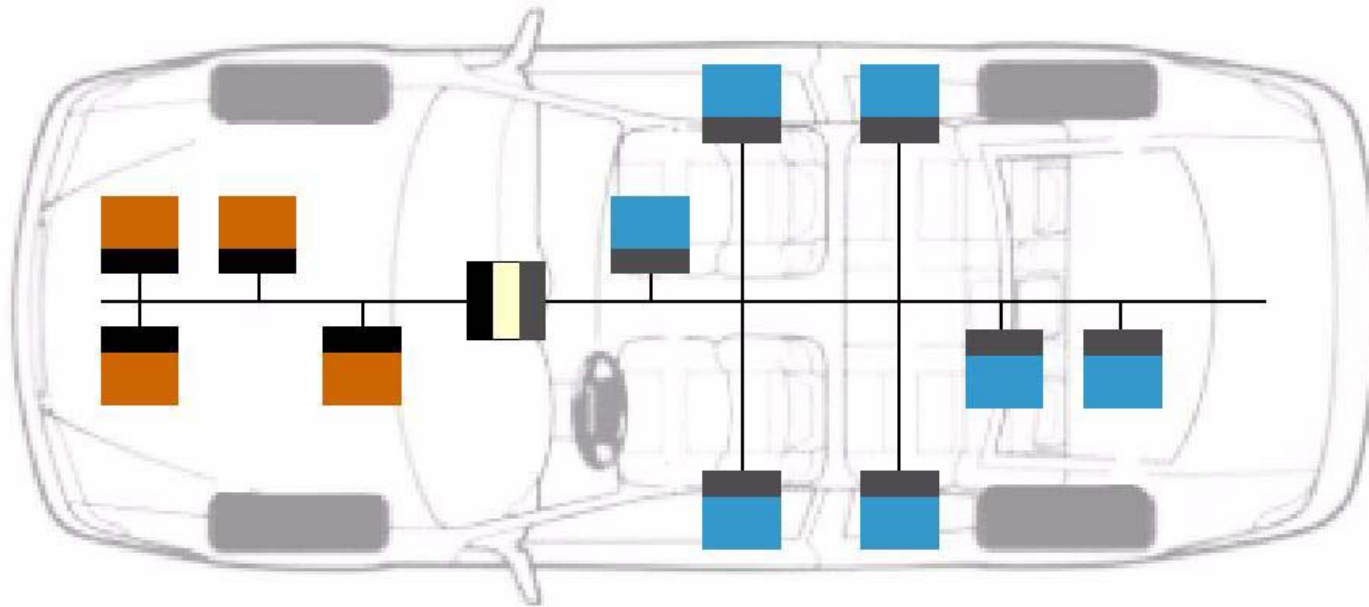


# Application Area

Automatic  
Cruise Control

Anti-lock Breaking  
System

Electronic  
Stability Program



Engine  
Control

Powertrain  
Control

Acceleration  
Skid Control



# Heterogeneous Distributed Embedded Systems



- RT Design Approach

- Network Protocol



# Heterogeneous Distributed Embedded Systems



- RT Design Approach
  - Time triggered
  - Event triggered

- Network Protocol



# Heterogeneous Distributed Embedded Systems



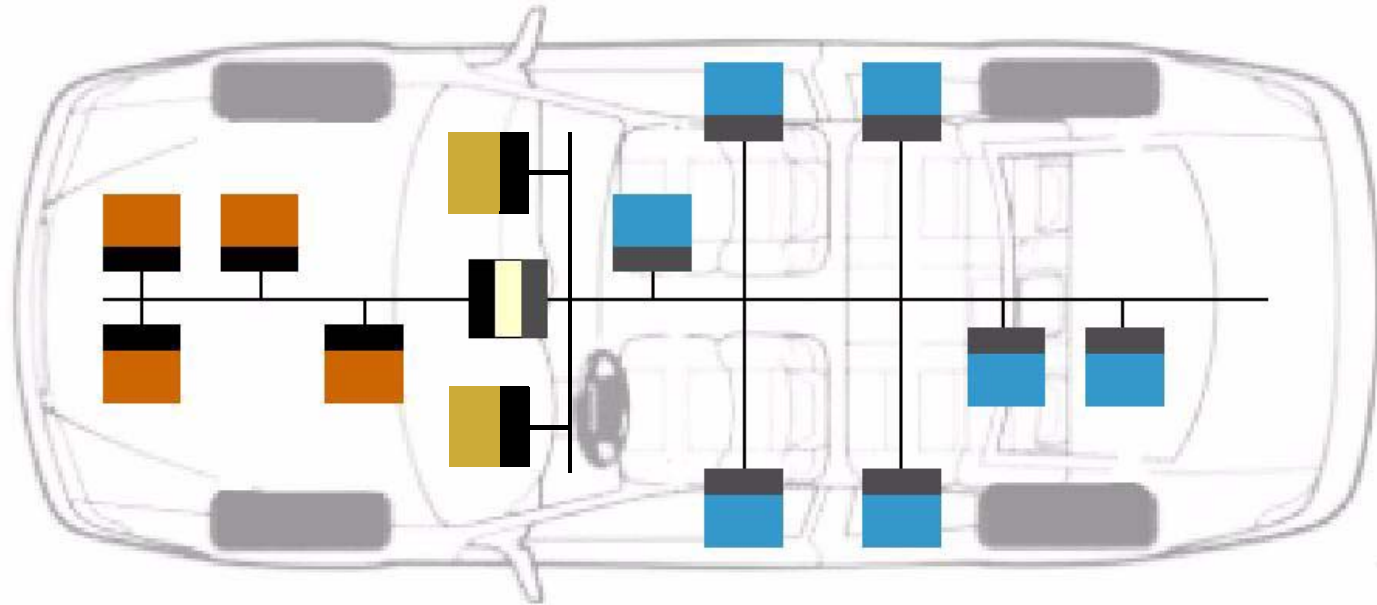
- **RT Design Approach**
  - Time triggered
  - Event triggered

- **Network Protocol**
  - Static
  - Dynamic



# Heterogeneous Distributed Embedded Systems

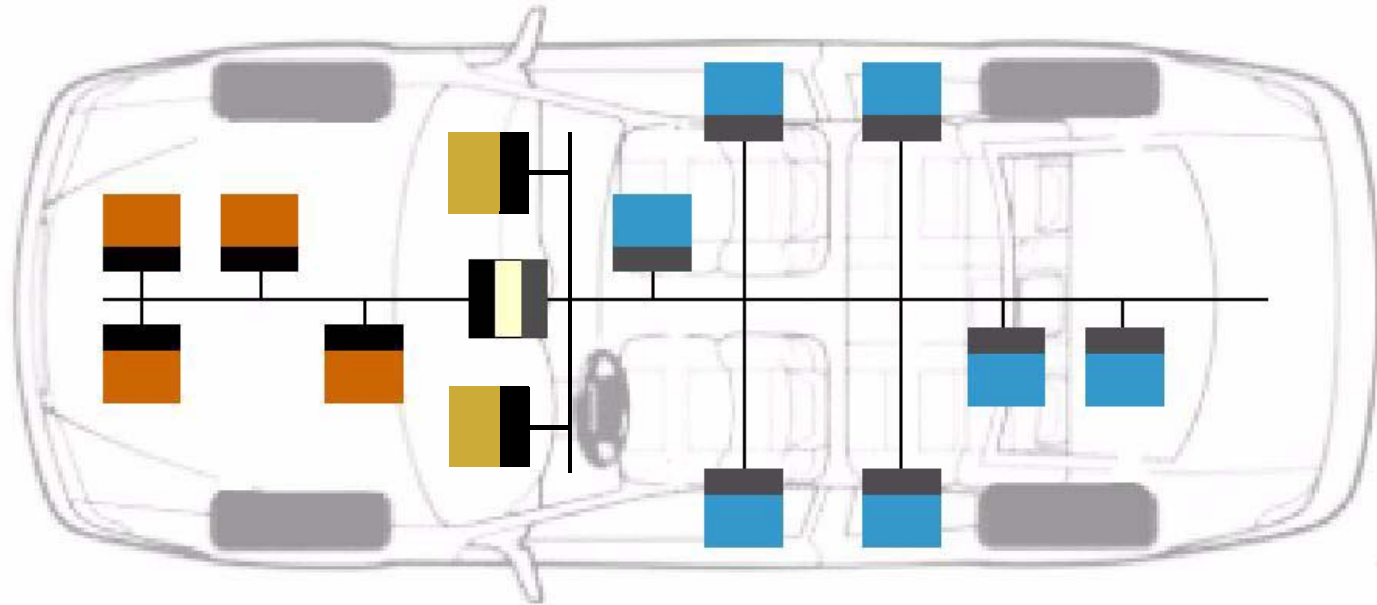
## ➡ Heterogeneous Nature of Implemented Functions



