

# **Modelling, Analysis and Scheduling with Dataflow Models**

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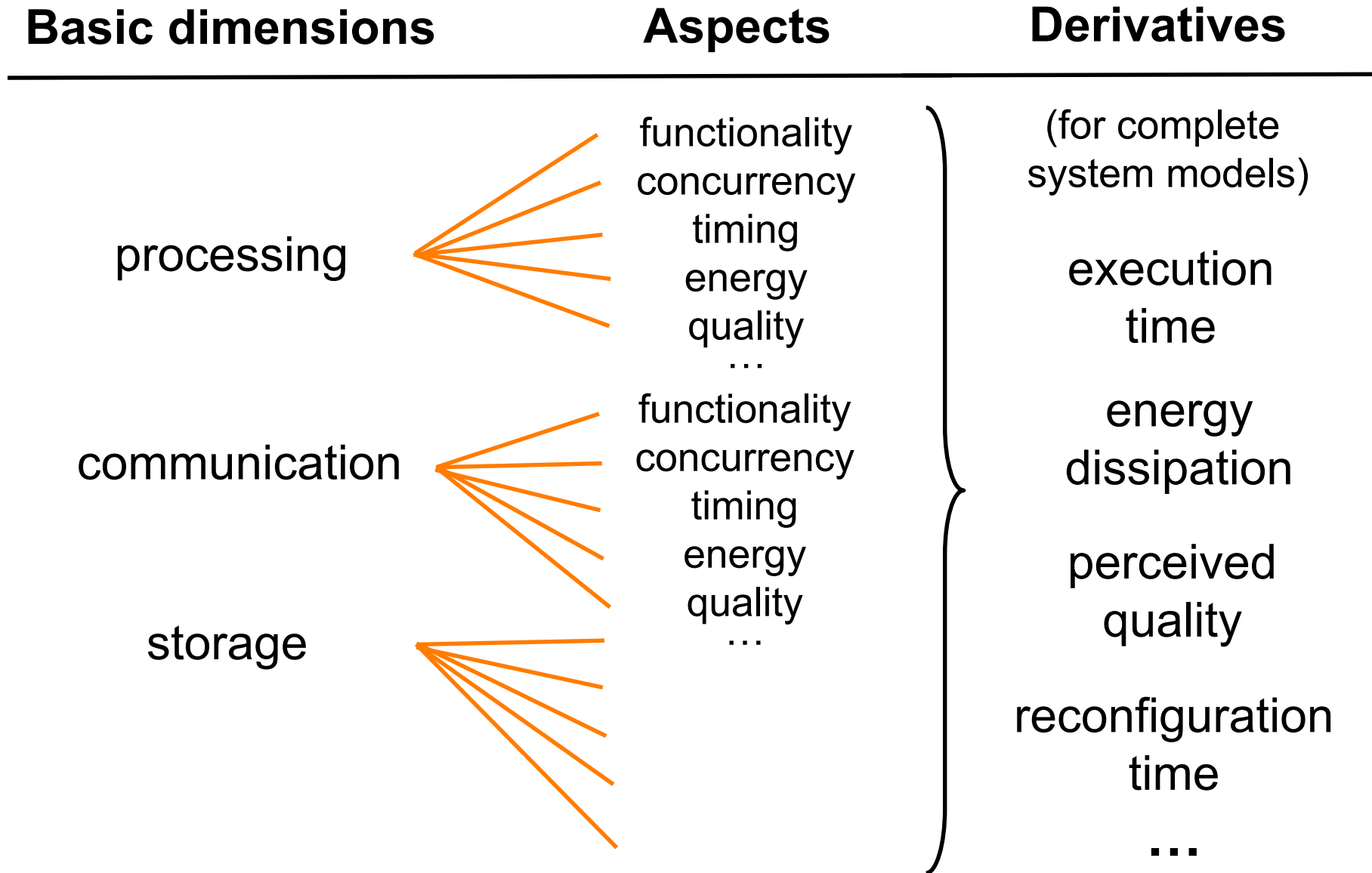
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## 2 Overview

- Dataflow model of computation
- Models of multiprocessor SoC and NoCs
  - Integrated model of application, architecture and mapping
- Synchronous Dataflow Graphs
  - Exact algorithms based on state-space exploration
- Kahn Process Networks
  - Implementation of KPNs, deadlock detection and resolution
- Reactive Process Networks
  - Integrating reactive behaviour with dataflow
- Scenarios and Trade-offs
  - Improving WCET estimation
  - Working with trade-offs

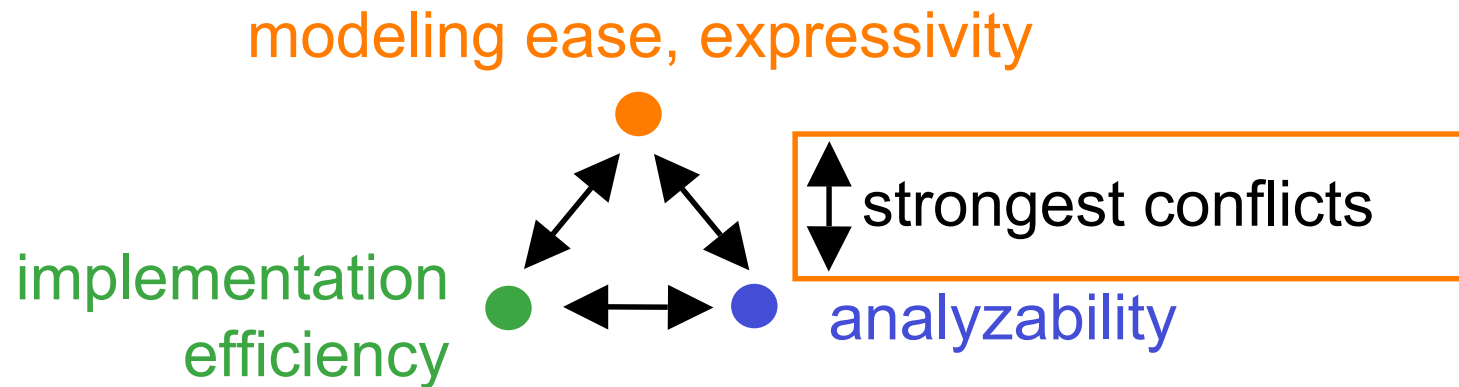
### 3 Models of Computation



## 4 Our Goals

- Models of computation (and communication)
- Aimed at automated analysis and synthesis
- Solid mathematical foundation
- Basic algorithms and properties
- Domain of embedded systems, often NoC based MPSoc
- Towards variability and sensor networks

## 5 Conflicting Requirements



Kahn Process Networks:

+ (streaming), - (only functional behavior), o (no static implementations)

