

# Real Time Controller Synthesis

With
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#### **UPPAAL TIGA**

UPPAAL for Timed Games

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#### Welcome!

UPPAAL TIGA (Fig. 1) is an extension of UPPAAL [BDL04] and it implements the first efficient on-the-fly algorithm for solving games based on timed game automata with respect to reachability and safety properties. Though timed games for long have been known to be decidable there has until now been a lack of efficient and truly on-the-fly algorithms for their analysis.

The algorithm we propose [CDFLL05] is a symbolic extension of the on-the-fly algorithm suggested by Liu & Smolka [LS98] for linear-time model-checking of finite-state systems. Being on-the-fly, the symbolic algorithm may terminate long before having explored the entire state-space. Also the individual steps of the algorithm are carried out efficiently by the use of so-called zones as the underlying data structure. Our tool implements various optimizations of the basic symbolic algorithm, as well as methods for obtaining time-ontimal.

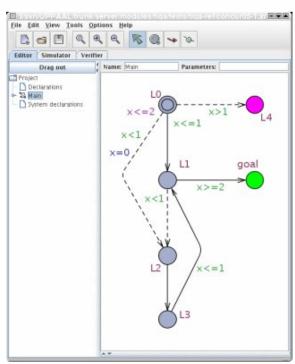


Figure 1: UPPAAL TIGA on screen.

#### Latest News

Versions 0.10 and 0.11 released.

7 July 2007

Versions 0.10 and 0.11 are released today. Version 0.11 contains a new concrete simulator that allows the user to play strategies from the GUI, Both versions fix the following bugs: maximal constants in the formula are now taken into account, the command line simulator is new and works better, delay when no clock was used, better user feedback, end-of-game detection fixed, other bugs involving delays in the strategy, precision problems in the simulator, and leak in the DBM library. These new versions have also the following new features: options to control the type of strategy output, better control on the search ordering (forward and backward), cooperative strategies, and time optimal strategies. The manual has been updated to reflect these new features.