# Heterogeneous Distributed Embedded Systems

## Engine Control

■ hard real-time





# Heterogeneous Distributed Embedded Systems

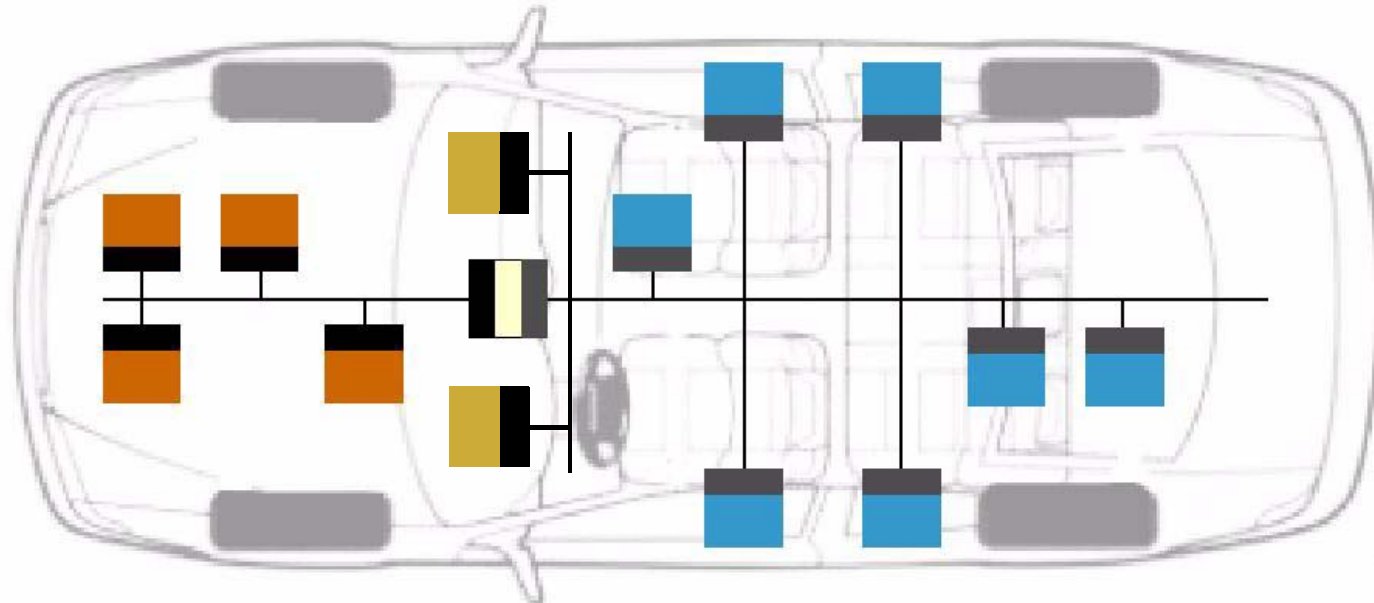
## Engine Control

- hard real-time



## Power Train (break-by-wire, ABS)

- hard real-time
- highly safety-critical



# Heterogeneous Distributed Embedded Systems

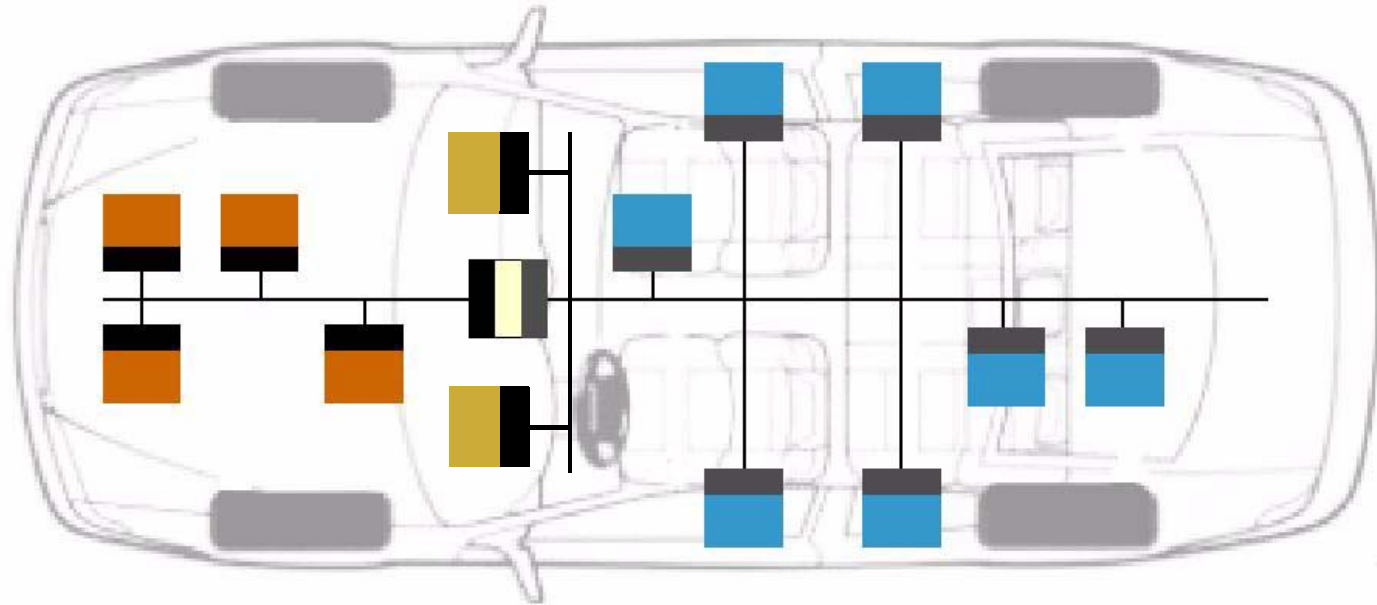
## Engine Control

- hard real-time



## Power Train (break-by-wire, ABS)

- hard real-time
- highly safety-critical

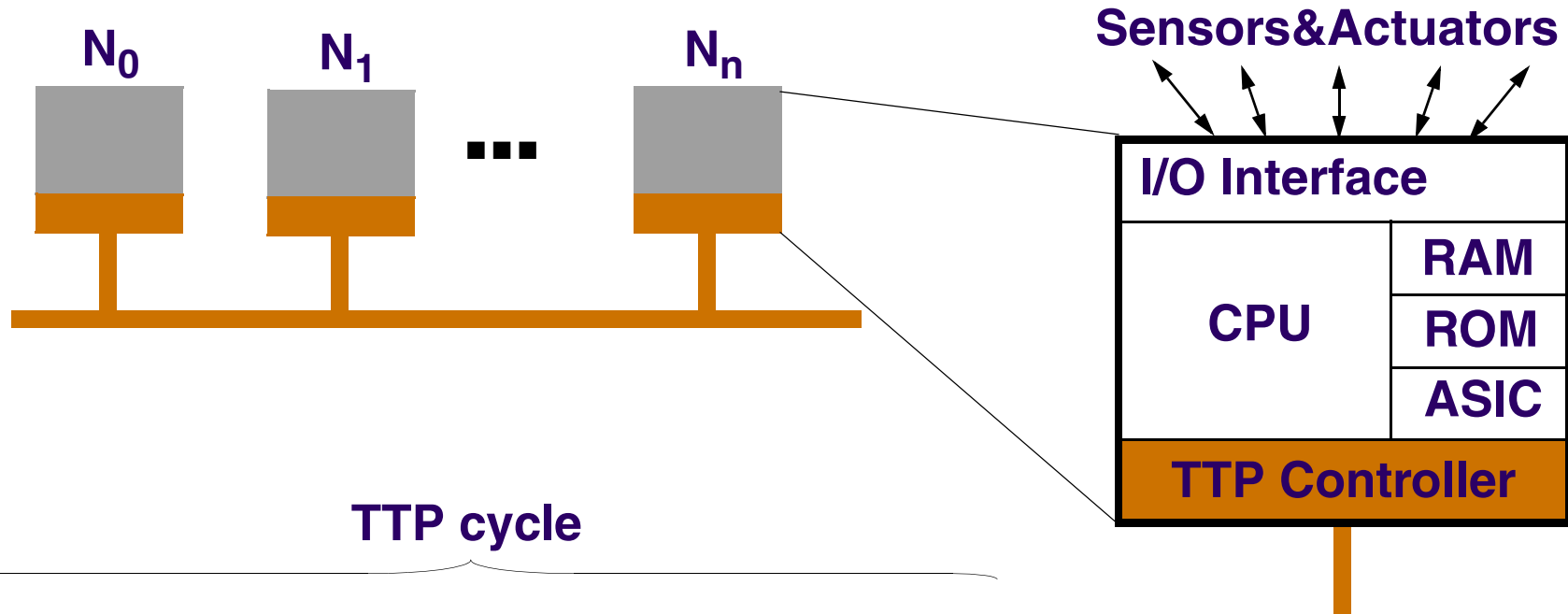


## Air Conditioning

- soft real-time



# Static Communication: TTP

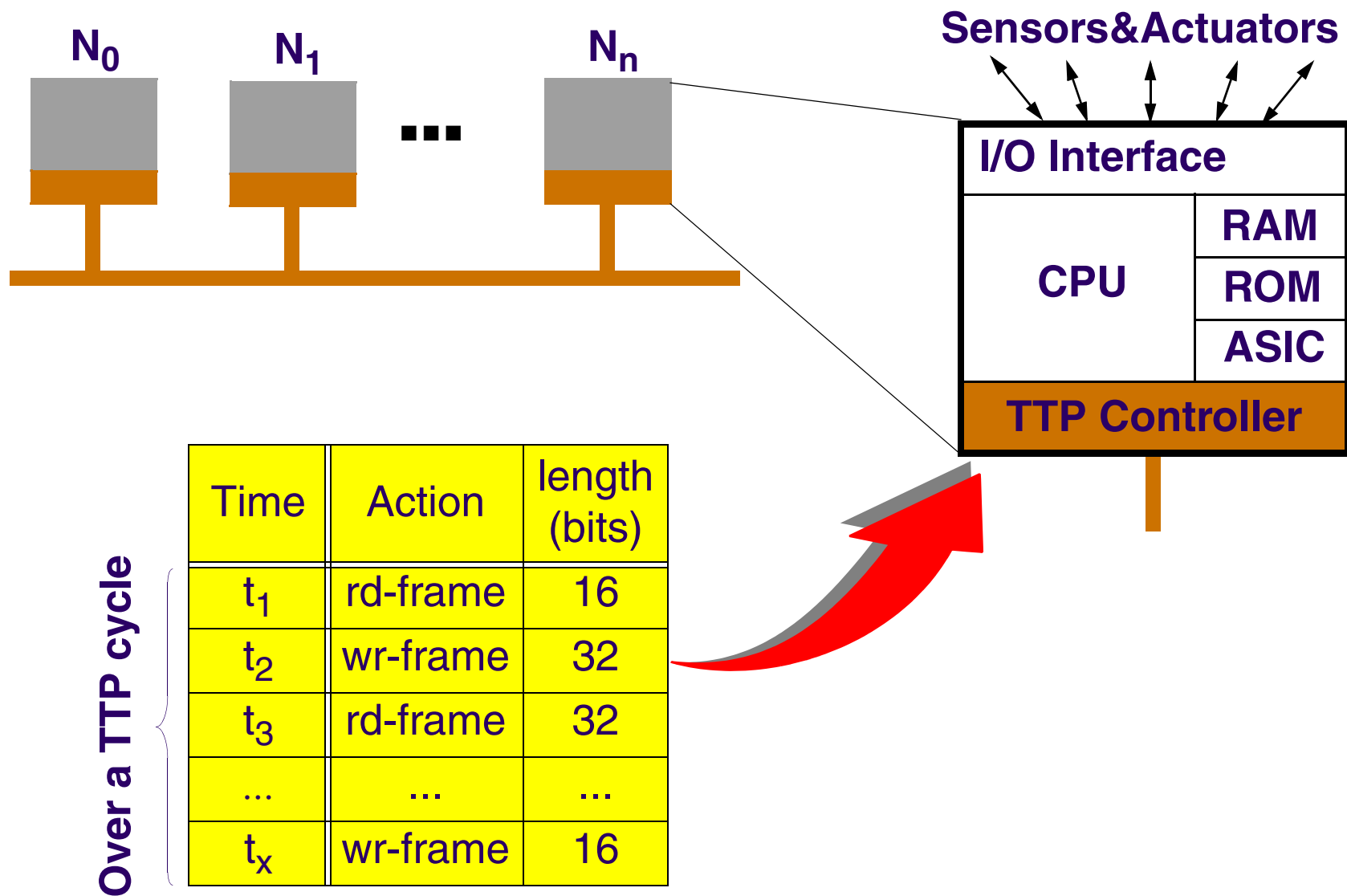


$N_0$  writes  $N_1$  writes

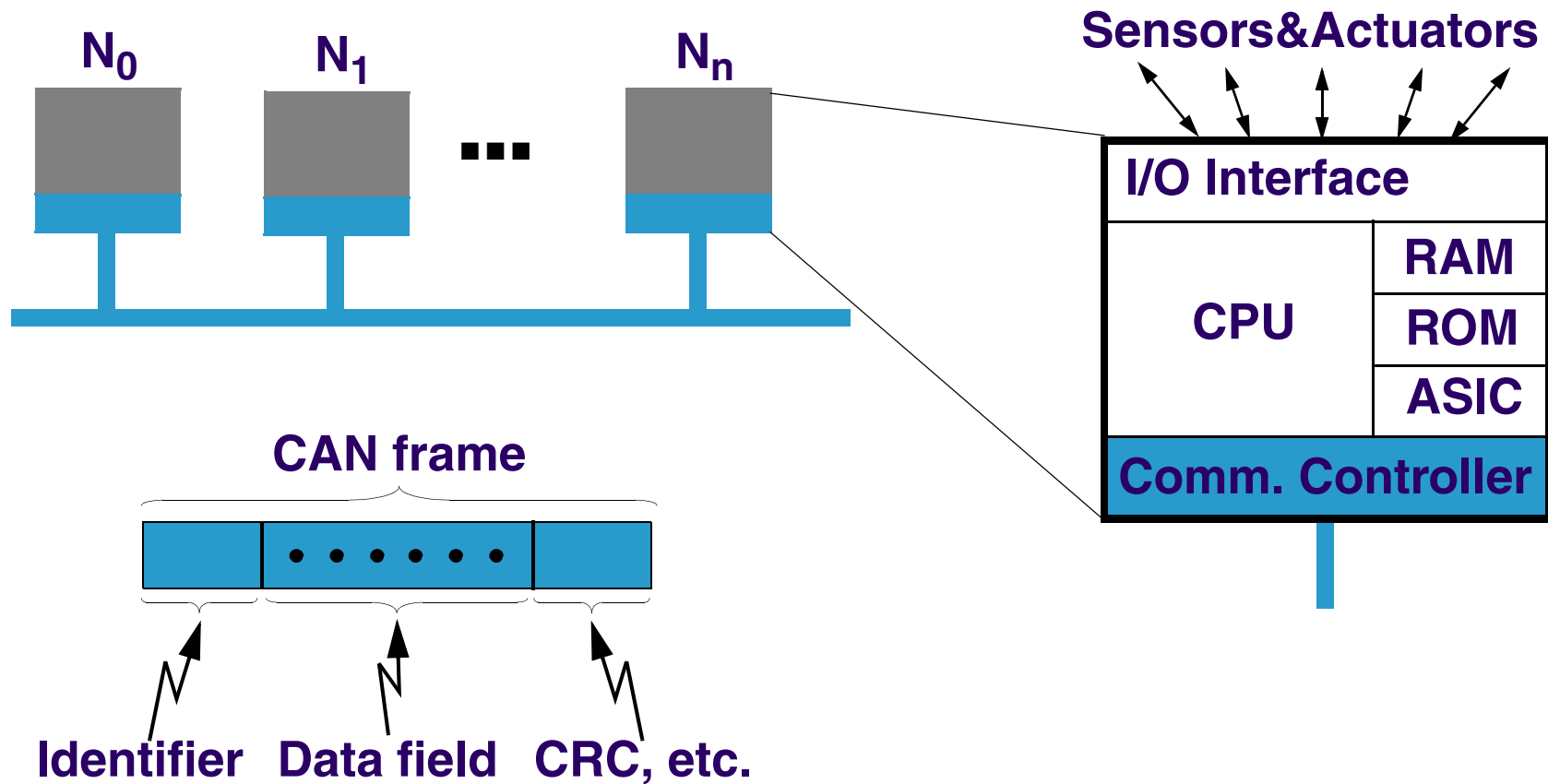
left empty in  
this round



# Static Communication: TTP



# Dynamic Communication: CAN

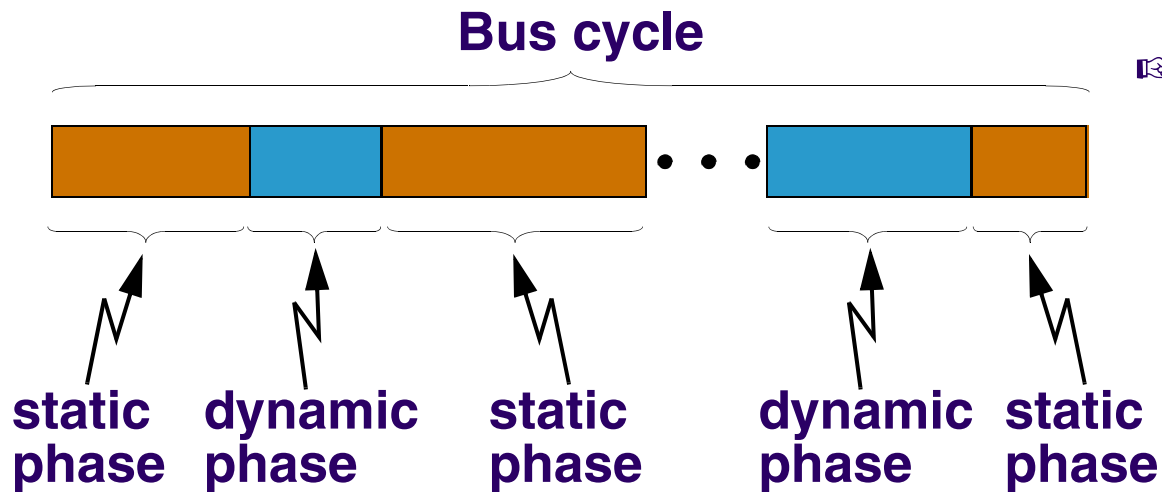
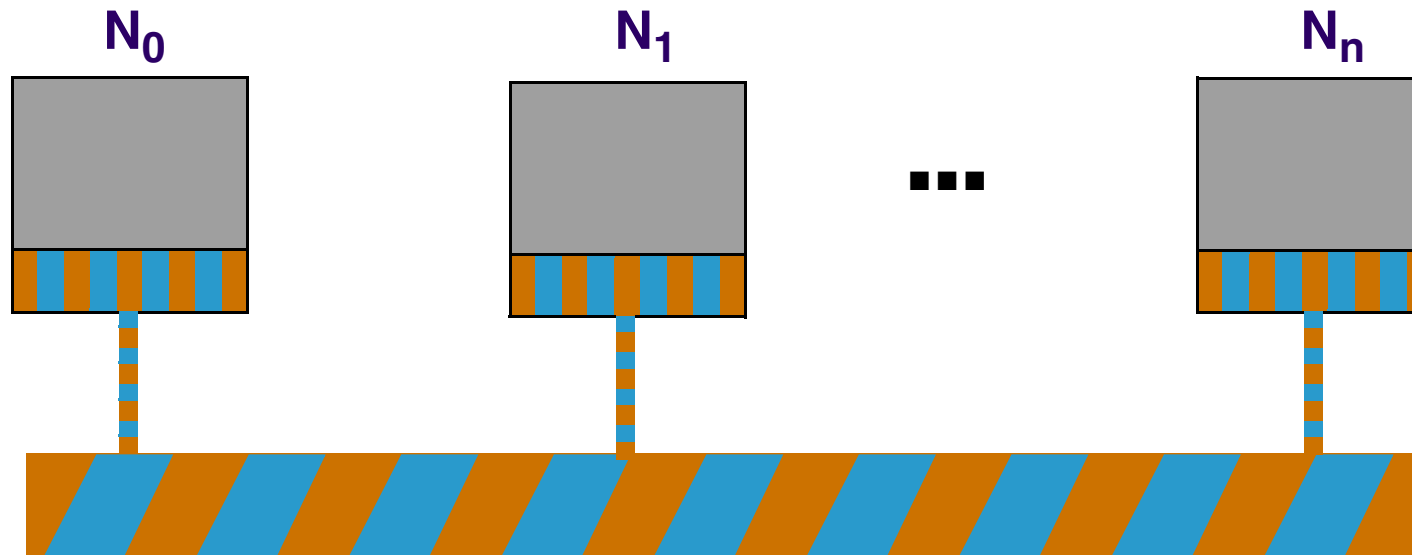


## ■ Priority bus with collision avoidance mechanism:

The node that transmits the highest priority frame wins the contention.



# Mixed Communication: UCM

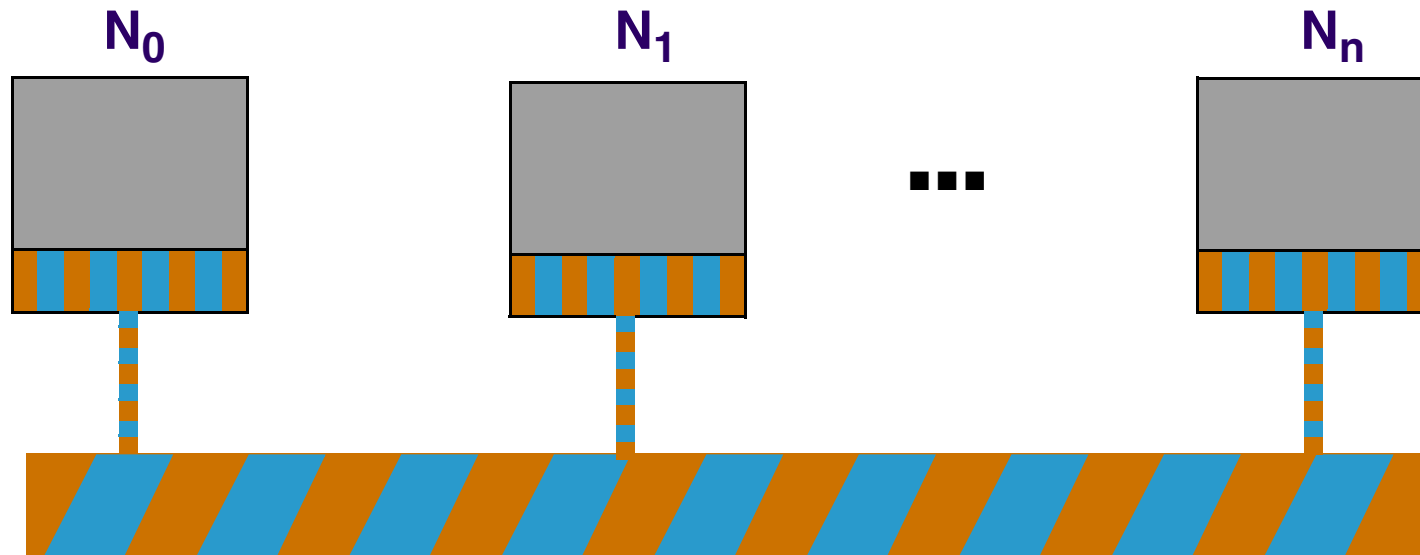


## Universal Communication Model

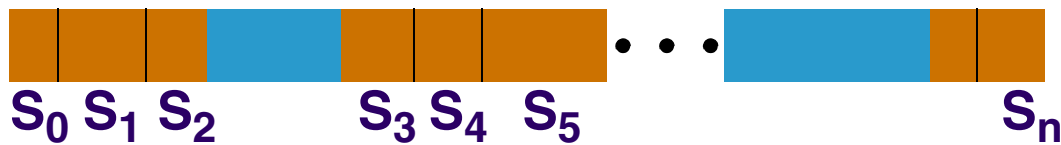
- Static phase: TDMA
- Dynamic phase: CAN



# Mixed Communication: UCM



Bus cycle

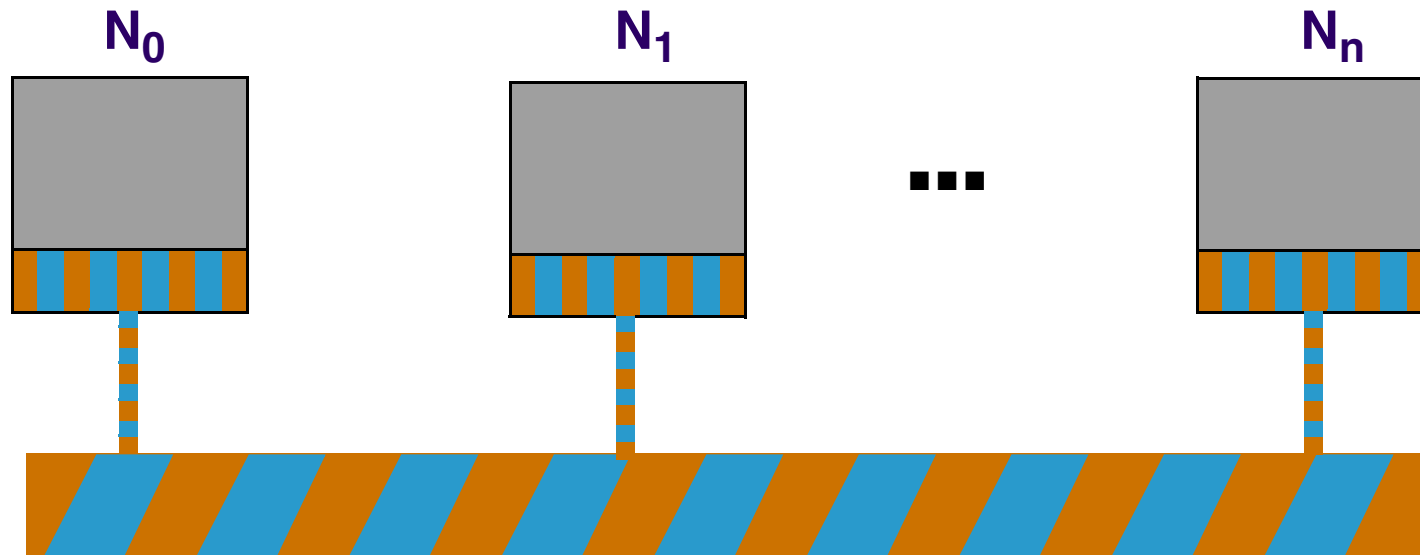


➡ Universal Communication Model

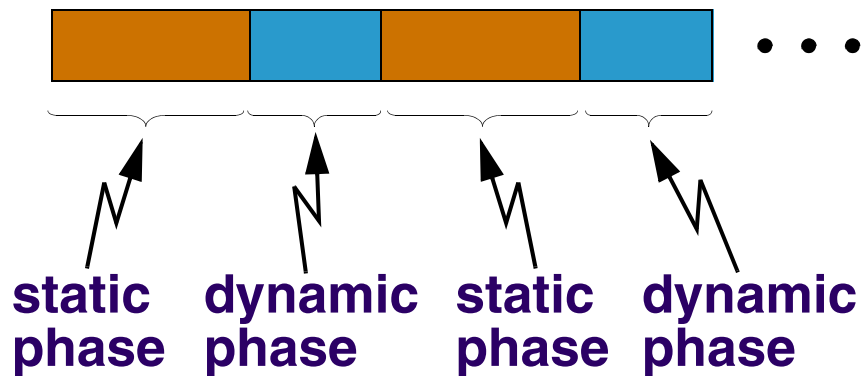
- Static phase: TDMA
- Dynamic phase: CAN