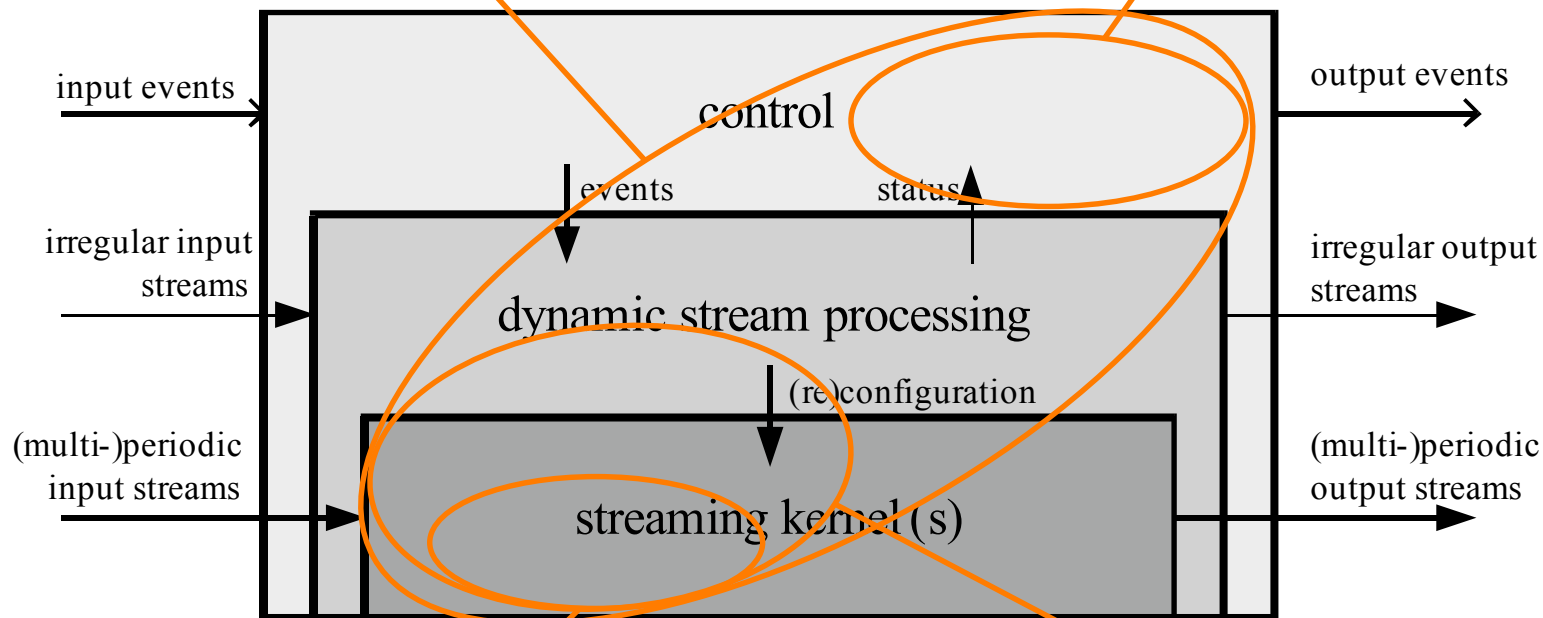
Synchronous Dataflow Graphs:

- (periodic kernels), + (timing, schedulability), + (static implementations)

# 6 Application Domain: Multimedia Applications

Reactive Process Networks (RPN)

Automata / State machines



Synchronous Data Flow (SDF)

Kahn Process Networks (KPN)

# 7 Streaming MoCs and the Design Flow

Reactive Process Networks (RPN)  
(Semantic framework)

Kahn Process Networks (KPN)  
(Executable specifications)

(Synchronous) Data Flow  
(Implementation and analysis)

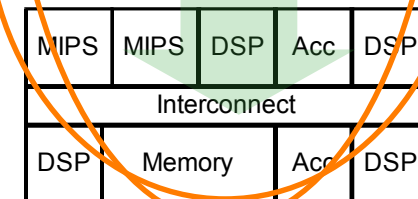
typically C code

```

// Implementation of the filter process procchannels
void procchannels(
    realType u, // formal input
    procChannelsContextType* context, // context
    realType y // formal output
)
/* implied statements */
context->u = u;
/* user-defined statements */
/* MI_Controller_1 */
MI_Controller_1(context->u, &context->MI_Controller_1,
&context->MI_Controller_1control);
/* MI_Controller_2 */
MI_Controller_2(context->u, &context->MI_Controller_2,
&context->MI_Controller_2control);
/* sum_1 */
context->sum_lo = context->MI_Controller_1control +
context->MI_Controller_2control;
/* copy */
context->y = context->sum_lo;
/* implied statements */
y = context->y;
    
```