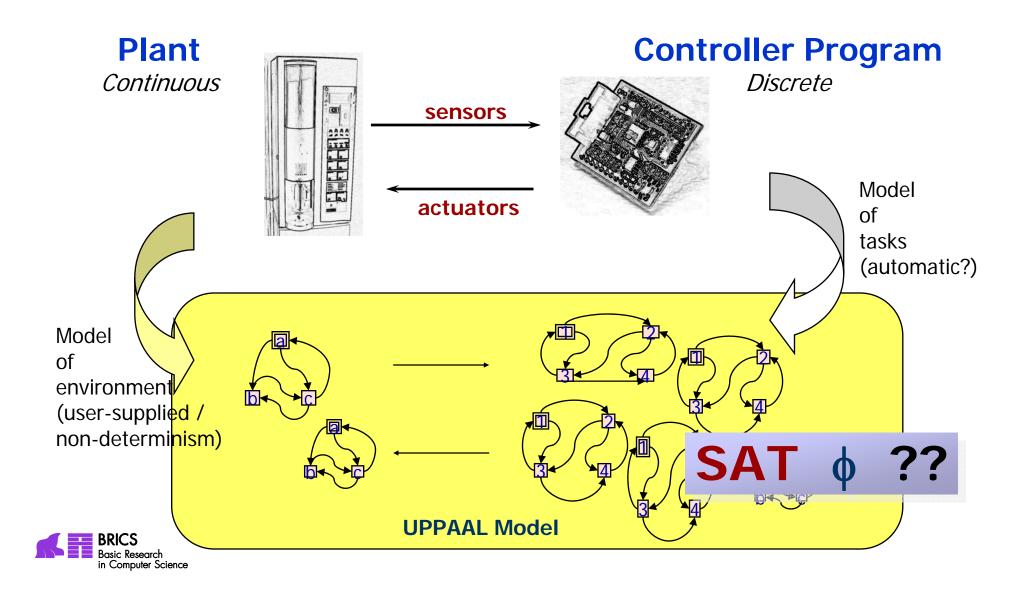


See CAV 2007 & CONCUR 2005



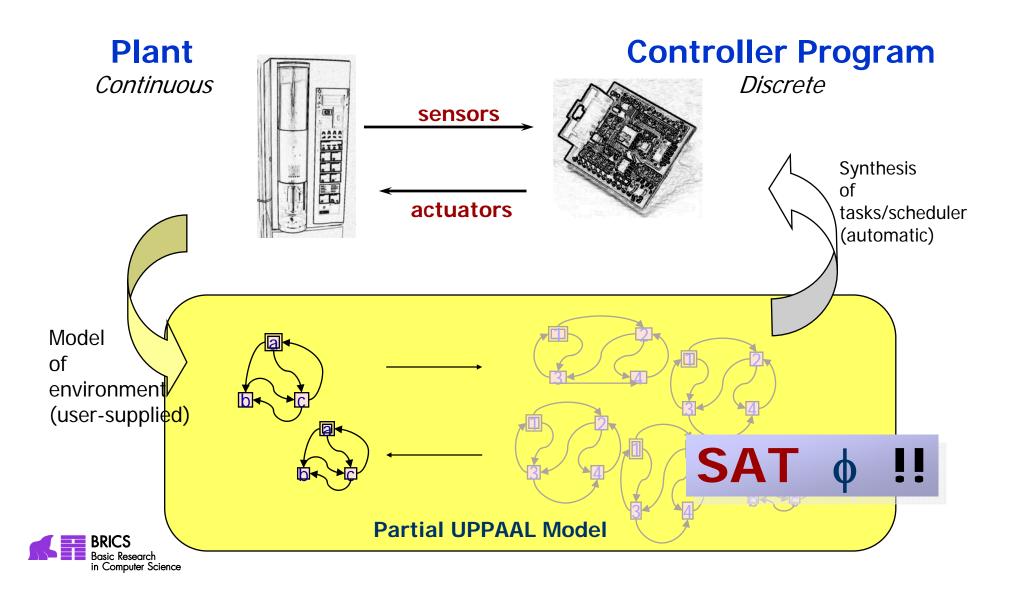


## Real Time Model Checking



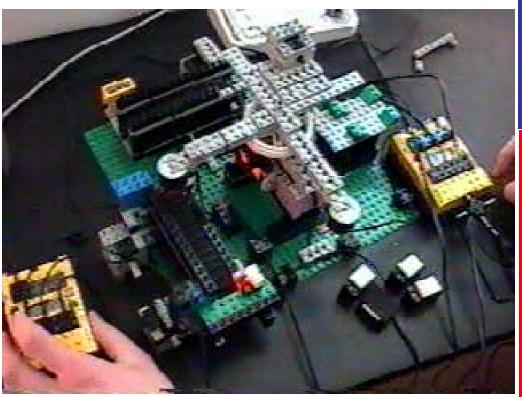


## Real Time Scheduling & Control Synthesis



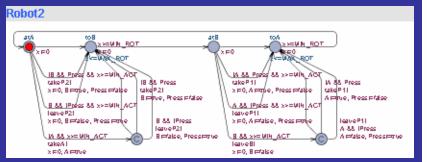
## Controller Synthesis and Timed Games

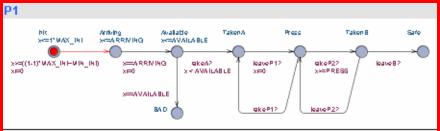
#### Production Cell

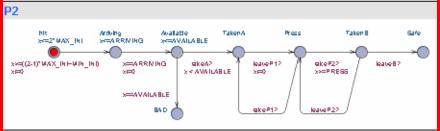


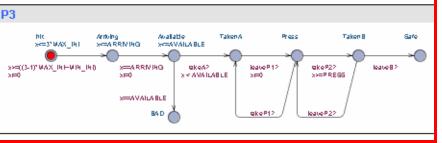
GIVEN System moves S, Controller moves C, and property  $\phi$ FIND strategy  $S_C$  such that  $S_C \mid S \models \phi$ 