# Mixed Communication: FlexRay



## Bus cycle



## FlexRay

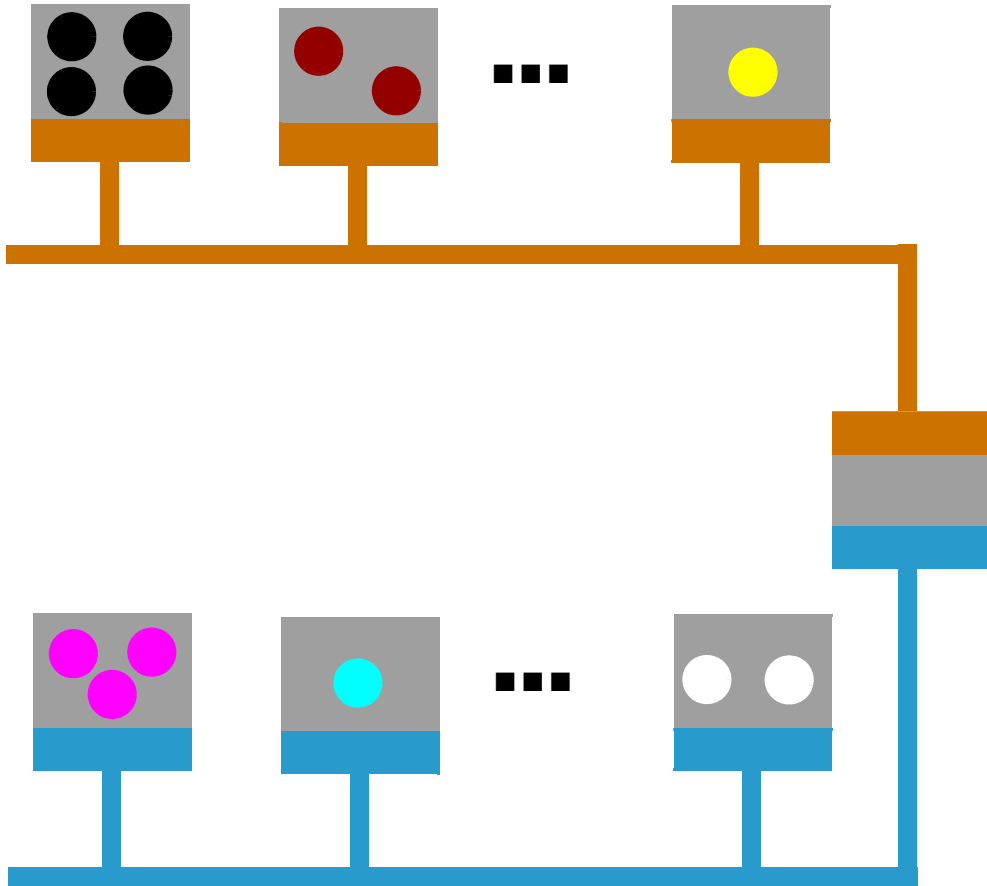
- Static phase: TDMA
- Dynamic phase: Flexible TDMA



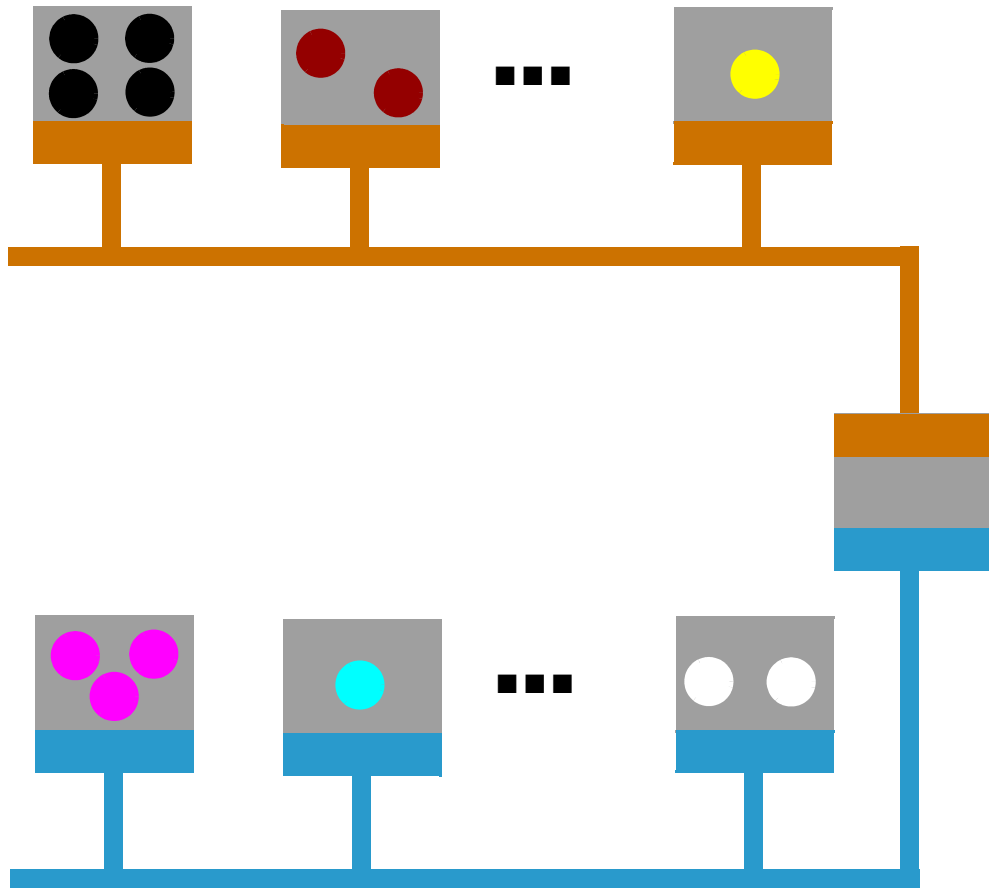


# The Traditional Approach

One node  $\longleftrightarrow$  One function



# The Traditional Approach



One node  $\longleftrightarrow$  One function

- Purchase node&function and integrate into system
- Sophistication grew quickly



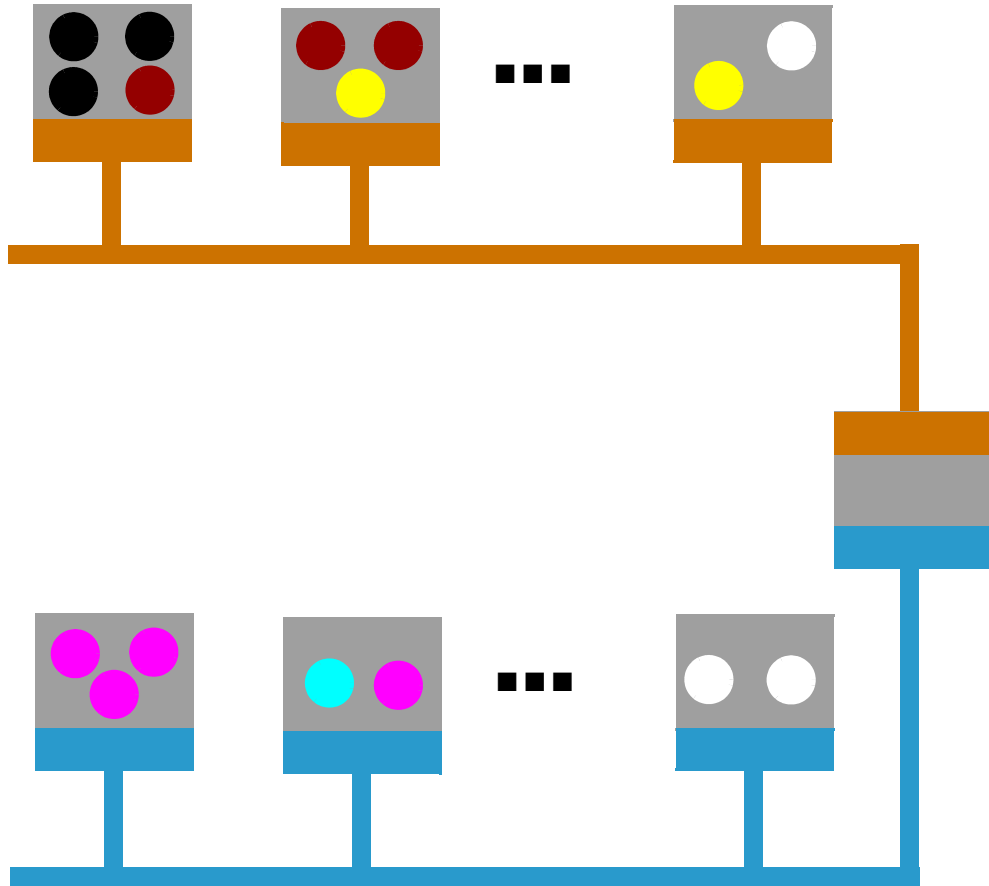
More than 100 nodes



Resources have to be used more efficiently



# What Comes



One node  $\longleftrightarrow$  Several functions

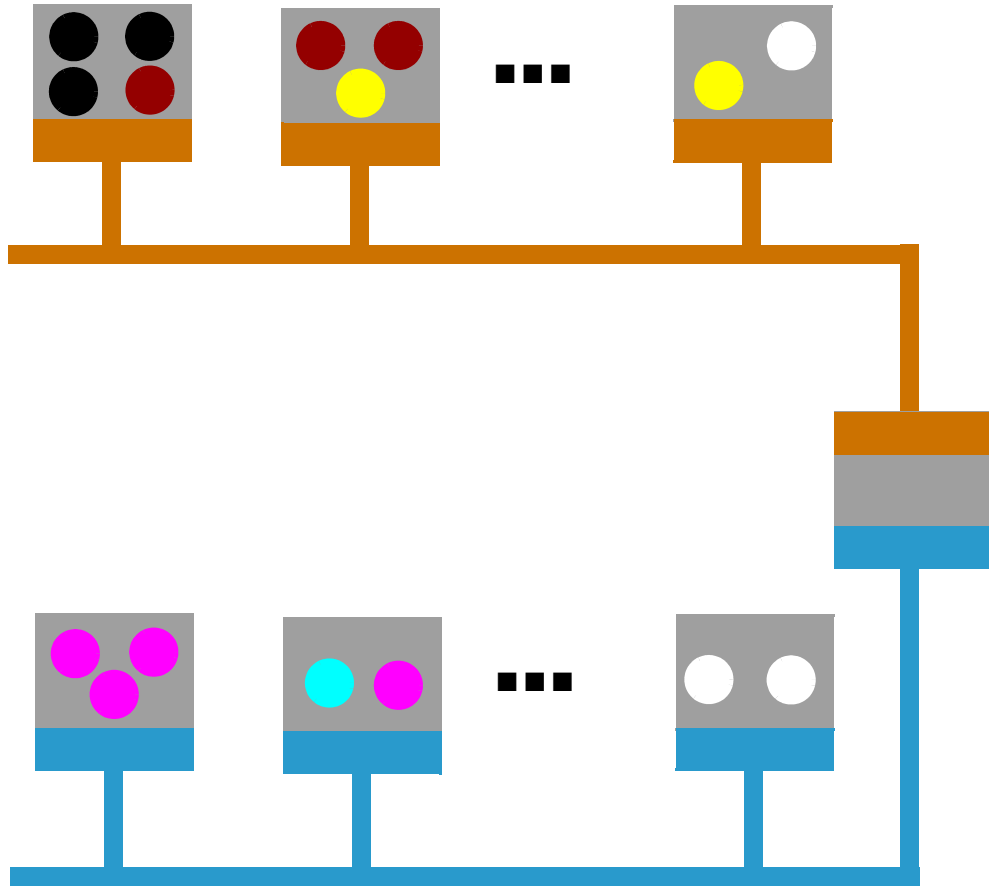
Several nodes  $\longleftrightarrow$  One function

## Flexibility!

- Reduce cost
- Improve resource usage
- Function close to sensor



# What Comes



One node  $\longleftrightarrow$  Several functions

Several nodes  $\longleftrightarrow$  One function

## Flexibility!

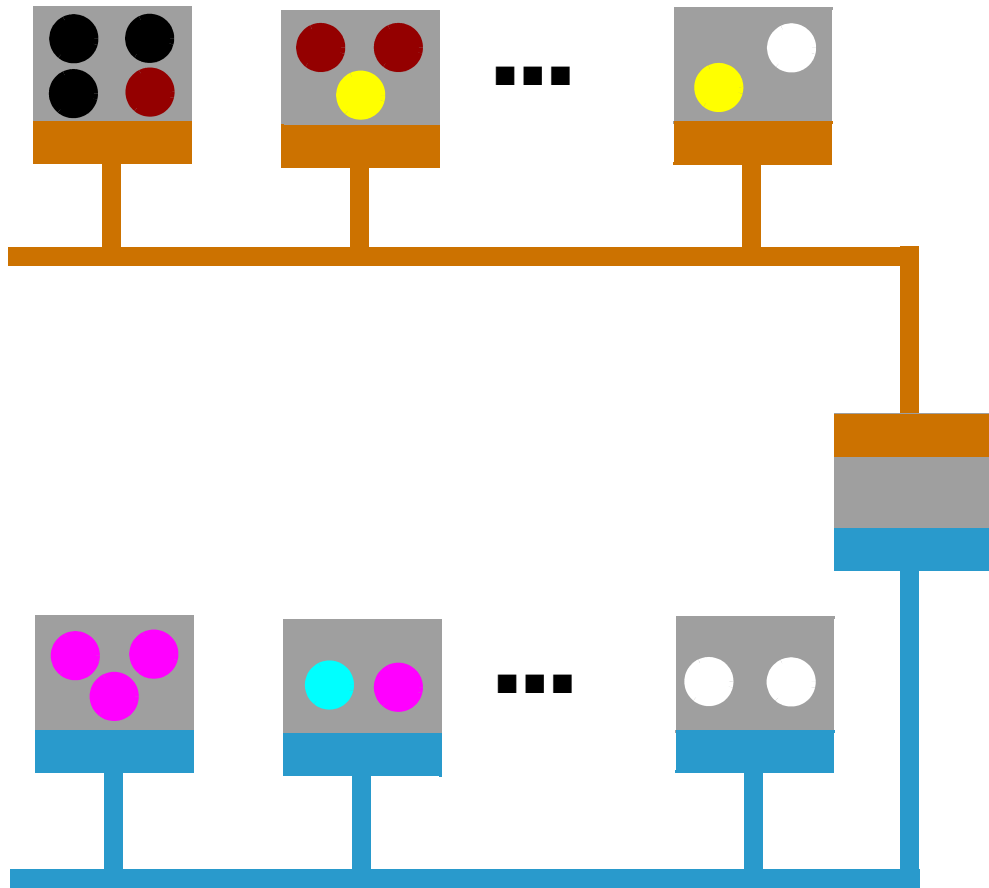
- Reduce cost
- Improve resource usage
- Function close to sensor

👉 Needed:

- Middleware software
- New analysis
- New system optimization



# What Comes



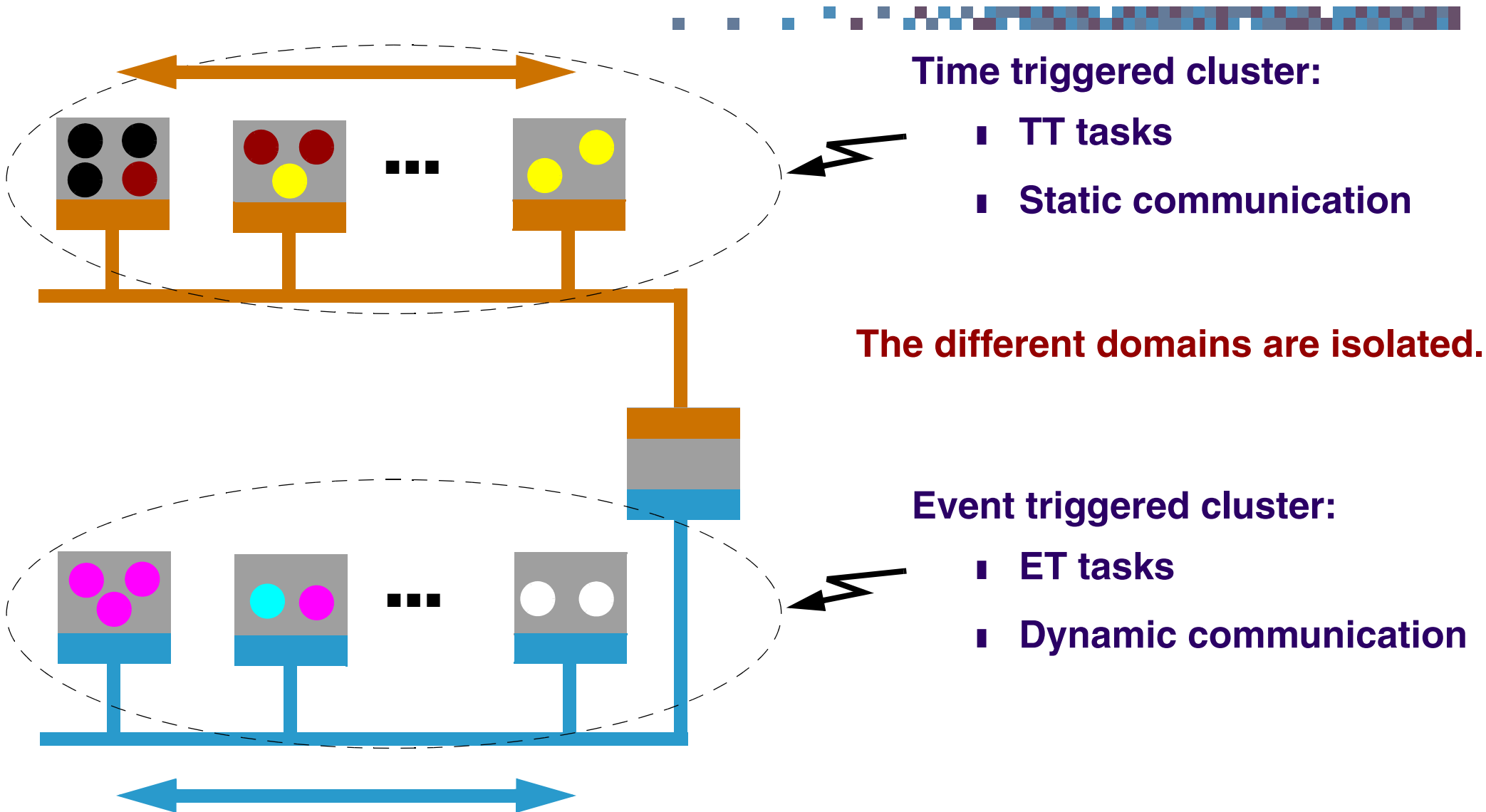
Navet et al.