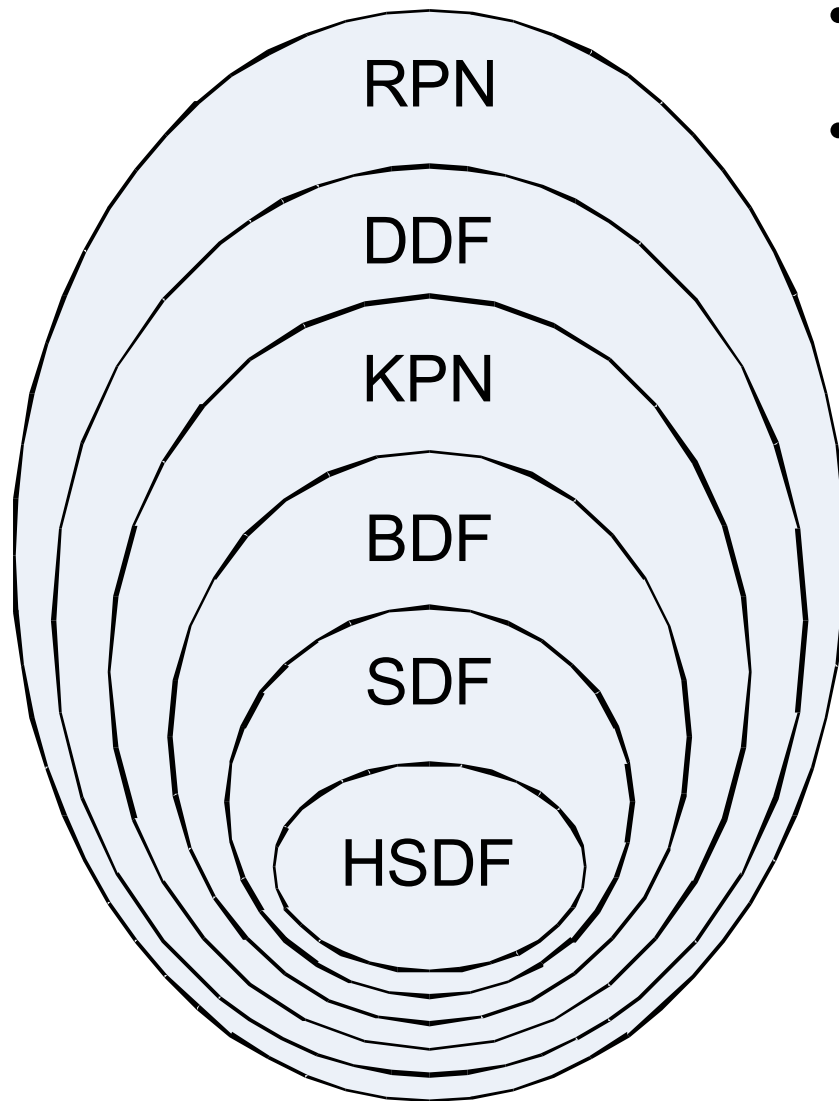
parallel code

implementation code



HW/SW

## Streaming MoCs Expressiveness Hierarchy



- BDF and larger: Turing complete
- Better notions of expressiveness needed

RPN: Reactive Process Networks

KPN: Kahn Process Networks

DF: Data Flow

DDF: Dynamic DF

BDF: Boolean DF

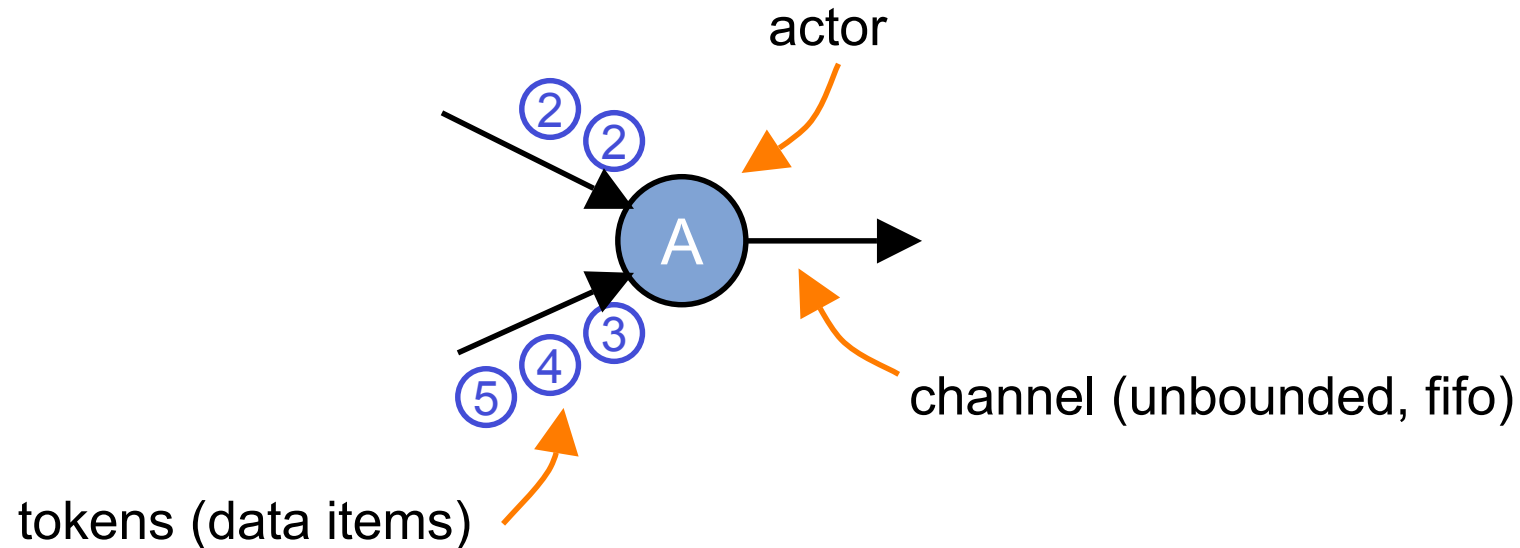
SDF: Synchronous DF

HSDF: Homogeneous SDF



## 9 Dataflow Actors

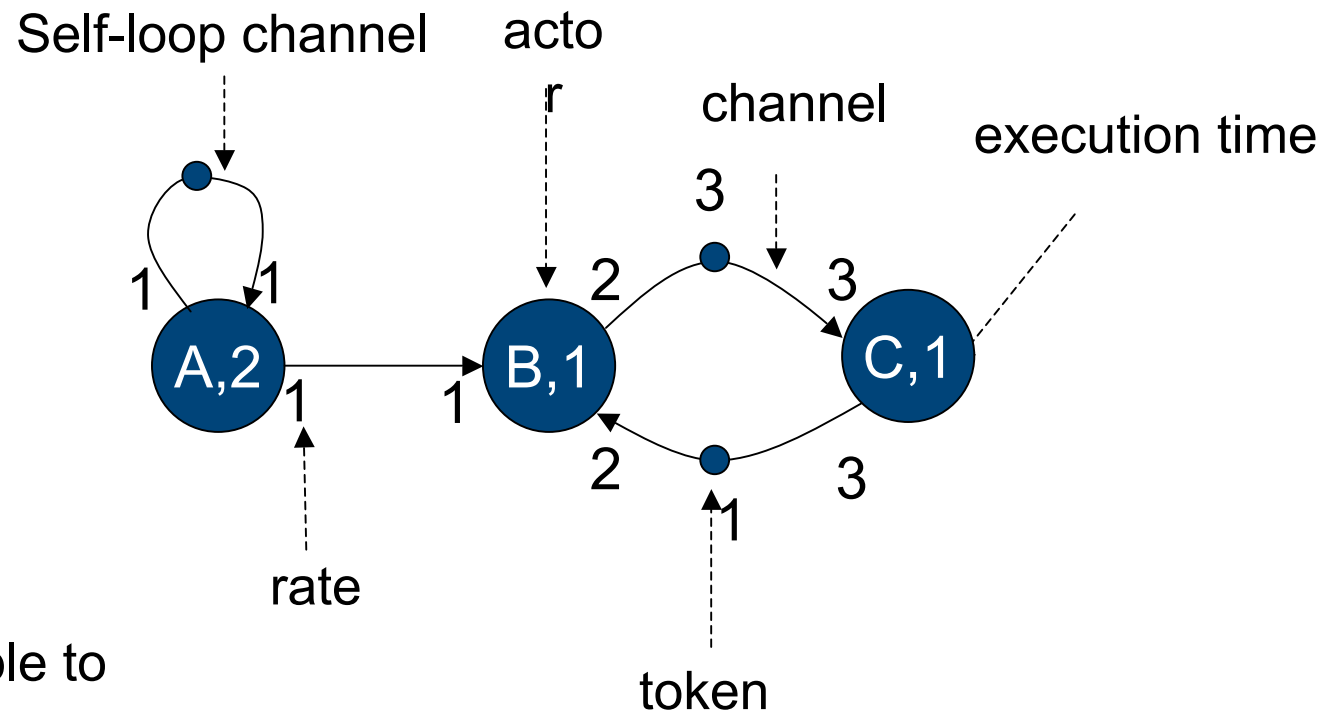
- Basic building blocks of any type of dataflow graph