A Two-Player Game

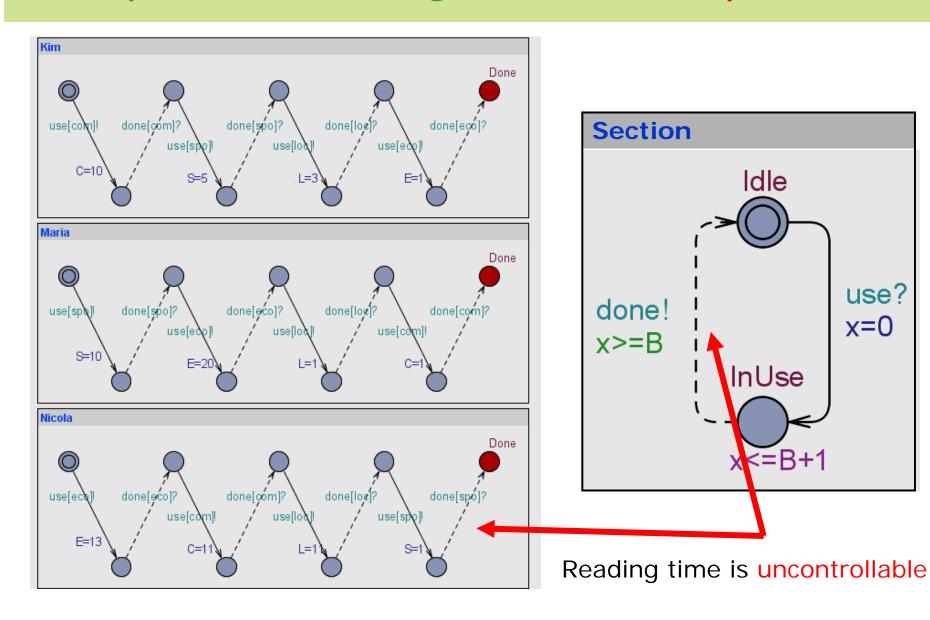






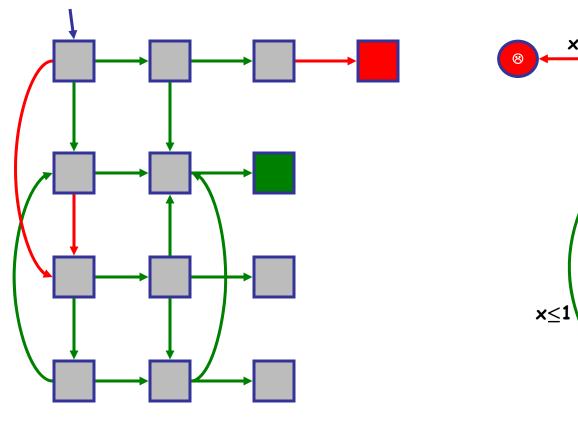


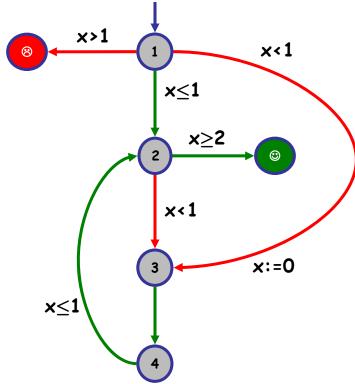
## Dynamic Scheduling = Controller Synthesis



## Untimed and Timed Games

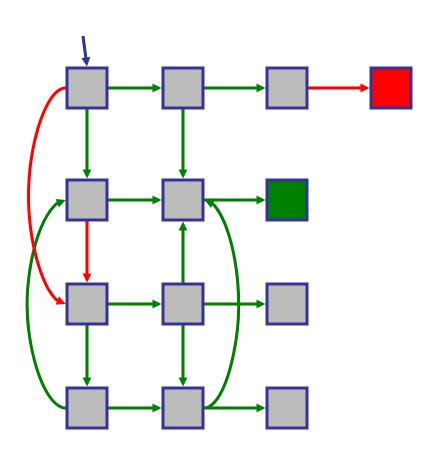
#### Reachability / Safety Games





- → Uncontrollable
- -- Controllable

#### Reachability / Safety Games



Strategy:

 $F: Run(A) \rightarrow E_c$ 

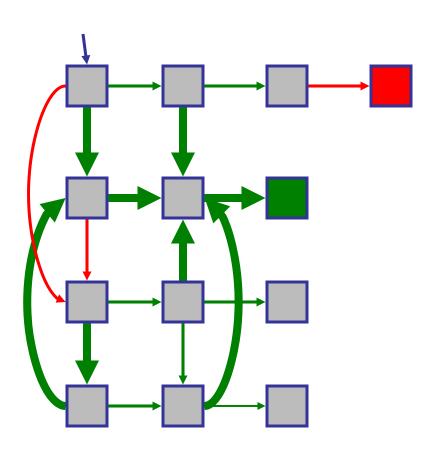
Memoryless strategy:

 $F: Q \rightarrow E_c$ 

→ Uncontrollable

→ Controllable

#### Reachability / Safety Games



Strategy:

 $F: Run(A) \rightarrow E_c$ 

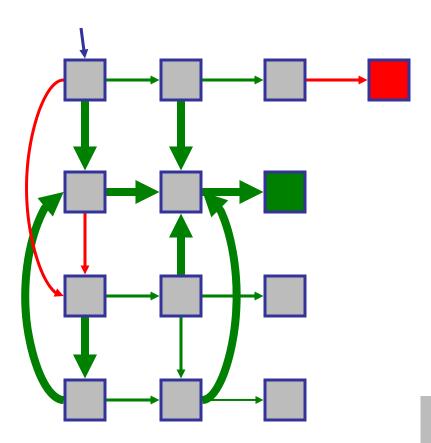
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#### Reachability / Safety Games



Strategy:

 $F: Run(A) \rightarrow E_c$ 

Memoryless strategy:

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Winning Run:

States( $\rho$ )  $\cap G \neq \emptyset$ 

States( $\rho$ )  $\cap$  B =  $\emptyset$ 

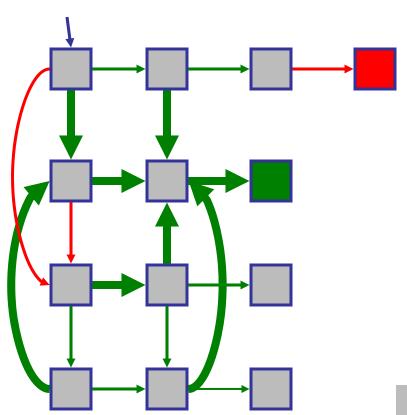
Winning Strategy:

 $Runs(F) \subseteq WinRuns$ 

## Loosing (memoryless) strategy

- Uncontrollable
- --> Controllable

#### Reachability / Safety Games



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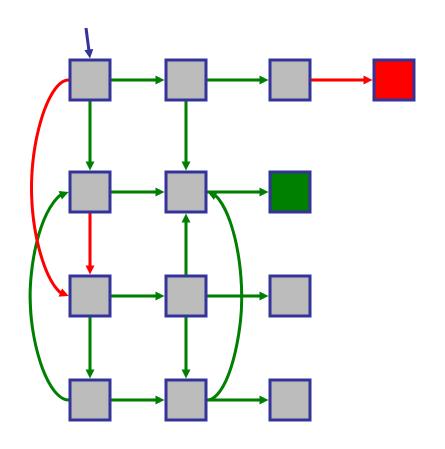
Winning Strategy:

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Winning (memoryless) strategy)

- → Uncontrollable
- --> Controllable

#### Backwards Fixed-Point Computation



cPred(X) = { 
$$q \in Q \mid \exists q' \in X. \ q \rightarrow_c q'$$
}  
uPred(X) = {  $q \in Q \mid \exists q' \in X. \ q \rightarrow_u q'$ }

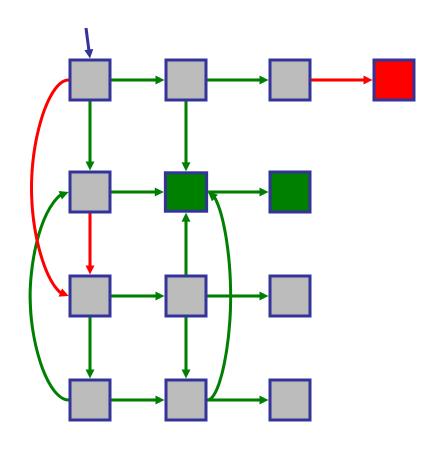
$$\pi(X) = cPred(X) \setminus uPred(X^C)$$