*Trends in Automotive Communication Systems*

Proceedings of the IEEE, June 2005.



# Isolated Domains



The TT & ET, Static & Dynamic domains are interacting because:

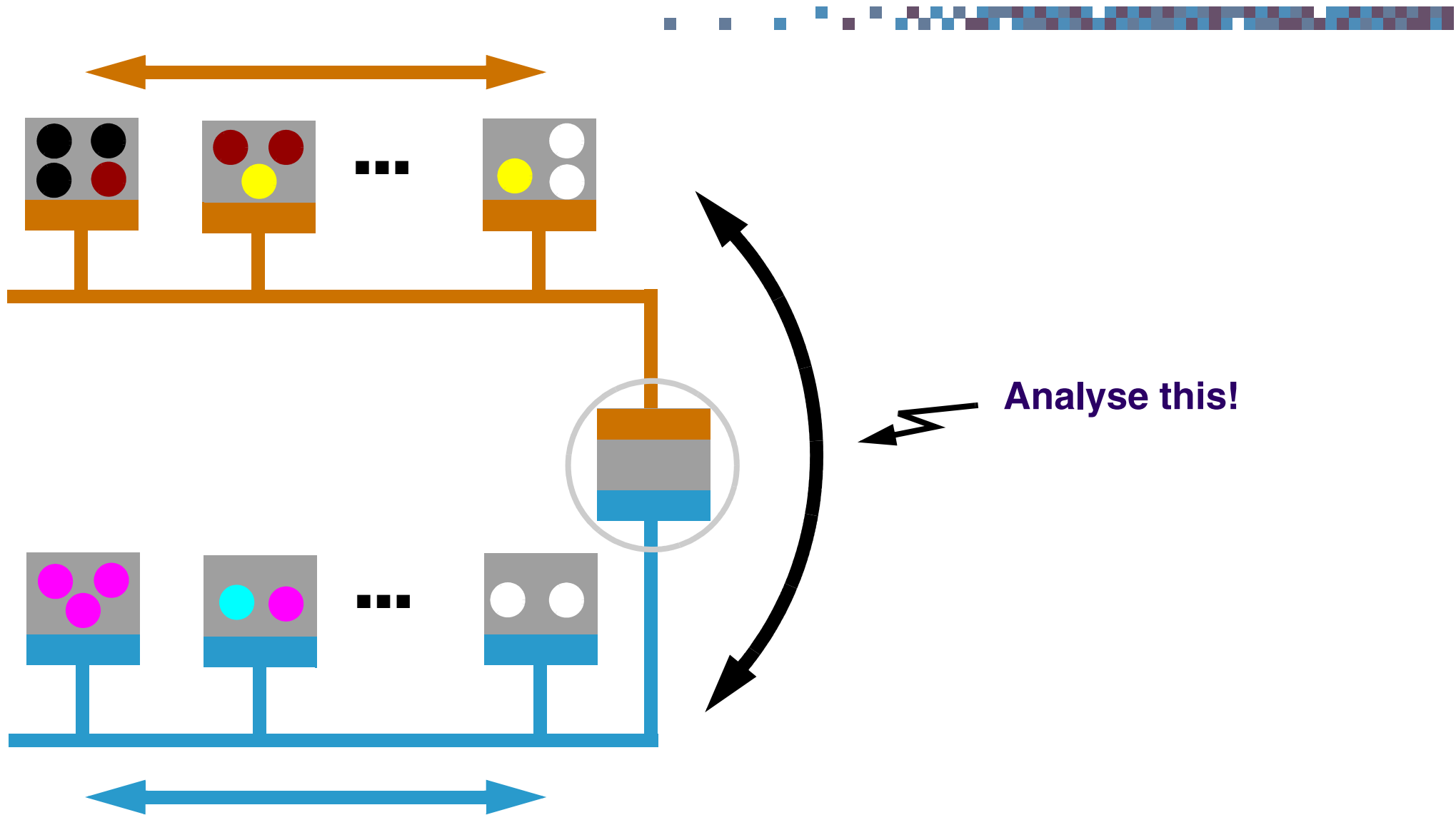
- They share resources (node, bus)

and/or

- They communicate

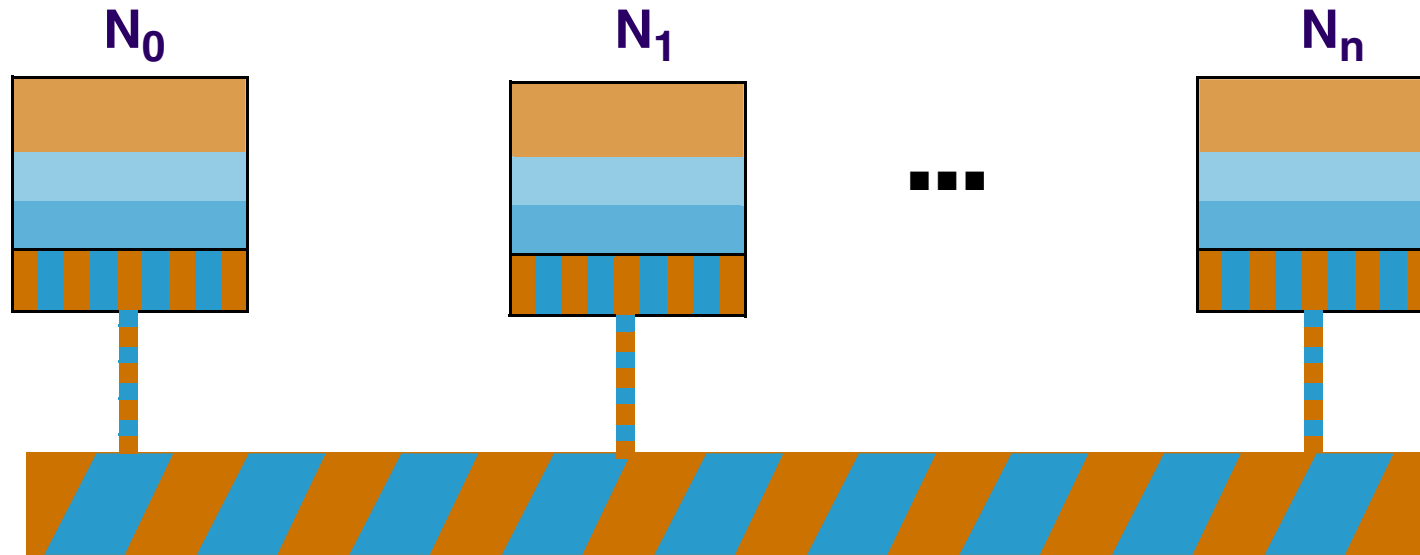


# Multi-cluster Heterogeneous Distributed Architecture

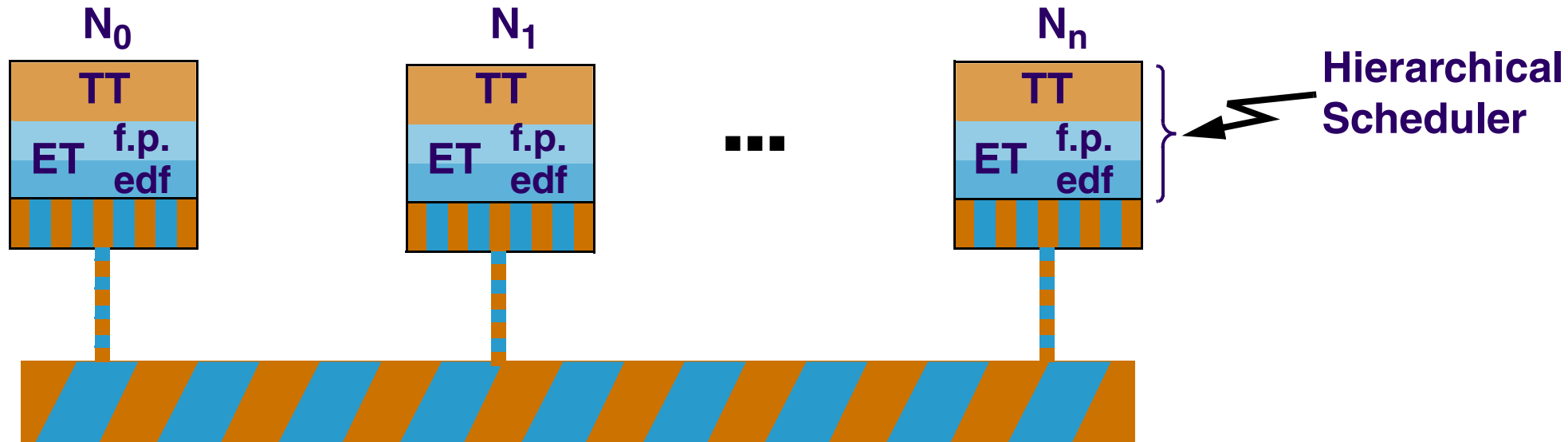




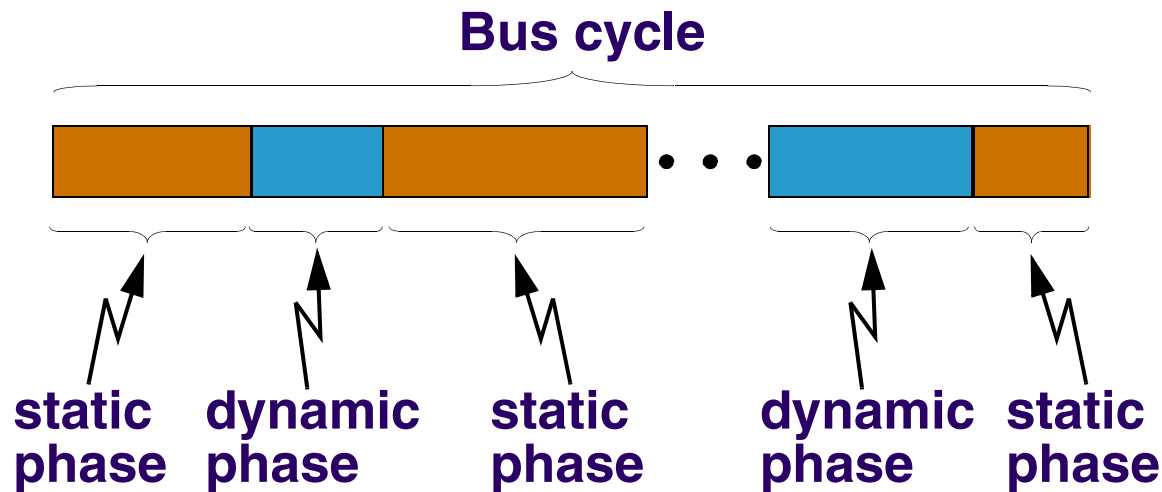
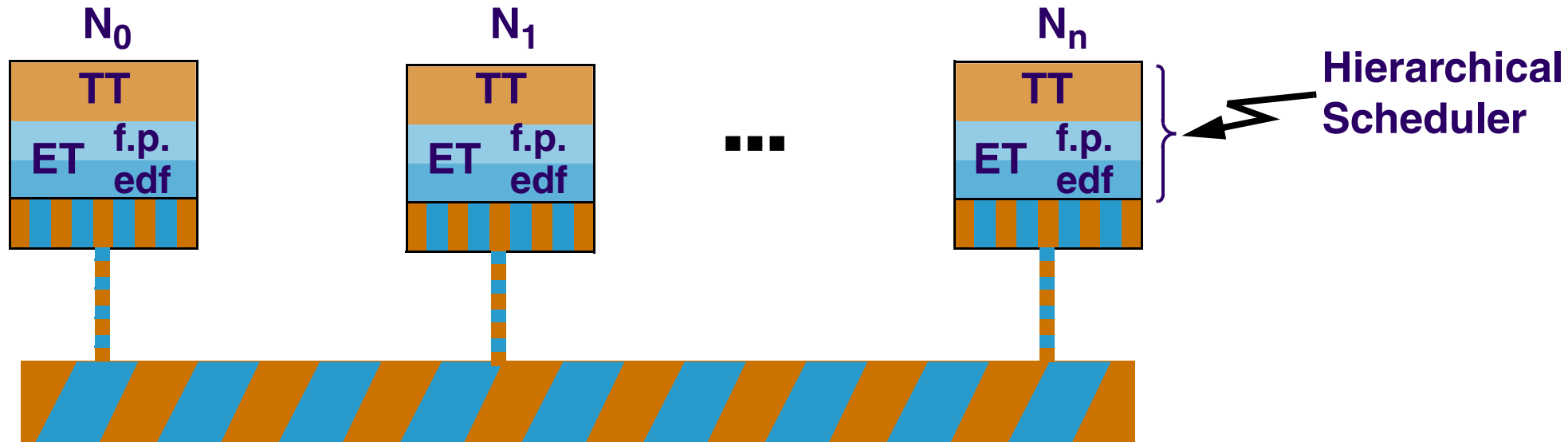
# Single-cluster Heterogeneous Distributed Architecture



# Single-cluster Heterogeneous Distributed Architecture



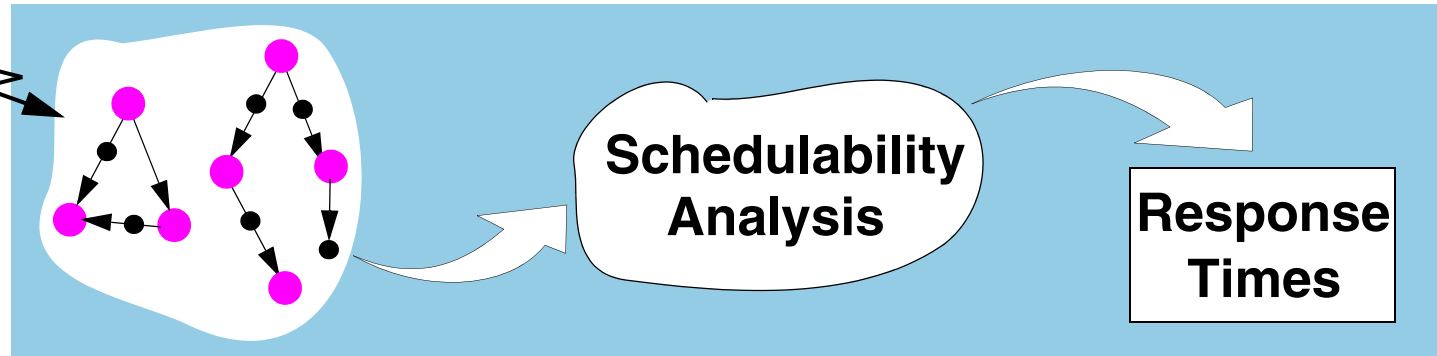
# Single-cluster Heterogeneous Distributed Architecture