- Actor firing: consumption and production of tokens

## 10 Synchronous Dataflow (SDF) Graphs

- Actor fires atomically, reading and writing fixed number of tokens on the inputs and outputs
- Formal semantics models conservatively the behaviour of real kernels



Comparable to

Computation Graphs (Karp, Miller)

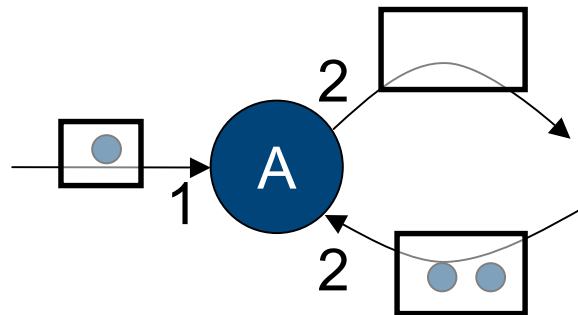
Weighted Marked (Timed) Graphs (Petri-Nets)

## 11 Synchronous Dataflow (SDF) Graphs

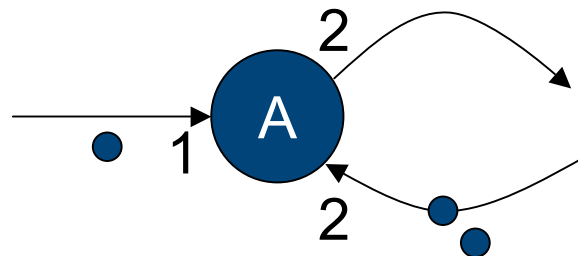
- Worst-case, conservative approximation of actual read and write instances and variable (bounded) execution time.
- Can model buffer storage limitations
- Can model scheduling decisions
- Models application mapping. E.g., communication latency or memory access latency
- Models multimedia applications
- Composibility, resource virtualization, TDMA