#### Theorem:

$$X \mapsto \pi(X) \cup Goal$$

- → Uncontrollable
- --> Controllable

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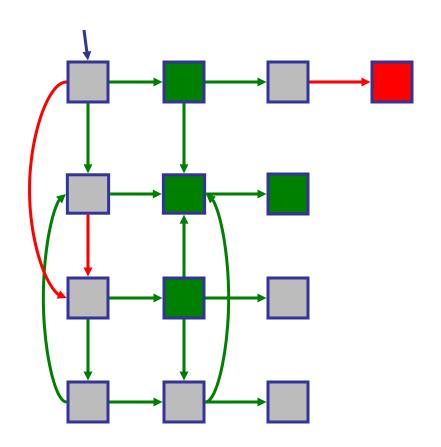
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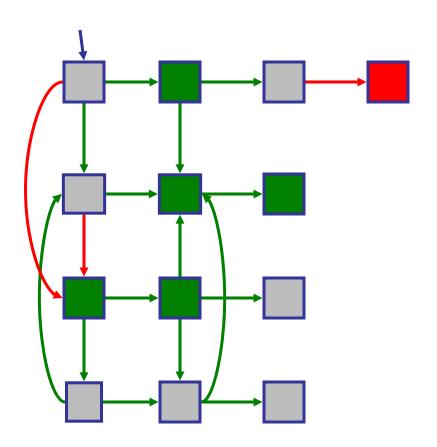
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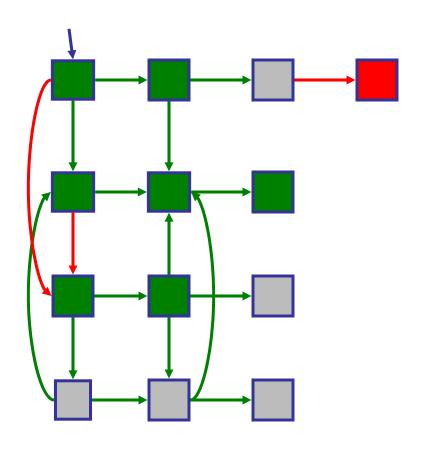
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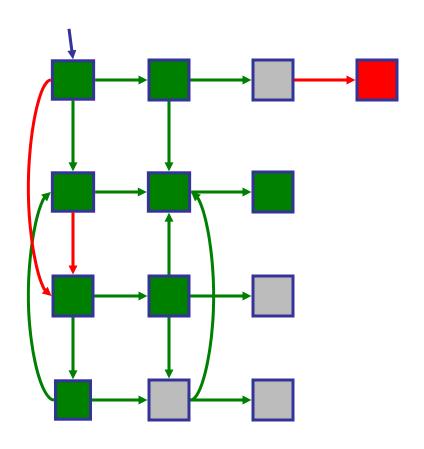
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#### Timed Games

#### Reachability / Safety Games

Strategy:

 $F: Run(A) \rightarrow E_c \cup \lambda$ 

Memoryless strategy:

 $F: Q \rightarrow E_c \cup \lambda$ 

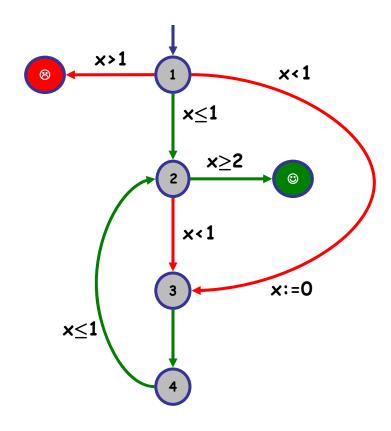
Winning Run:

States( $\rho$ )  $\cap G \neq \emptyset$ 

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Reachability / Safety Games

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States( $\rho$ )  $\cap G = \emptyset$ 

Winning Strategy:

 $Runs(F) \subseteq WinRuns$ 

 $x = 1 : \lambda$ x=1:cx>1 x<1 x≤1 x≥2  $x<2:\lambda$  $x \ge 2 : c$ x<1 x:=0 x≤1  $x<1:\lambda$ x≥1 : c  $x = 1 : \lambda$ x=1:c

Winning (memoryless) strategy)

Uncontrollable

-- Controllable

UPPAAL

- Timed Automata + Reachability [AD94]
- Time Game Automata: Control [MPS95, AMPS98]
- Time Optimal Control (reachability) [AM99]
- "False" On-the-fly Algorithm [AT01]

To be improved!!