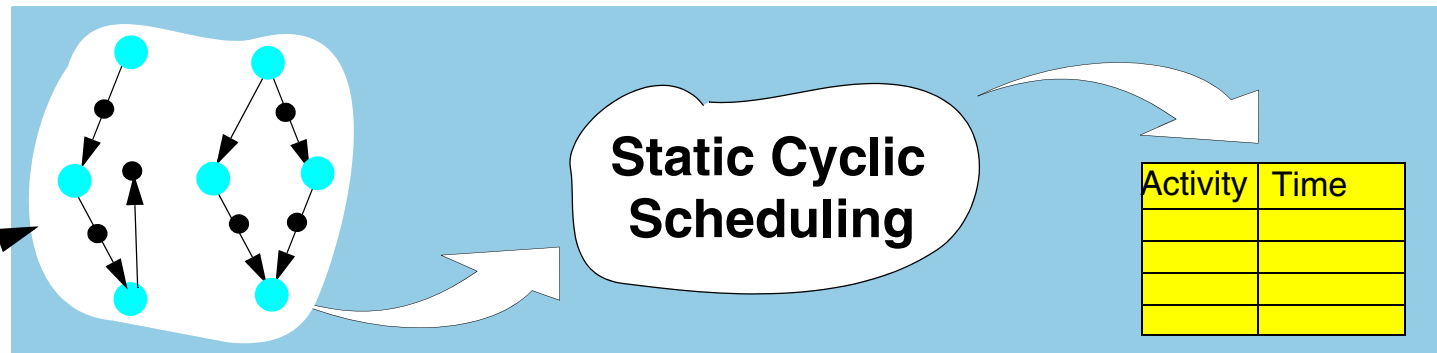
- UCM (TTP&CAN)
- FlexRay

## Isolated Domains

ET tasks  
DYN messages

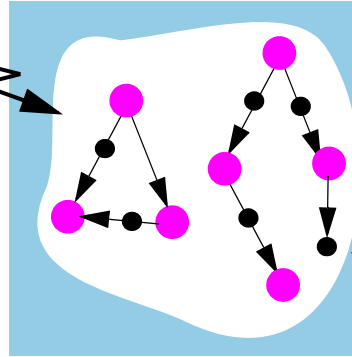


TT tasks  
ST messages



## ☞ Resource sharing, no communication

ET tasks  
DYN messages

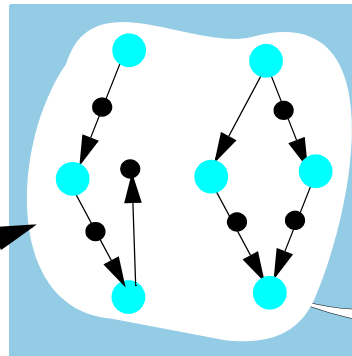


Schedulability  
Analysis

Response  
Times

Slacks

TT tasks  
ST messages

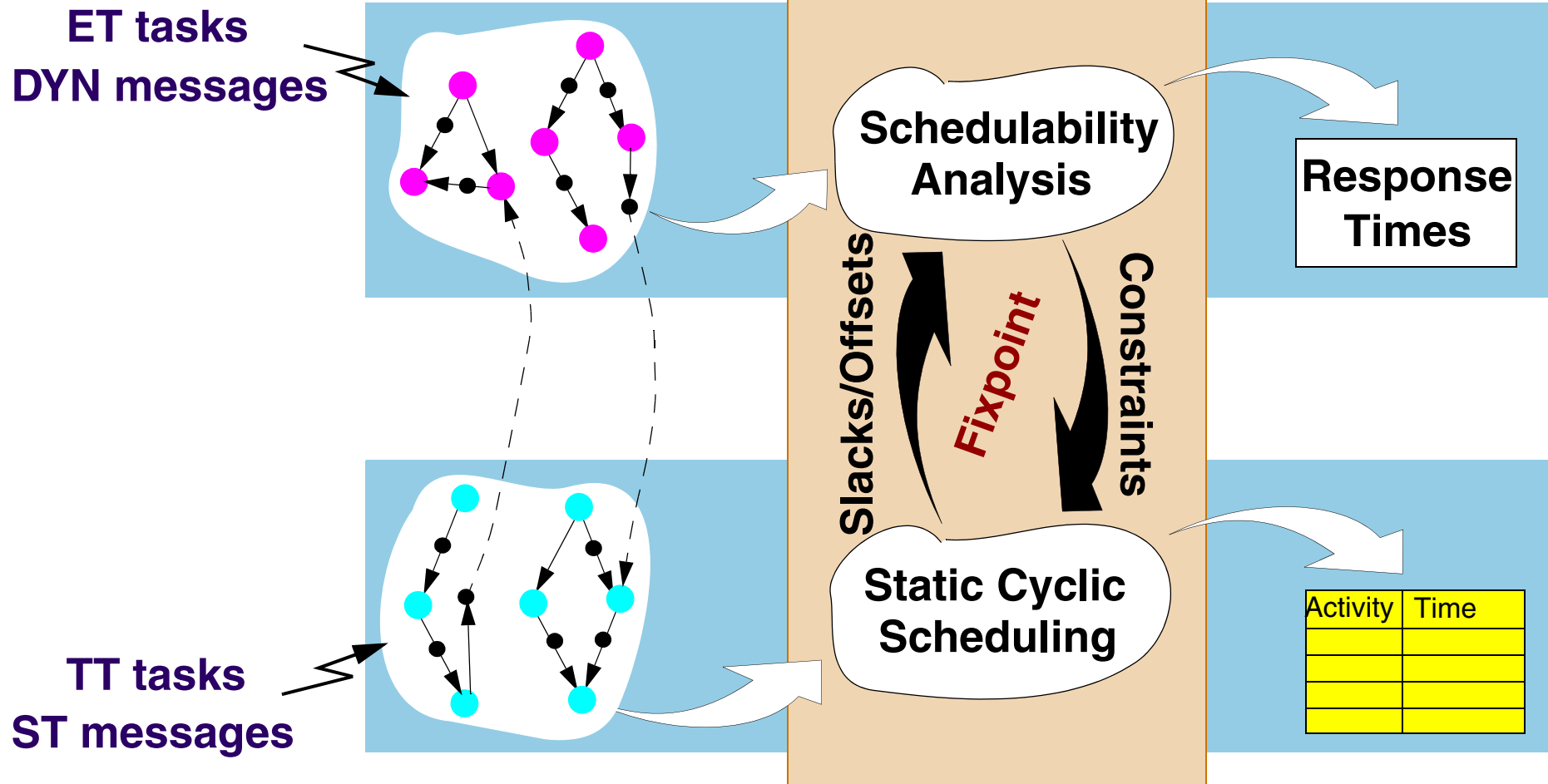


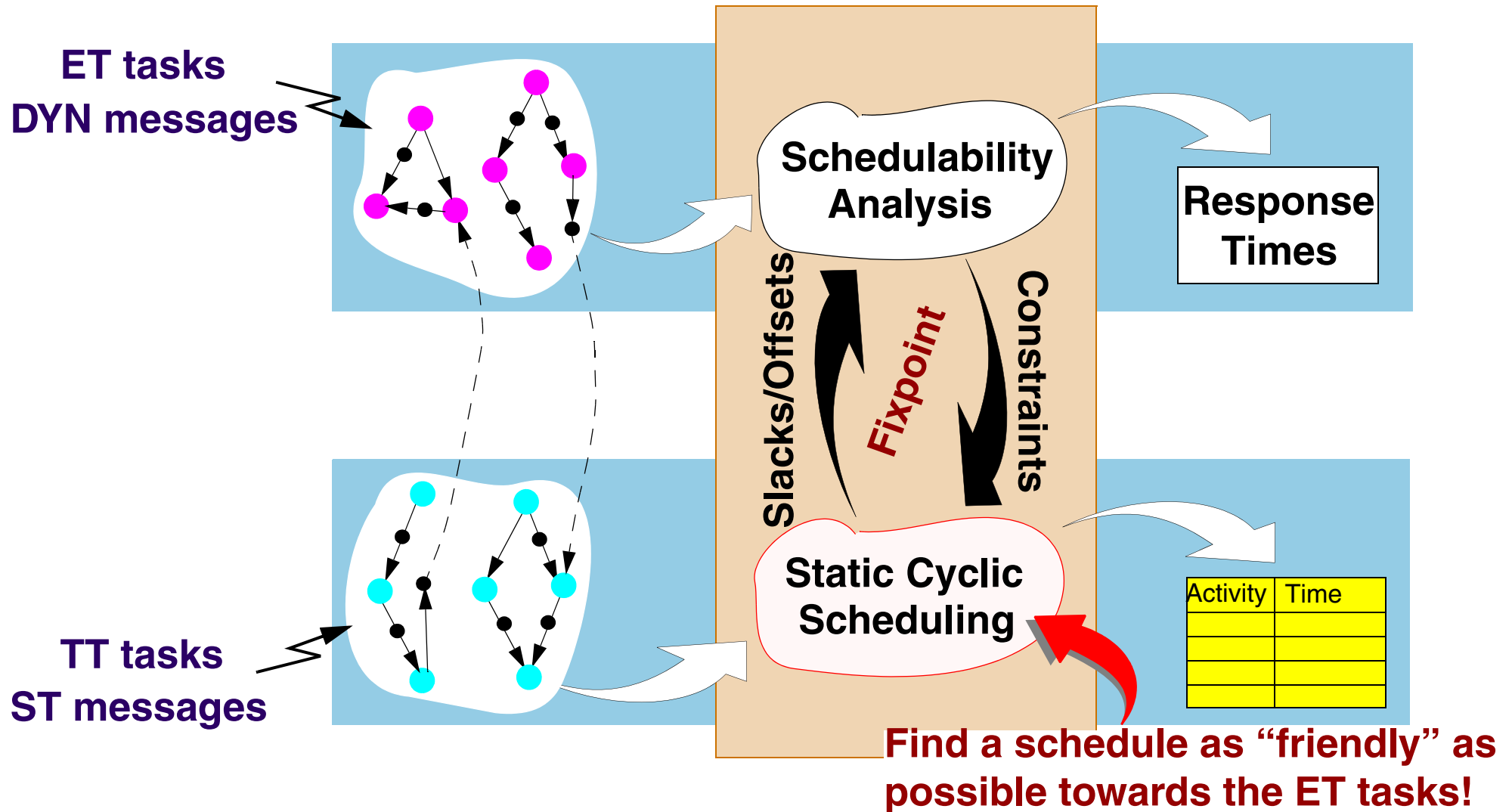
Static Cyclic  
Scheduling

Activity	Time



## ☞ Resource sharing and communication



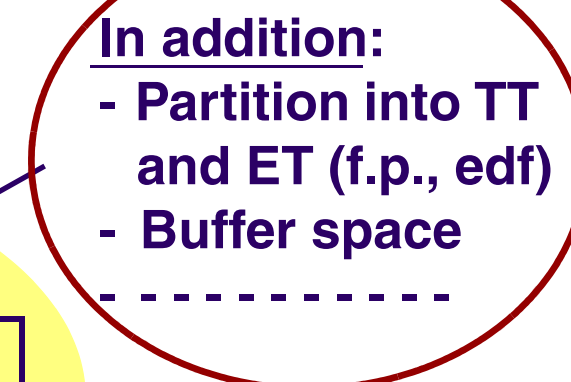


☞ Once the analysis approach is in place, several new, specific optimization tasks can be performed (in addition to “classical” ones, like task mapping):

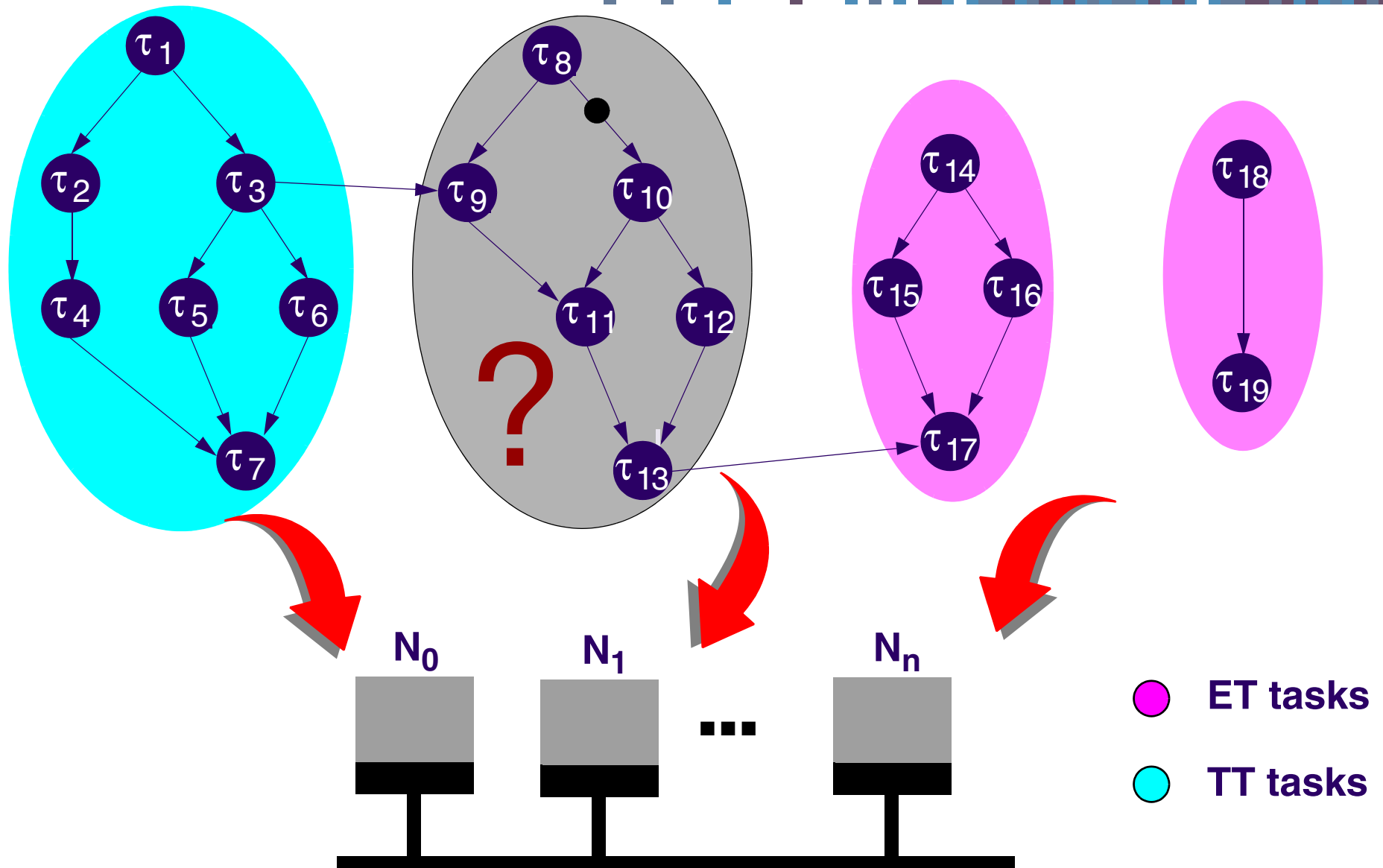
- Task partitioning into TT, ET
- Cluster mapping
- Bus access optimization (static, dynamic phases)
- Buffer minimisation



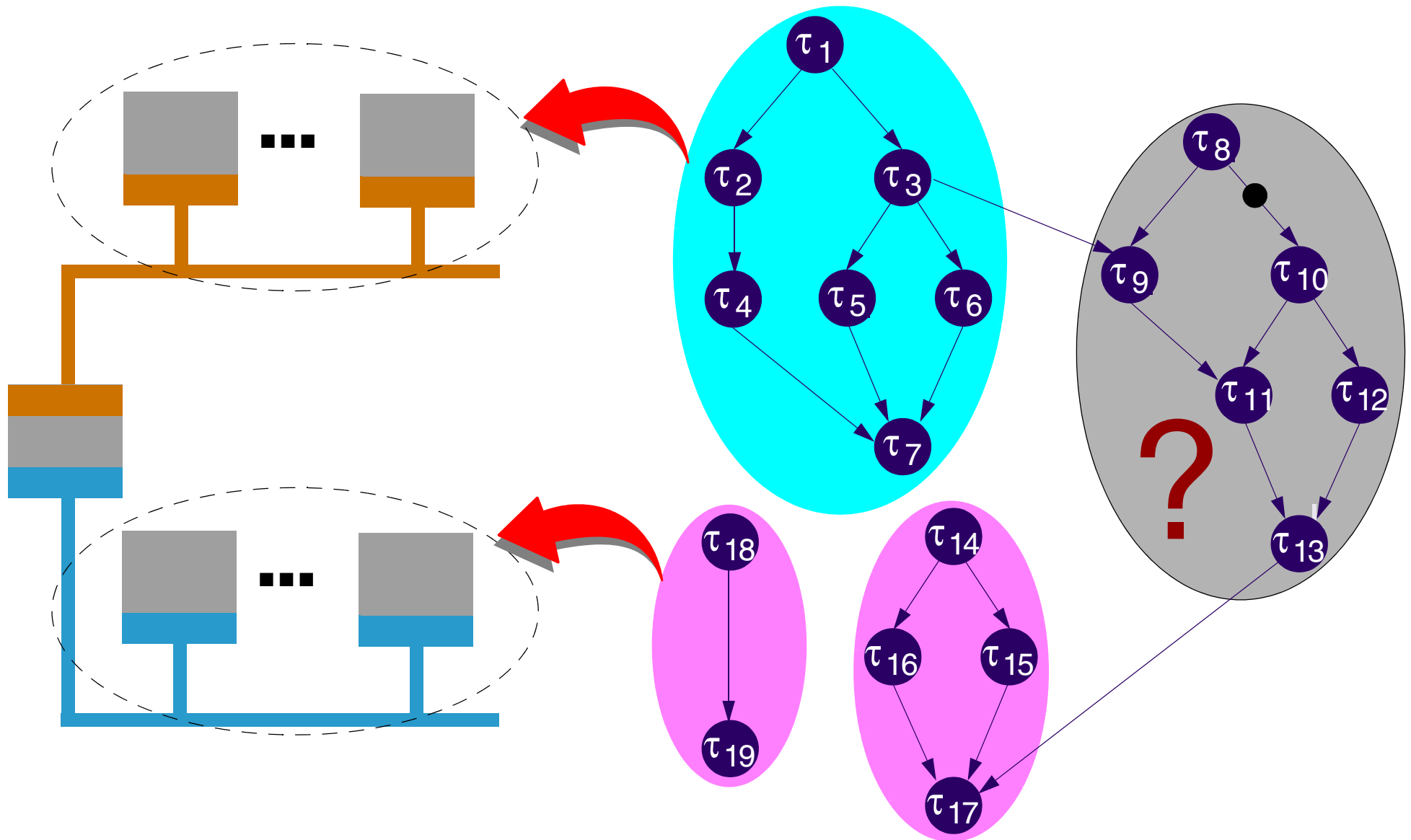




# Mapping & Task Partitioning



# Mapping & Task Partitioning



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# Another Issue: Fault Tolerance



## Transient faults

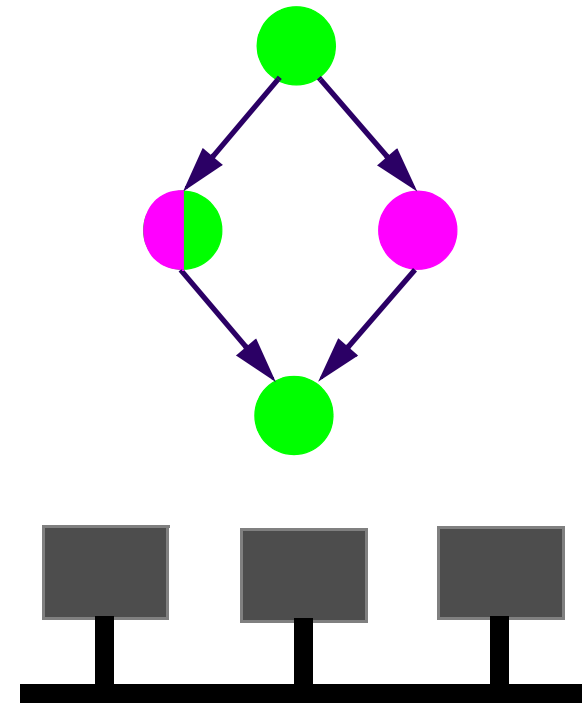
- Their number can be much larger than that of permanent faults.

- Find cost-effective implementations that are fault tolerant and satisfy time constraints.