## 12 Conservative model

model execution

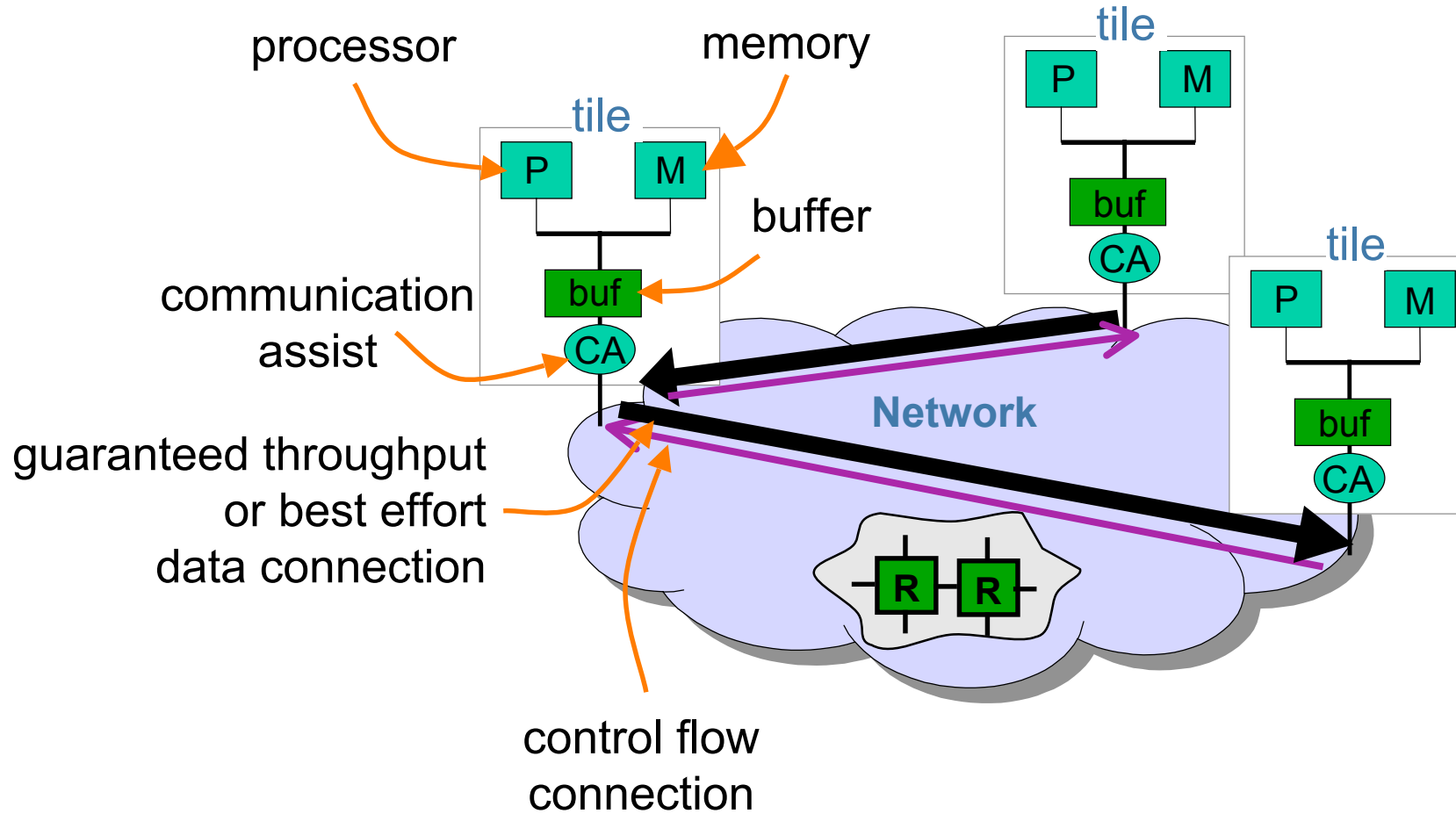


actual execution

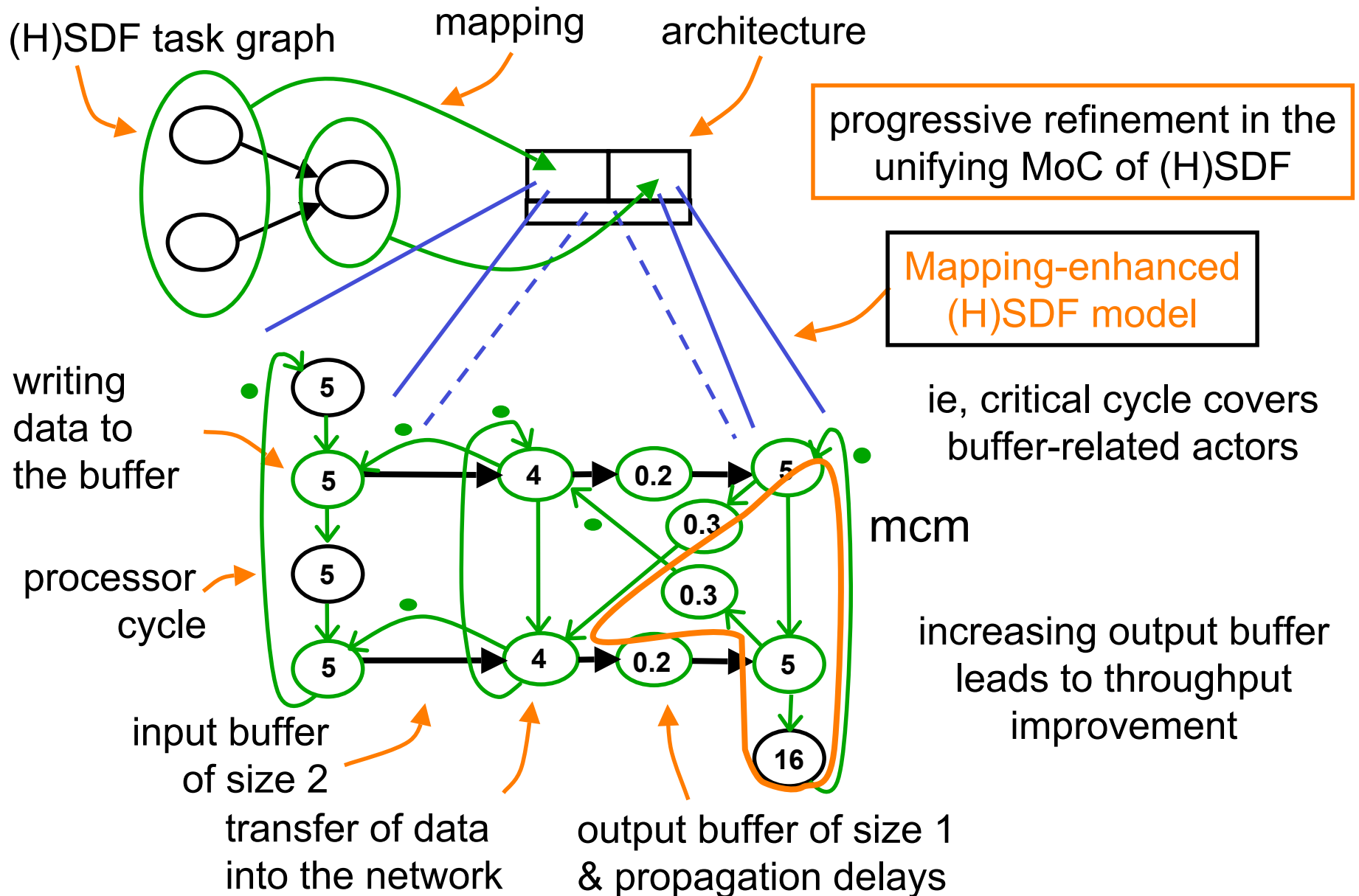


conservativity + monotonicity

# 13 A NoC-based SoC Platform

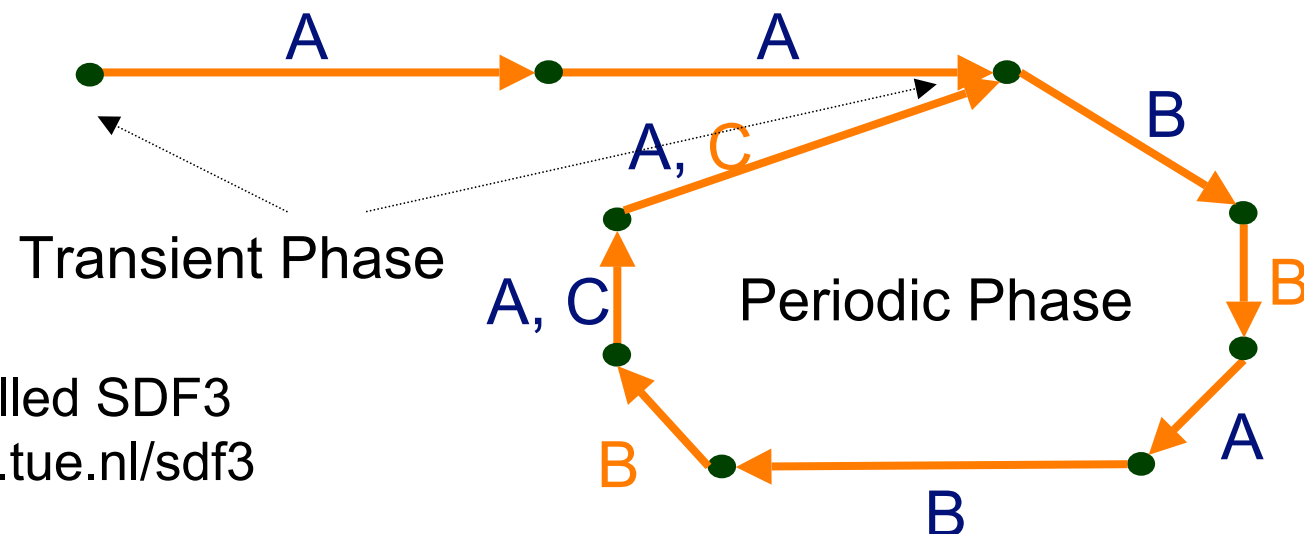


# 14 Philosophy



## 15 Analysis

- Many problems NP Complete, defined on HSDF only  
buffer sizes, throughput, (deadlock?)
- Conversion SDF to HSDF leads to potentially exponential blowup
- We have implemented exact methods based on state-space exploration  
Surprisingly efficient compared to Maximum Cycle Mean methods