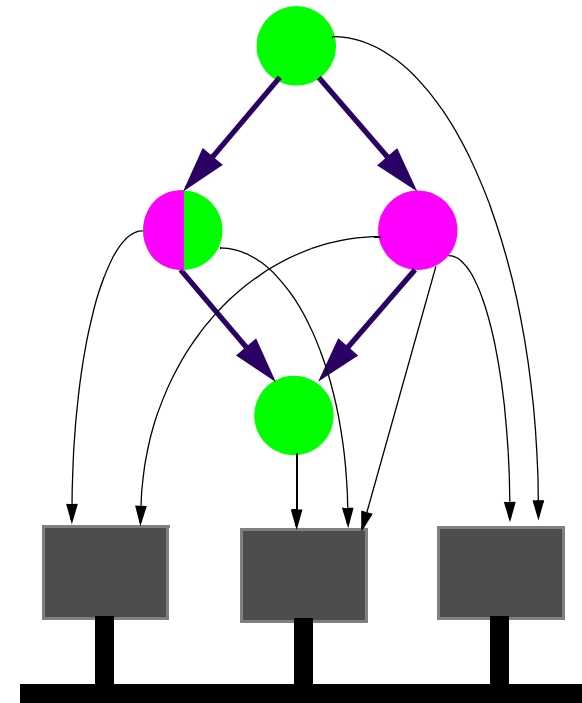
**Some Interesting trade-offs!**



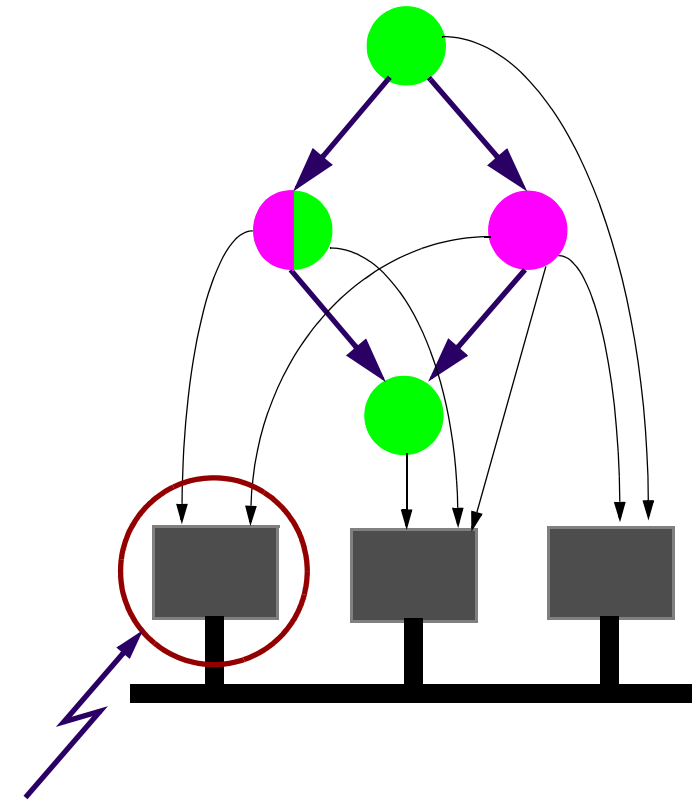
- Decide which fault tolerance technique to apply:
    - re-execution
    - re-exution&checkpointing
    - replication
- } different techniques can be applied to different tasks



- Decide which fault tolerance technique to apply:
  - re-execution
  - re-exution&checkpointing
  - replication
- Map the tasks (including eventual replicas)



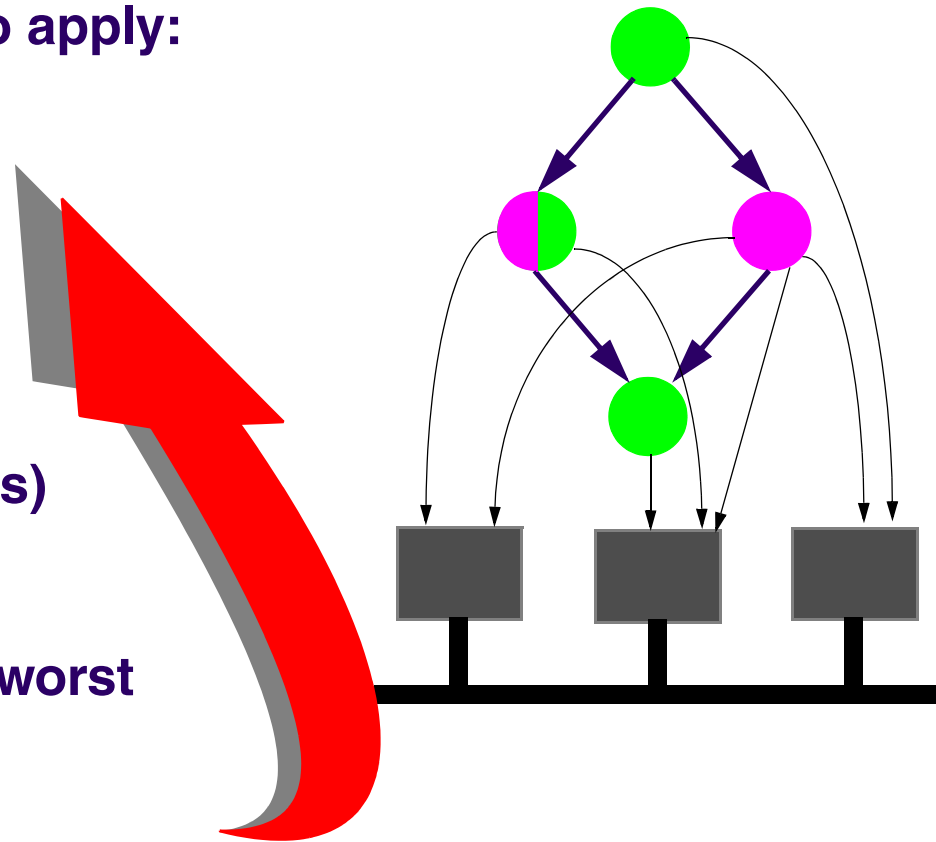
- Decide which fault tolerance technique to apply:
  - re-execution
  - re-exution&checkpointing
  - replication
- Map the tasks (including eventual replicas)
- Decide on transparency



Transparent: The schedule of outgoing messages does not depend on occurrence of faults (faults are not visible to the outside).

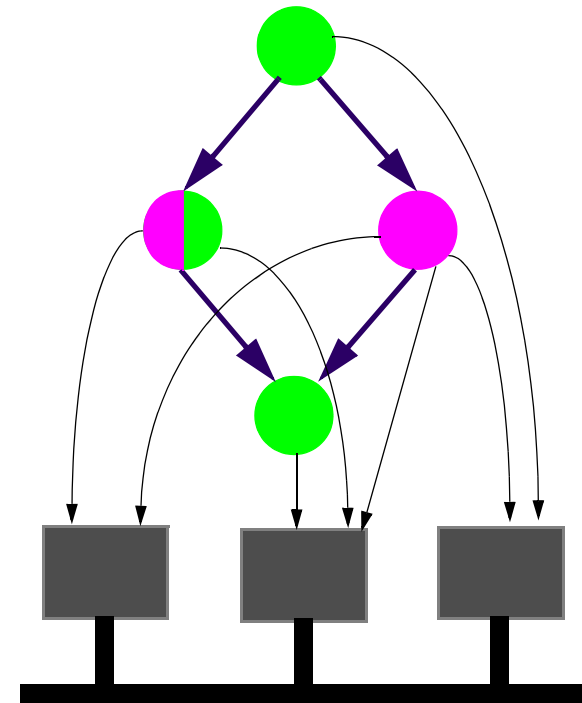


- Decide which fault tolerance technique to apply:
  - re-execution
  - re-exution&checkpointing
  - replication
- Map the tasks (including eventual replicas)
- Decide on transparency
- Do the analysis/scheduling, considering worst case number of faults (re-executions).  
Are time constraints satisfied? If not, go back!



- Decide which fault tolerance technique to apply:
  - re-execution
  - re-exution&checkpointing
  - replication
- Map the tasks (including eventual replicas)
- Decide on transparency
- Do the analysis/scheduling, considering worst case number of faults (re-executions).  
Are time constraints satisfied? If not, go back!

☞ Which is the optimal number of check-points?



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  - **Distributed Soft Real-Time Systems**
    - **Analysis Approaches and Optimization**
    - **Optimization**



# Distributed Soft Real-Time Systems



## ■ Given:

- ~~WCET and BCET~~ of each task
- Dimension of messages
- Deadlines for tasks/task graphs

👉 ~~All~~ deadlines have to be satisfied!



# Distributed Soft Real-Time Systems



## ■ Given:

- Execution Time Probability Distribution Function (ETPDF) of each task
- Dimension of messages
- Deadlines for tasks/task graphs

☞ A certain percentage of deadlines have to be satisfied!



# Distributed Soft Real-Time Systems



## ■ Given:

- Execution Time Probability Distribution Function (ETPDF) of each task
- Dimension of messages
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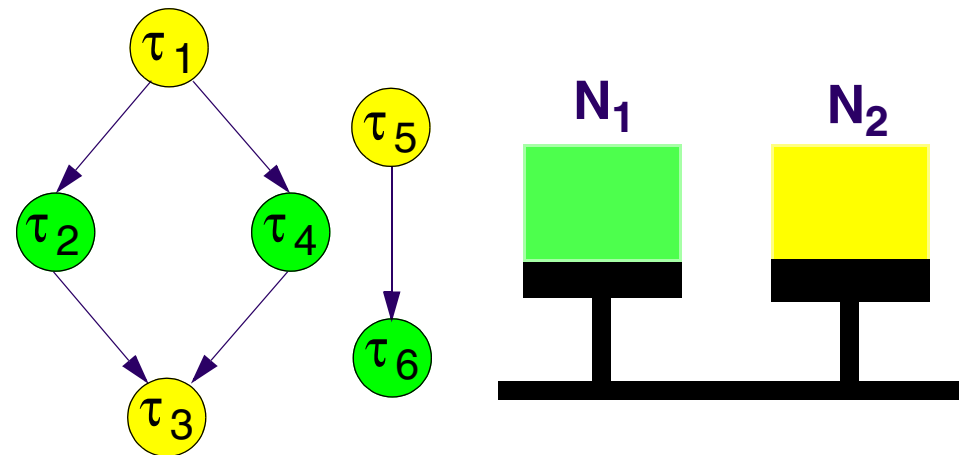
## ■ Problems:

- Determine the percentage of missed deadlines for each task/task graph.
- Optimize task mapping and priority assignment, such that a required percentage of satisfied deadlines is achieved.



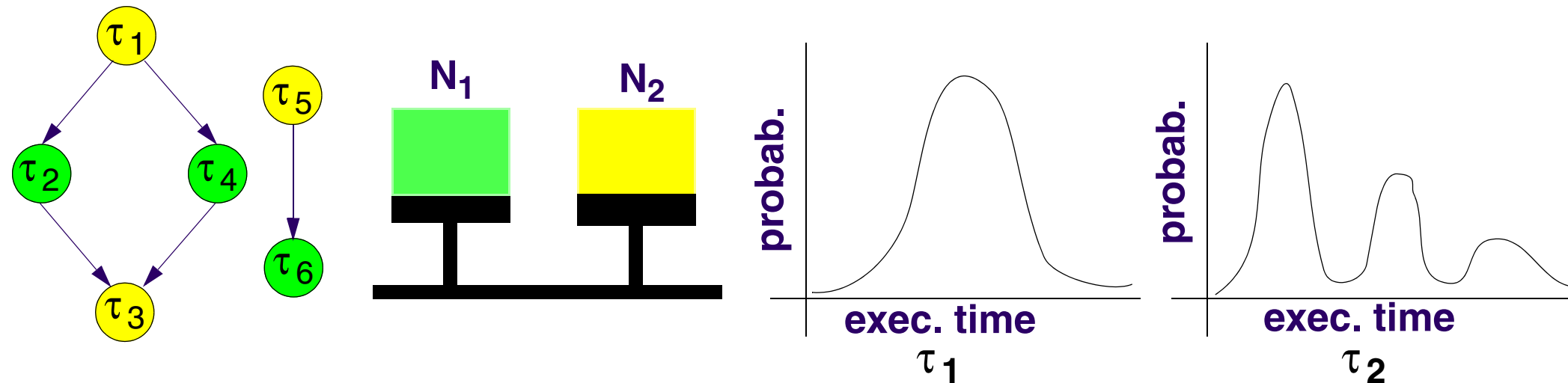
## Input:

- Set of mapped task graphs, periods, deadlines, priorities.



## Input:

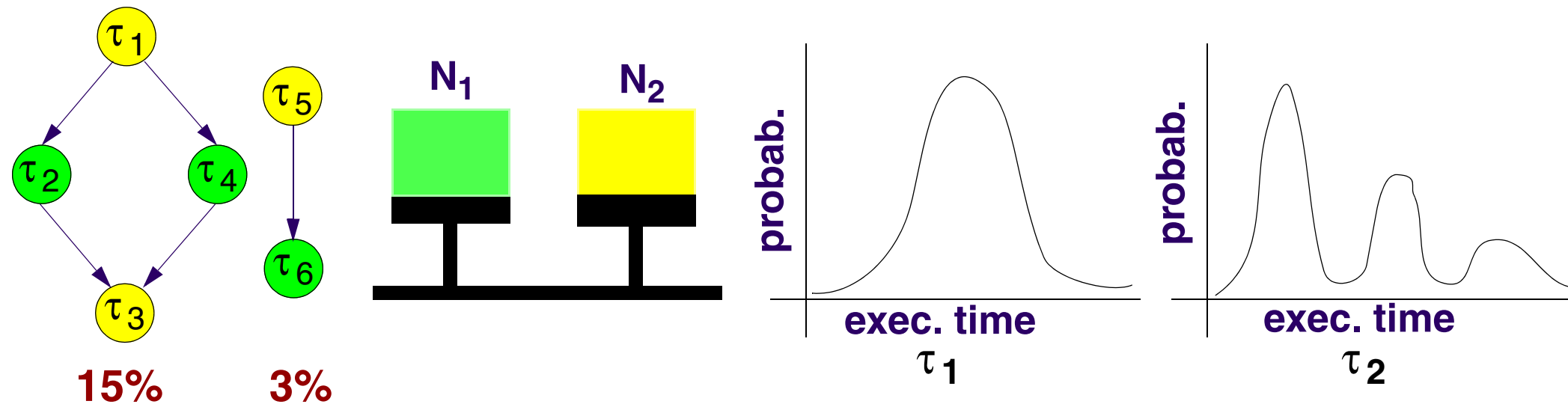
- Set of mapped task graphs, periods, deadlines, priorities.
- Set of execution times probability density functions.
- Scheduling policy.





## Output:

- Ratio of missed deadlines per task/task graph



- The main problem is **Complexity** (in terms of analysis time and memory).
  - Applying straight-forward solutions is possible
    - only for very(!) small applications.
    - and/or
    - for very particular cases (e.g. exponential distributions).



- An exact method for schedulability analysis, efficiently applicable (but not limited) to monoprocessor systems.
- An method for schedulability analysis, trading analysis efficiency for result accuracy; efficiently applicable to multiprocessors.
- A very fast, approximate analysis, to be used inside an optimization loop.



# Stochastic Process Construction



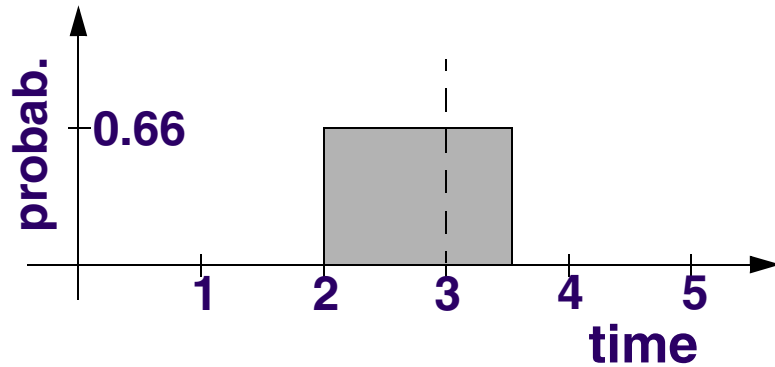
- **Analyse of the underlying stochastic process.**
  - **A state of the process should capture enough information to be able to generate the next states and to compute the corresponding transition probabilities**



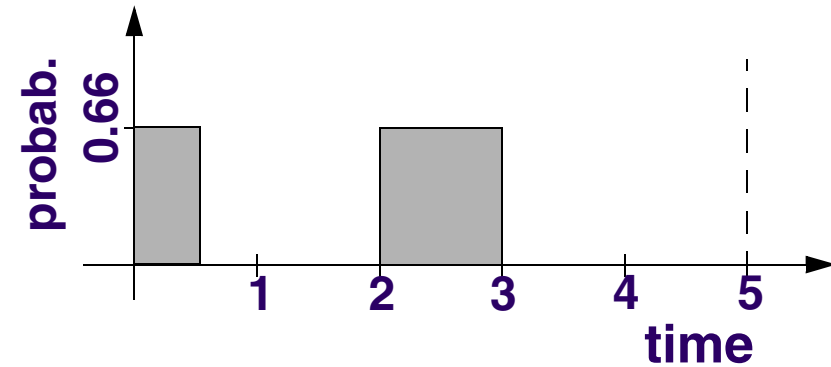
# Stochastic Process Construction



Task A: period=3



Task B: period=5

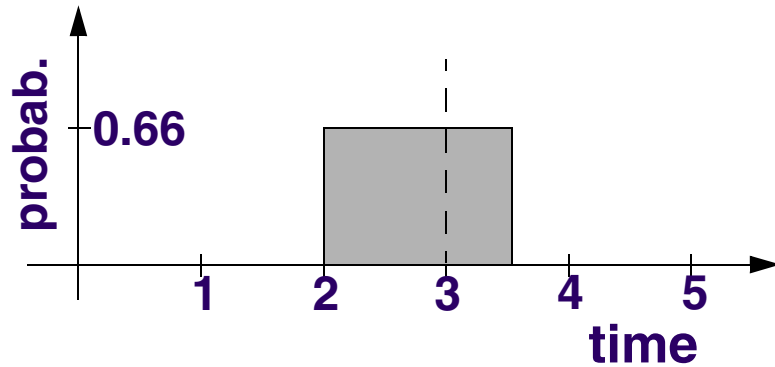


👉 EDF scheduling

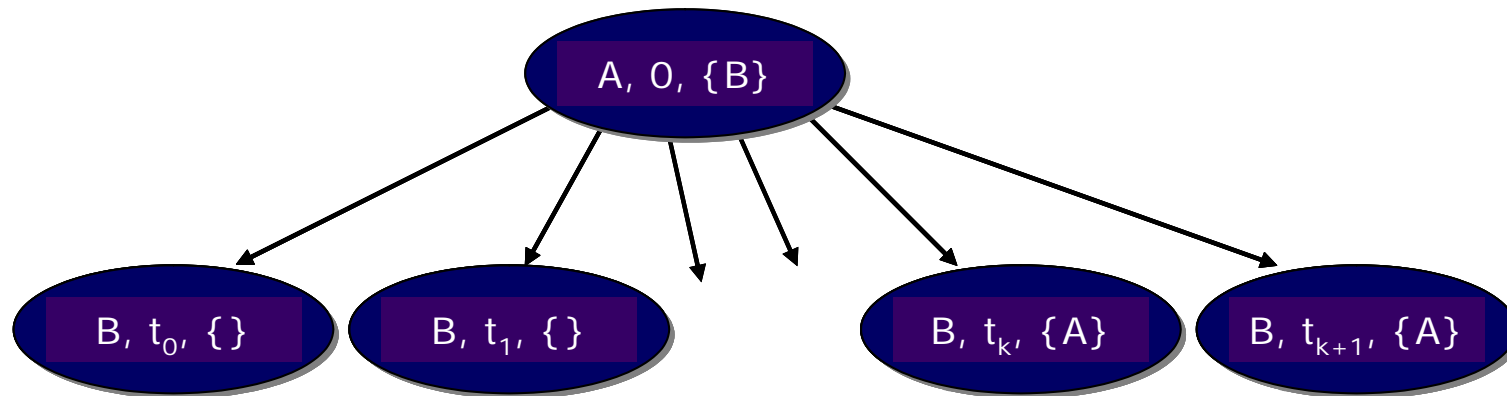
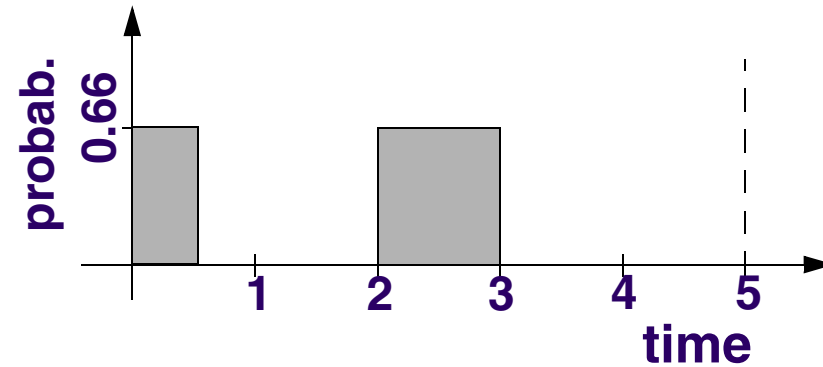


# Stochastic Process Construction

Task A: period=3

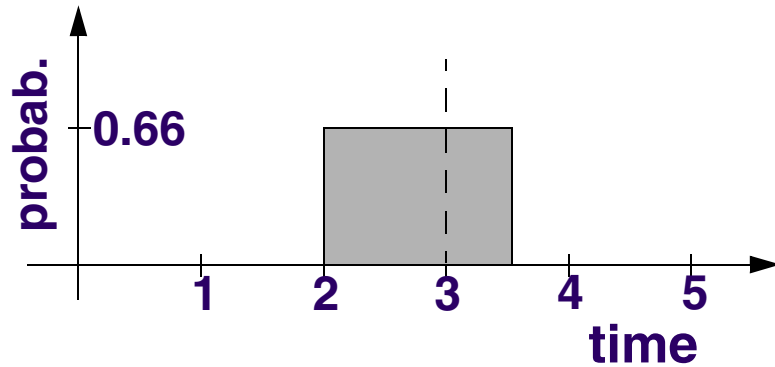


Task B: period=5

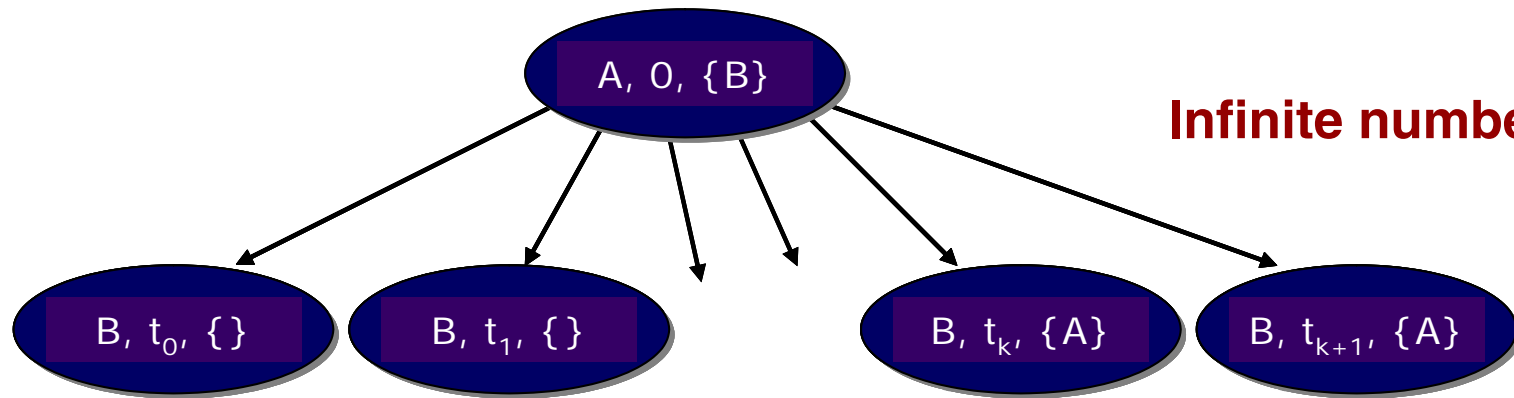
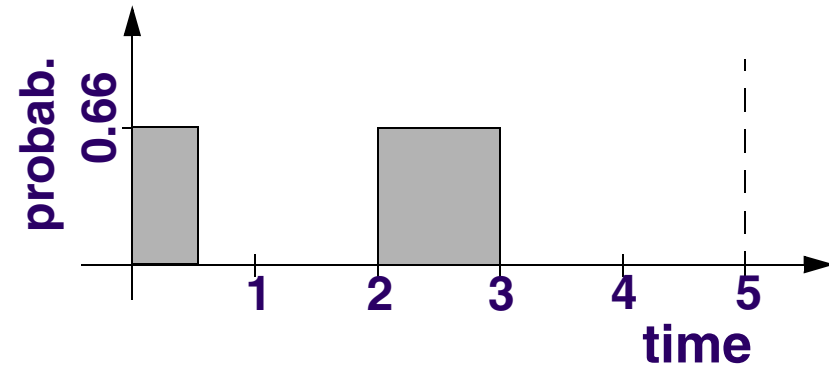


# Stochastic Process Construction

Task A: period=3



Task B: period=5

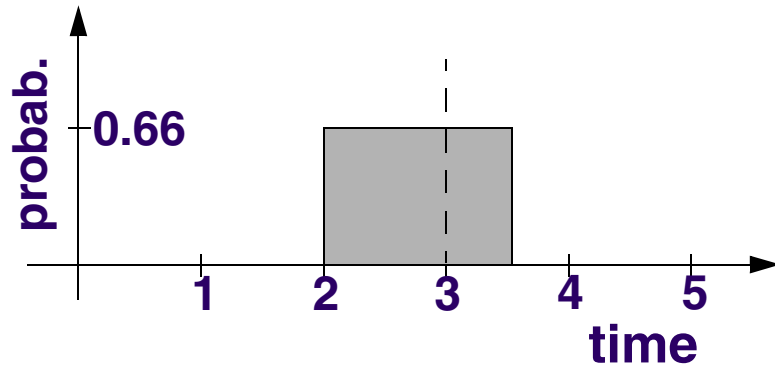


**Infinite number of states!**

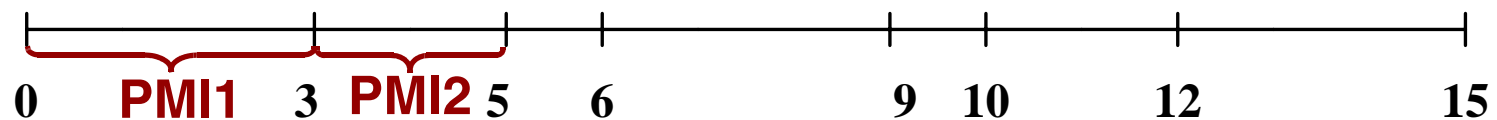
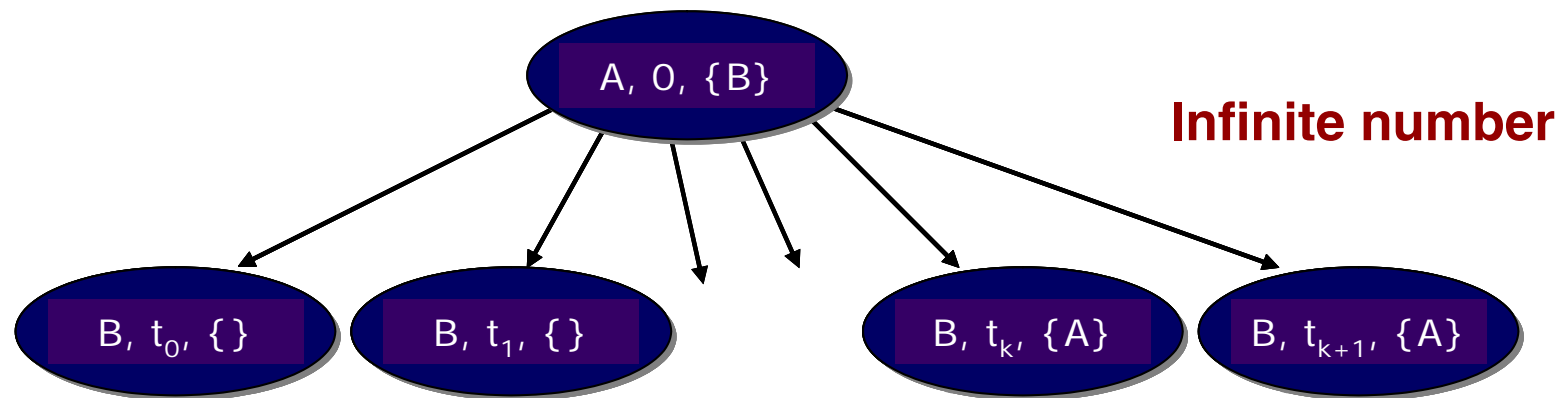
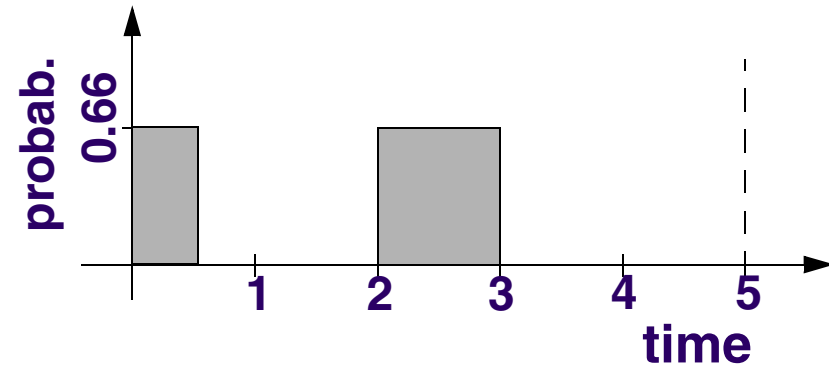


# Stochastic Process Construction

Task A: period=3



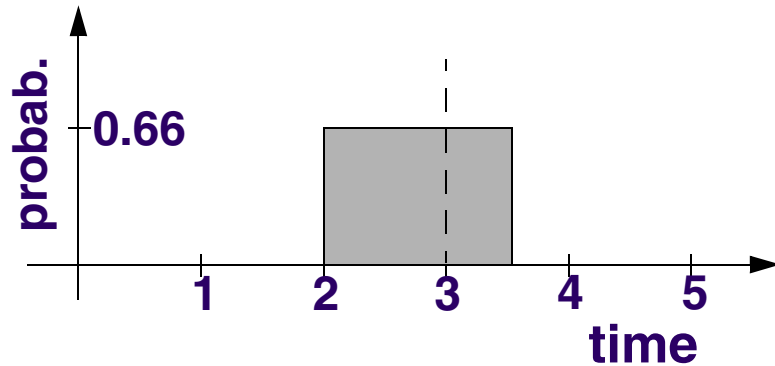
Task B: period=5



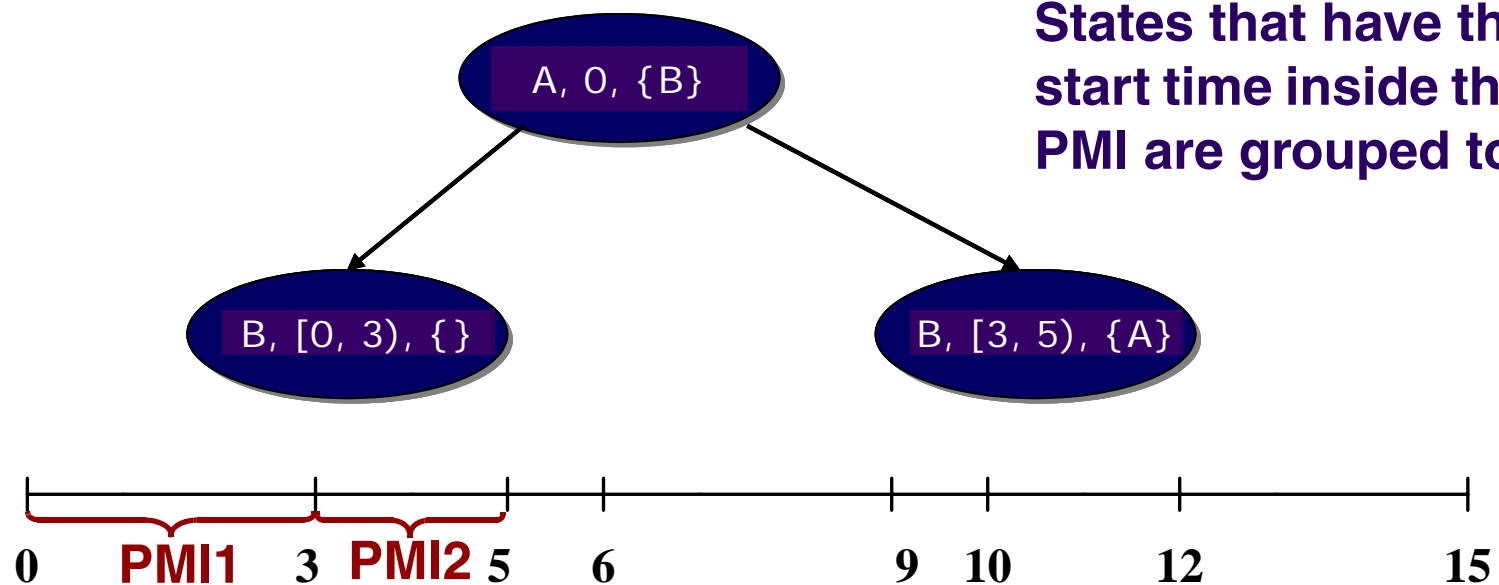
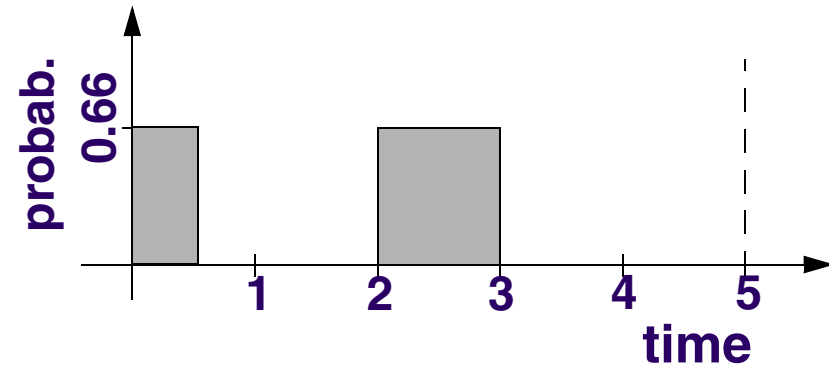


# Stochastic Process Construction

Task A: period=3



Task B: period=5

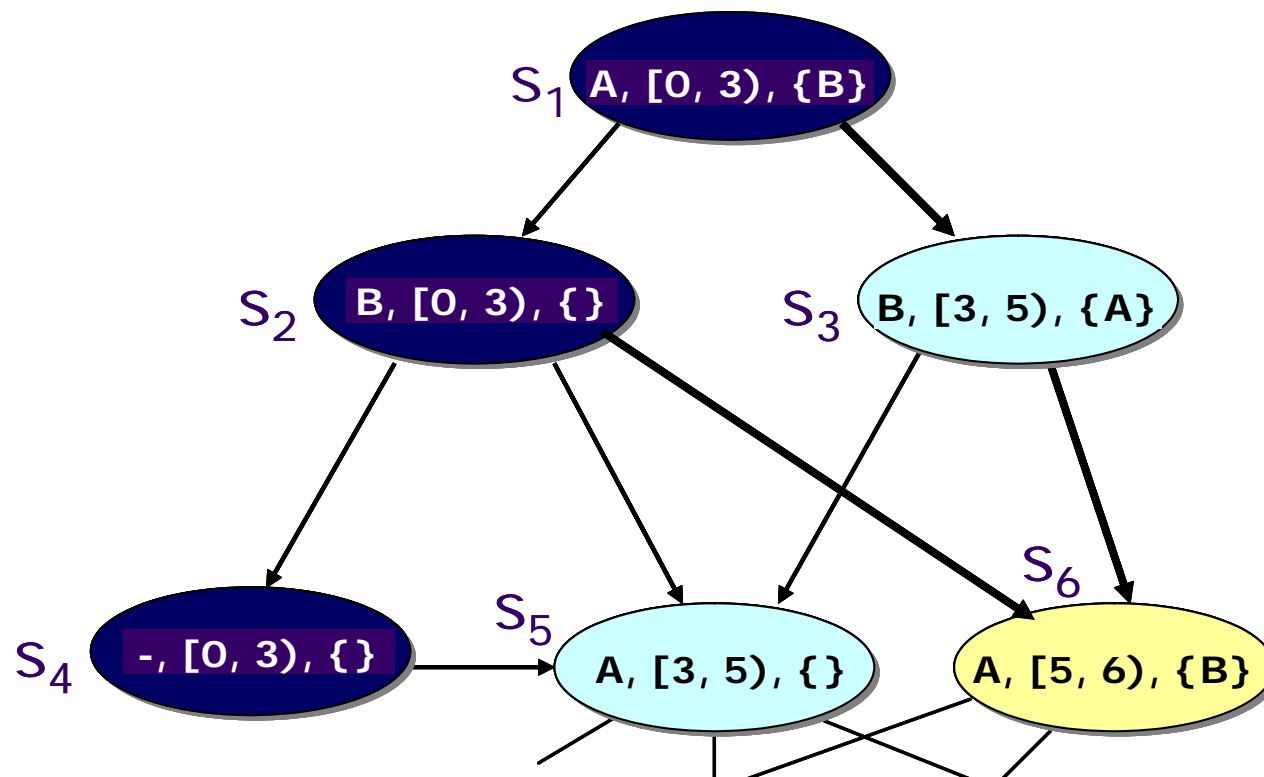


States that have their start time inside the same PMI are grouped together.