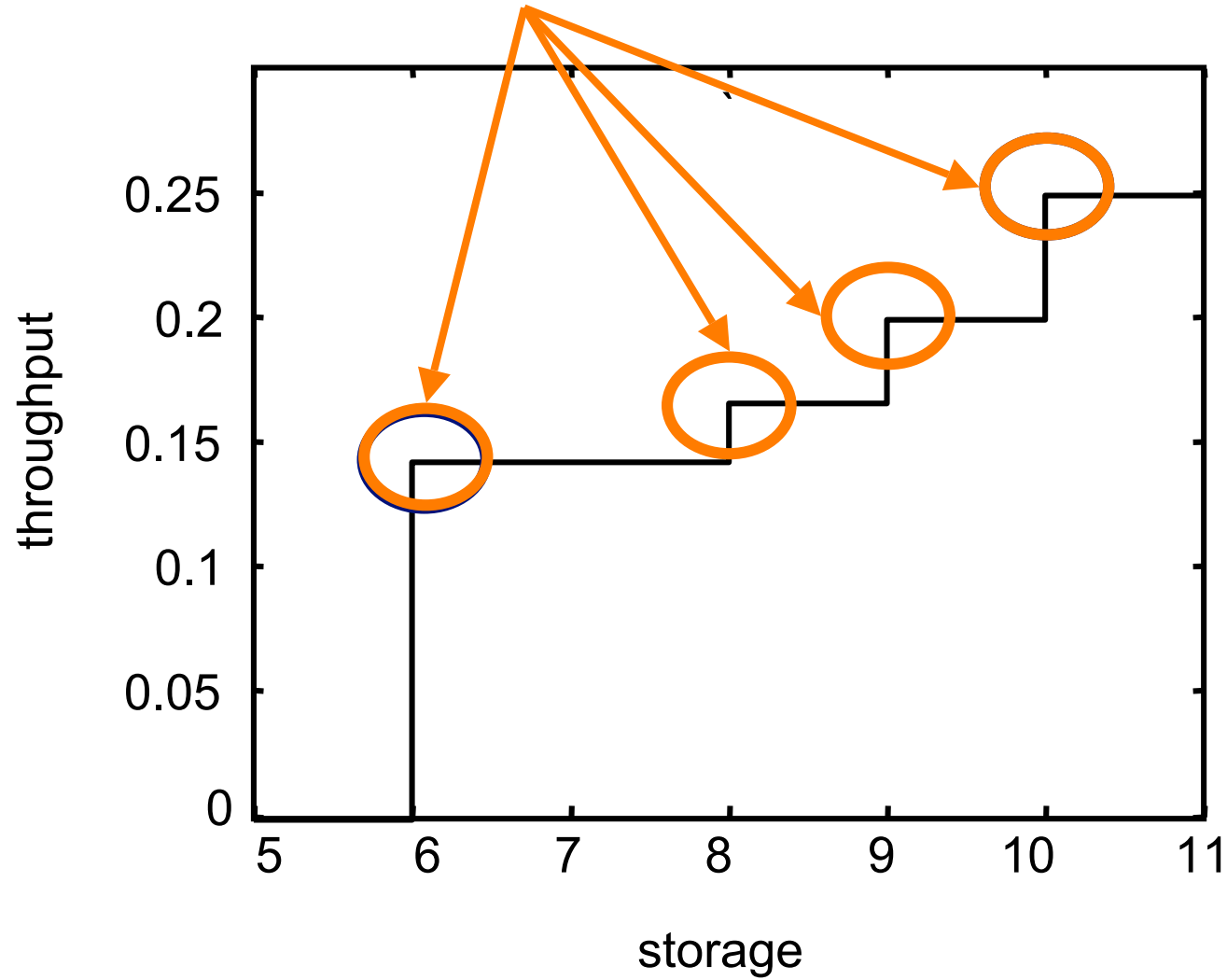
- Tool set, called SDF3  
[www.es.ele.tue.nl/sdf3](http://www.es.ele.tue.nl/sdf3)

## 16 Analysis

- Throughput computation
- Latency definition for SDF
- Liveness, boundedness, consistency  
Based on throughput analysis
- Minimum buffer sizes  
State-space exploration; critical cycle analysis
- Buffer size vs. Throughput (latency) trade-offs  
Generalization of minimum buffer size problem



### Pareto optimal trade-offs



## 18 Limitations of SDF Graphs

### Limitations

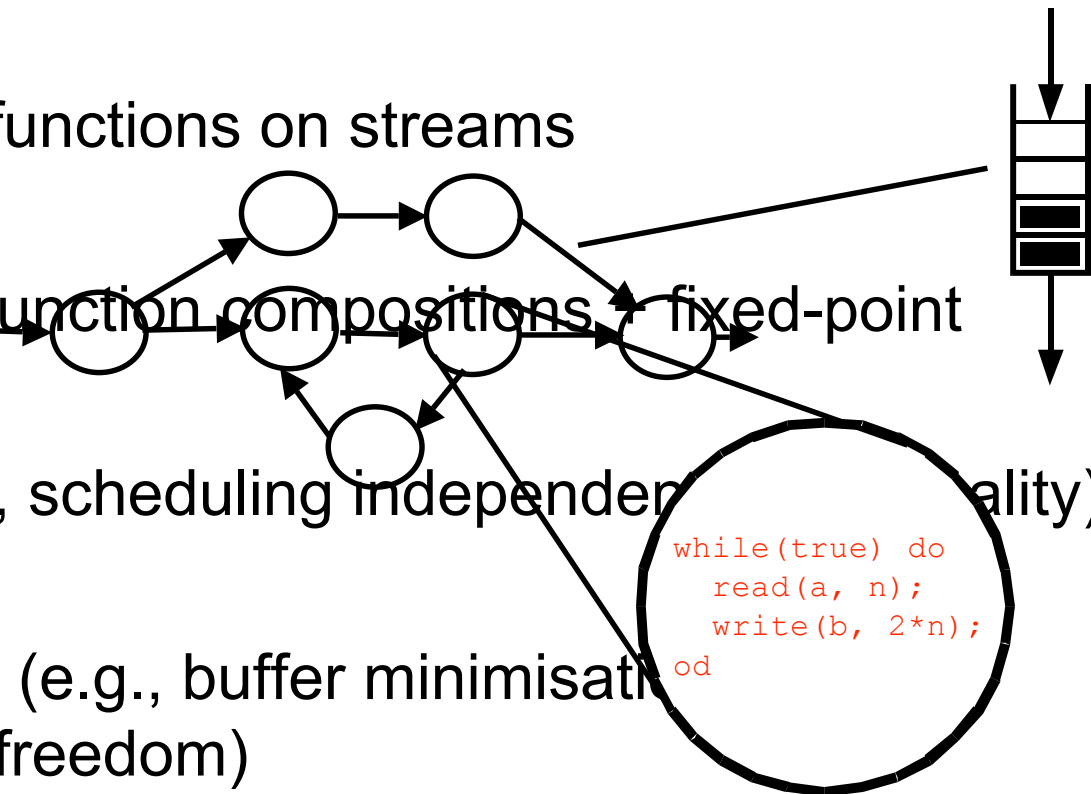
- Static, periodic behaviour
- Fixed execution times  
(potentially high over-estimation of worst-case)
- No Dynamic instantiation, reconfiguration

### Extensions

- Kahn Process Networks (KPN)
- Scenarios (Scenario Aware Dataflow)
- Reactive Process Networks (RPN)