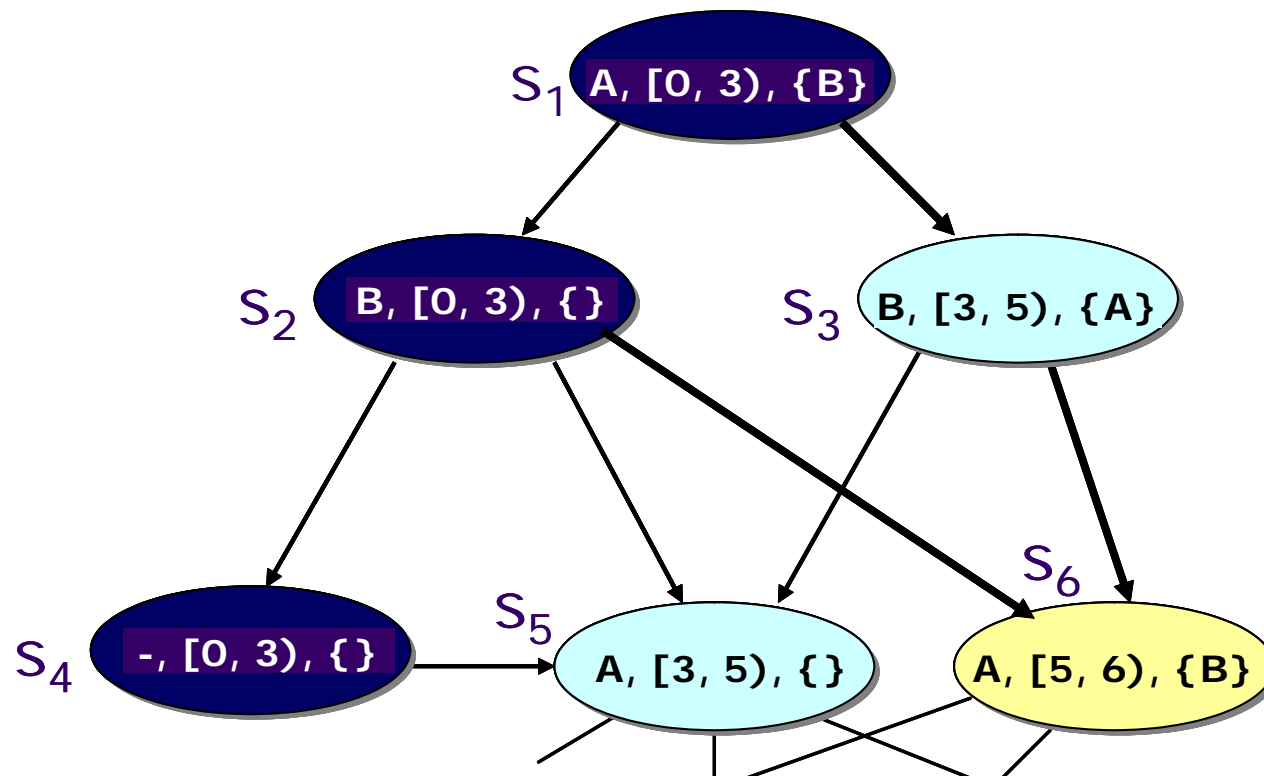
# Stochastic Process Construction

- ✎ The Stochastic process is constructed and probabilities corresponding to individual states are calculated by convolution.



# Stochastic Process Construction

- ➡ The Stochastic process is constructed and probabilities corresponding to individual states are calculated by convolution.
- ➡ **Good News:** Process construction and analysis are performed simultaneously. Only a (very small) sliding window of the states has to be stored in memory at any time.



- The number of states increases very much in the case of *interacting tasks implemented on multiprocessor systems*.
- We need to avoid
  - storing explicitly the distribution of residual exec. time in each state;
  - calculation of the convolutions.



# Multiprocessor Approach



The generalised ETPDFs are approximated by weighted sums of exponential functions (Coxian approximation).



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The initial generalised semi-Markov process is transformed into a continuous time Markov chain.

Larger, but much easier to analyse



# Multiprocessor Approach



The generalised ETPDFs are approximated by weighted sums of exponential functions (Coxian approximation)

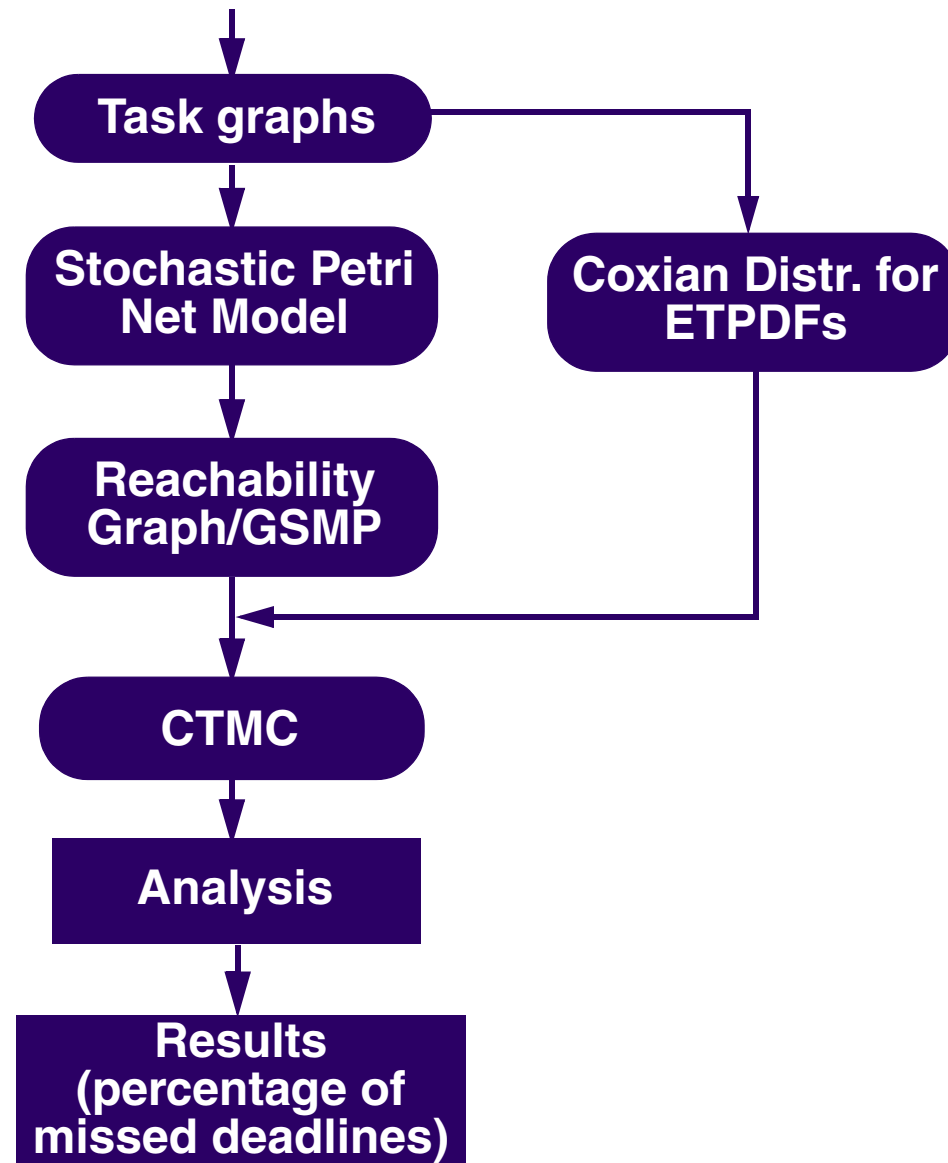


The initial generalised semi-Markov process is transformed into a continuous time Markov chain.

- ☞ **Good News:** The whole matrix, corresponding to the complete model, has *not* to be stored in memory; it is generated on the fly, from terms expressed as small matrices.
- ☞ Accuracy can be traded for analysis time/memory.



# Multiprocessor Approach





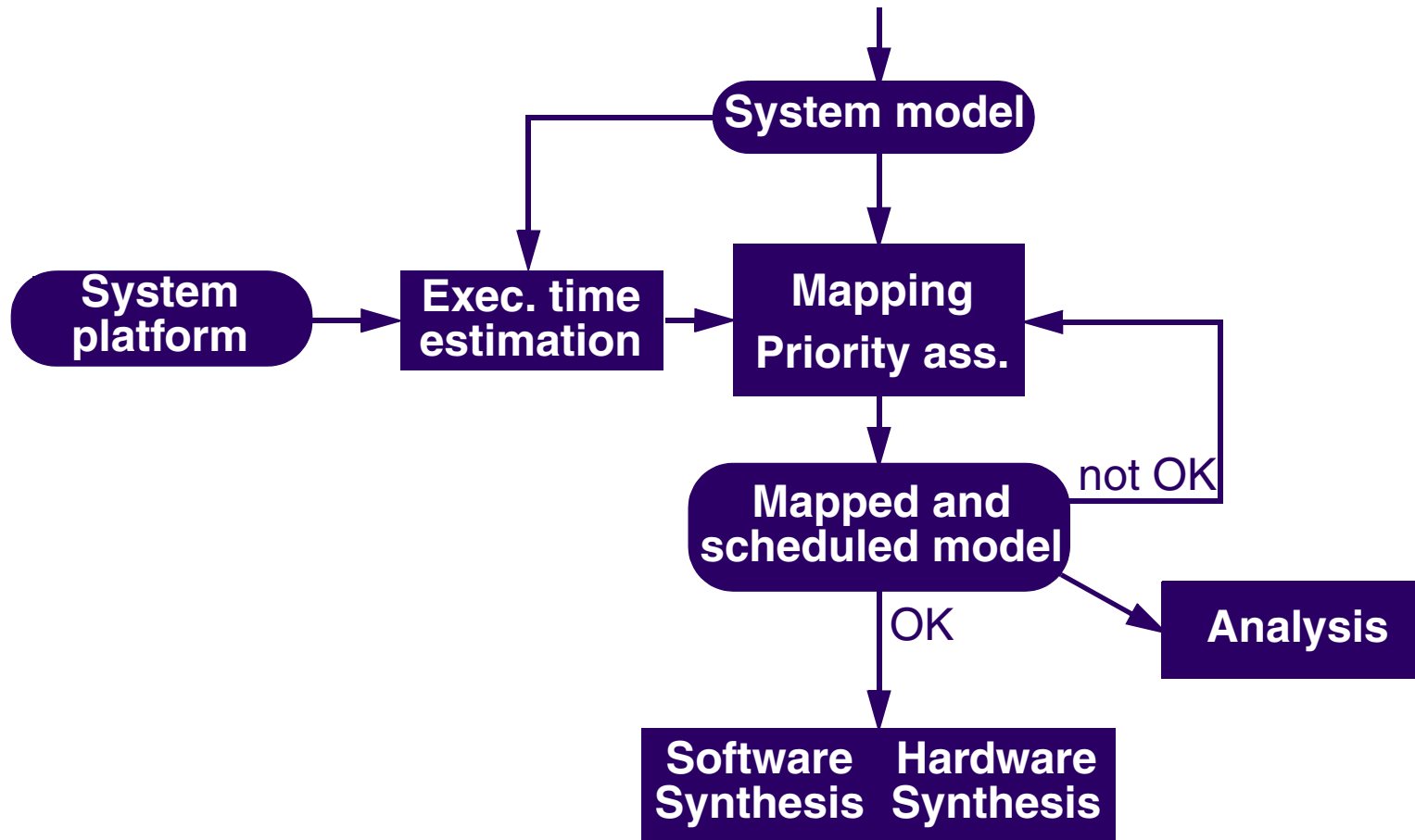
## ■ Problem:

- Optimize task mapping and priority assignment, such that a required percentage of satisfied deadlines is achieved.



## ■ Problem:

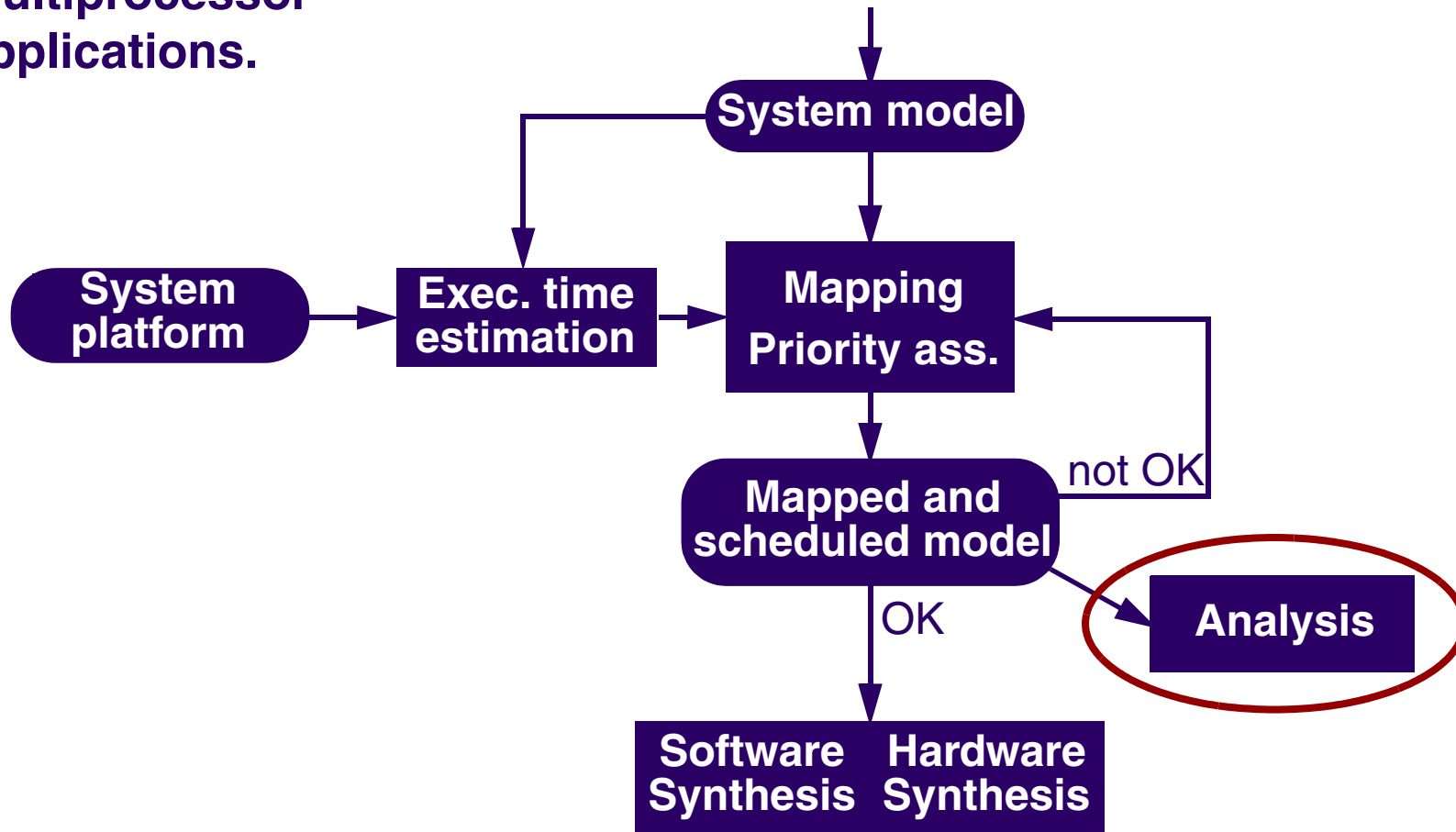
- Optimize task mapping and priority assignment, such that a required percentage of satisfied deadlines is achieved.



☞ The presented analysis approach works for large multiprocessor applications.

**But**

☞ It is too slow to be used inside an optimization loop.



☞ An approximate analysis method of polynomial complexity has been developed.

## ■ Basic idea:

- Weak dependencies among the random variables have been neglected.



**Very fast analysis, sufficiently accurate  
to guide the design space exploration.**



If you optimize your system to minimise average or worst case execution time



**If you optimize your system to minimise average or worst case execution time and you hope that the resulted design is close to optimal with regard to the percentage of missed deadlines**



If you optimize your system to minimise average or worst case execution time and you hope that the resulted design is close to optimal with regard to percentage of missed deadlines

then

**YOU ARE VERY WRONG!!!**



- Distributed embedded systems are becoming common.
- They are communication dominated and heterogeneous.
- They have to be safe (fault tolerance).
- Hard distributed real-time systems. }
- Soft distributed real-time systems. } How to guarantee timing constr.?
- Analysis (in particular timing) is difficult, but possible.  
Simulation is not the right solution!
- It is not sufficient to analyse! Help the designer to implement a cost effective system that satisfies the imposed constraints!  
Efficient optimization tools are needed.