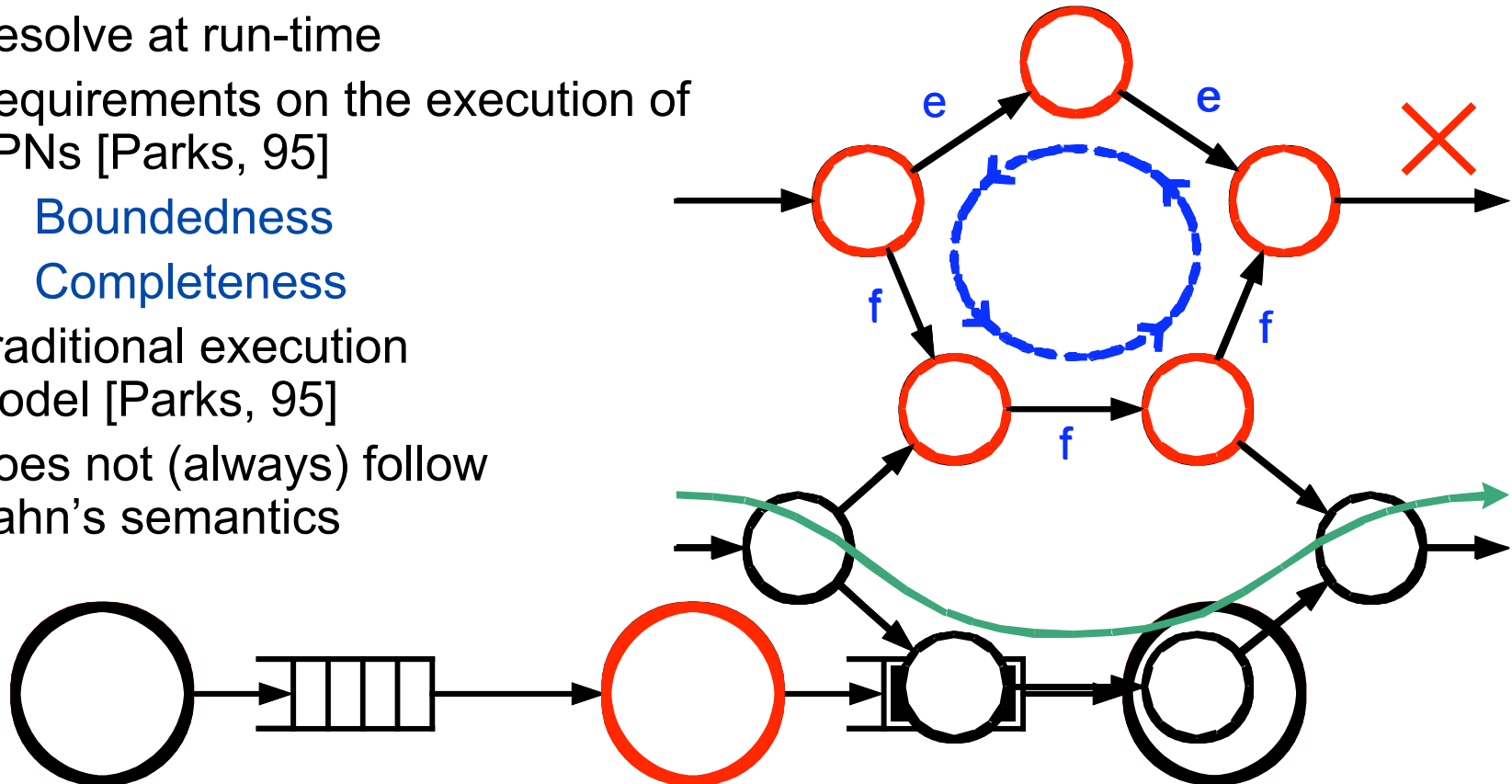
# 19 Kahn Process Networks (KPN)

- Data-dependent data rates  
(for instance Variable Length Decoding)
- Asynchronous reads and writes
- Continuous functions on streams
- Semantics: function compositions → fixed-point
- Determinate, scheduling independent (locality)
- Undecidable (e.g., buffer minimisation or deadlock freedom)




## 20 KPN

- Buffer management needs to be done at run-time
- Too small buffers lead to artificial deadlock  
Resolve at run-time
- Requirements on the execution of KPNs [Parks, 95]
  - Boundedness
  - Completeness
- Traditional execution model [Parks, 95]
- Does not (always) follow Kahn's semantics



## 21 Improved KPN scheduler

- A scheduler that is correct for every KPN cannot exist
- A scheduling algorithm has been defined which is correct for every **bounded** and **effective** KPN. It is executed in bounded memory by our scheduler and produces the complete output.

- 
1. Schedule enabled processes (in a fair way)
  2. Until (local) deadlock occurs (cyclic causal chain)
  3. Resolve deadlock by increasing the smallest full FIFO

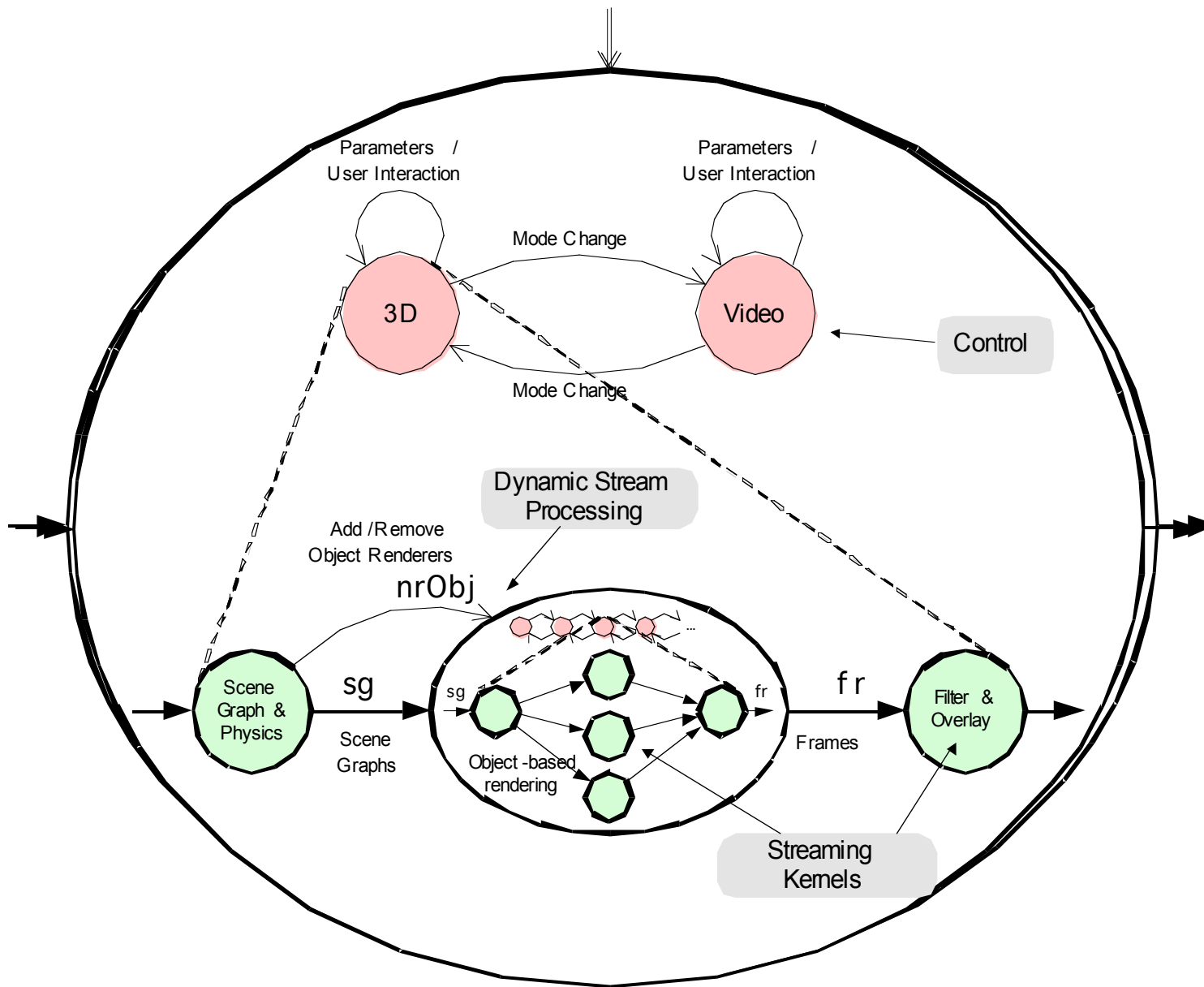
## 22 Reactive Process Networks

### Limitations of KPN

- No non-determinism / reactive behaviour
- Only continuous functions

### Extension Reactive Process Networks

- Integrate reactive behaviour, (sporadic) event communication with determinate dataflow models
- Coordination between streaming and control required to get some level of predictability
- Determinacy is lost



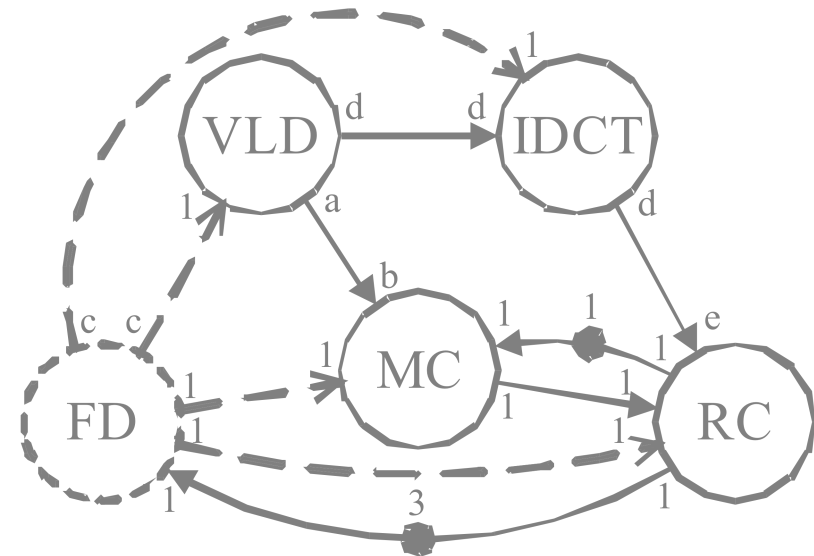
## 24 Scenarios

- Worst-case execution time estimation is overly pessimistic in many modern dynamic applications
- Scenarios are detectable situations in which better bounds can be given. This can e.g. be exploited by on-line scheduling and frequency and voltage scaling methods.



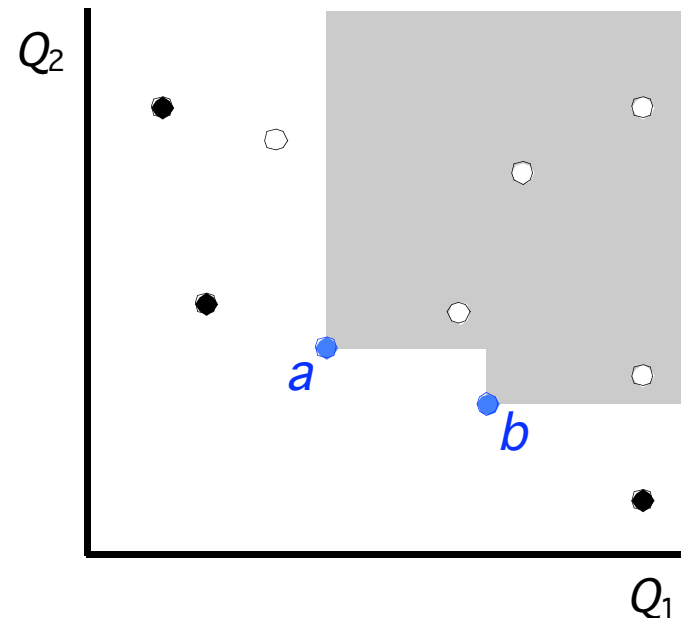
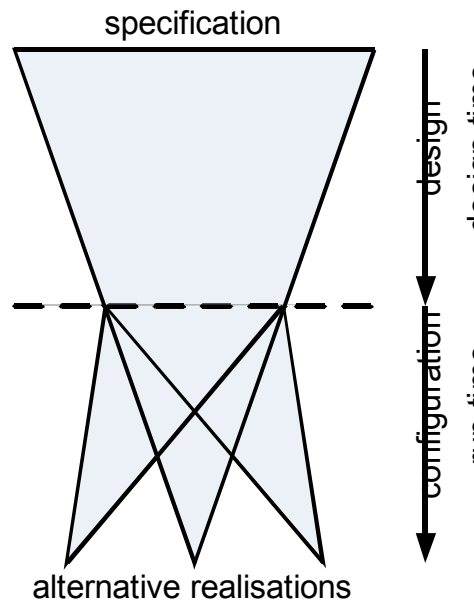
## 25 Scenario-Aware Data Flow (SADF)

- Problem - traditional data flow models are not capable of expressing the dynamism of modern streaming applications
- Dynamism supported by SADF
  - Parameterized numbers of consumed/produced tokens
  - Inactive processes
  - Discrete execution time distributions
  - Correlations between above for different processes
- Example: Pipelined MPEG-4 SP
- Analysis of correctness as well as worst-case and long-run average performance is possible
- Tool support for exhaustive and simulation-based performance analysis



## 26 Analysing trade-offs

- Inherent trade-offs between computation, communication, storage and quality or other non-functional properties
- Pareto points are abstractions of multi-dimensional optimisation criteria / cost functions
- An Algebra of Pareto Points  
Incremental, compositional computation of system trade-offs.



## 27 Challenges

- Expressivity while maintaining analyzability
- Dynamism and reconfiguration
- Abstraction without losing accuracy
- Composability and compositionality
- MoCs for non-functional aspects
- Unification or integration of MoCs

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