- Priced Timed Automata (reachability) [LBB+01, ALTP01, LRS04, RL05]
- Price Timed Automata (safety) [BBL04]
- Price Optimal Control (reachability):
  - Acyclic PTA [LTMM02]
  - Bounded length [ABM04]
  - Strong non-zeno cost-behaviour [BCFL04]
- More to come !!

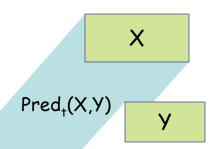
UPPAAL Cora

Backwards Fixed-Point Computation

#### Definitions

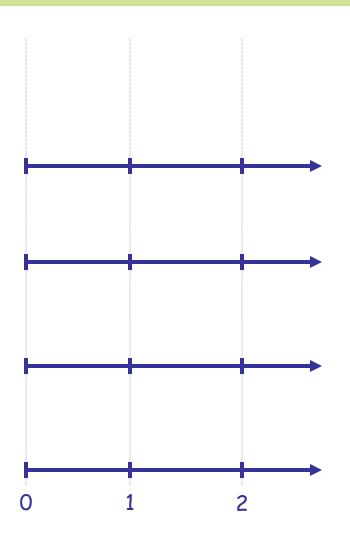
cPred(X) = { 
$$q \in Q \mid \exists q' \in X. q \rightarrow_c q'$$
}  
uPred(X) = {  $q \in Q \mid \exists q' \in X. q \rightarrow_u q'$ }  
Pred<sub>t</sub>(X,Y) = {  $q \in Q \mid \exists t. q^t \in X$  and  $\forall s \leq t. q^s \in Y^c$  }

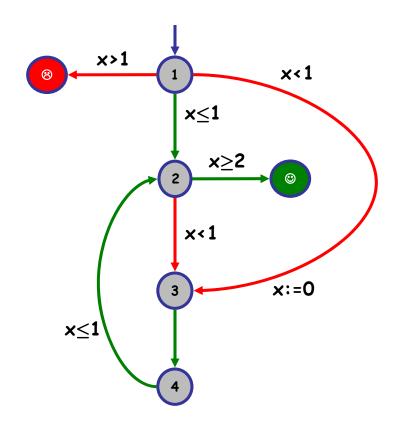
$$\pi(X) = \text{Pred}_{t}[X \cup \text{cPred}(X), \text{uPred}(X^{C})]$$

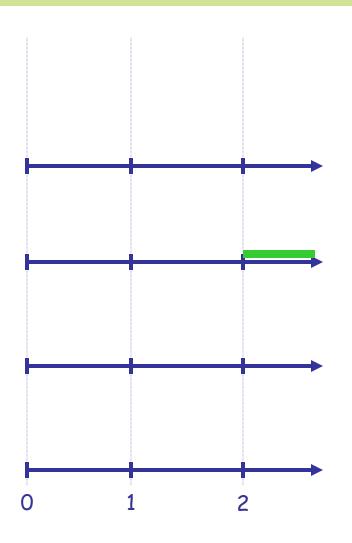


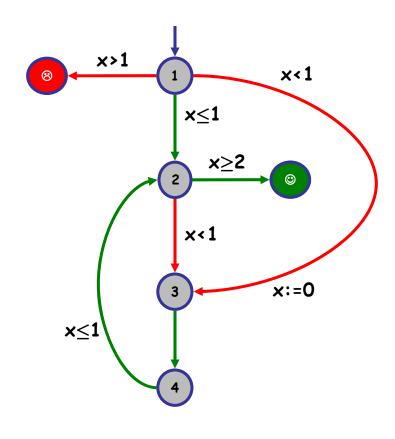
#### Theorem:

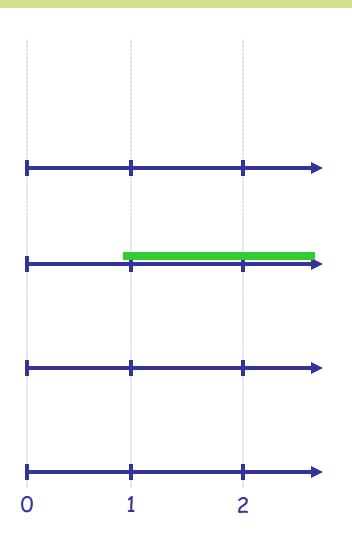
The set of winning states is obtained as the least fixpoint of the function:  $X \mapsto \pi(X) \cup Goal$ 

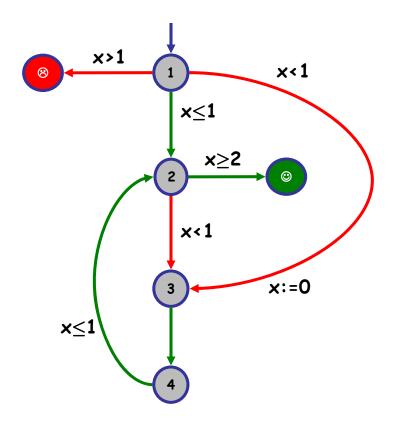


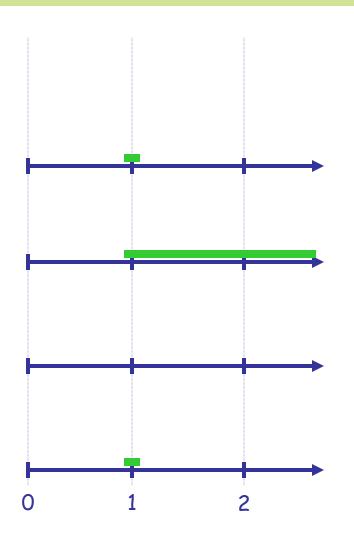


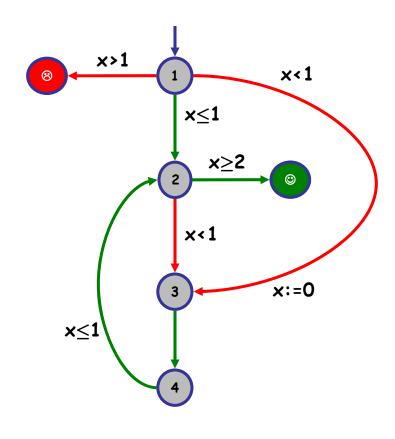


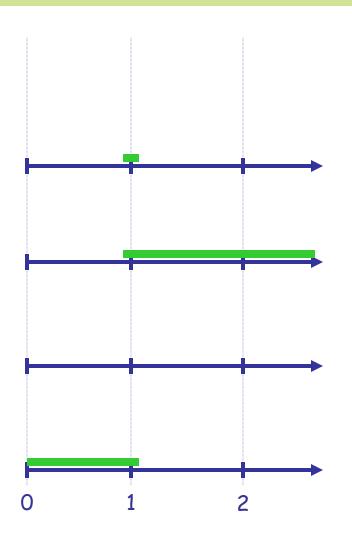


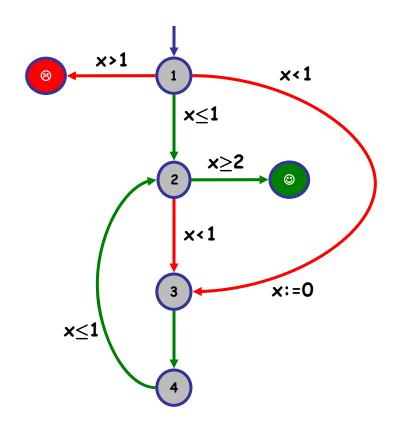


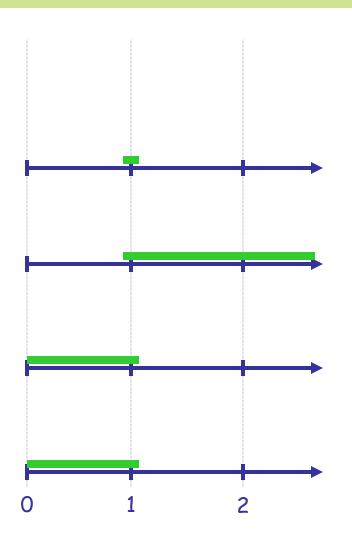


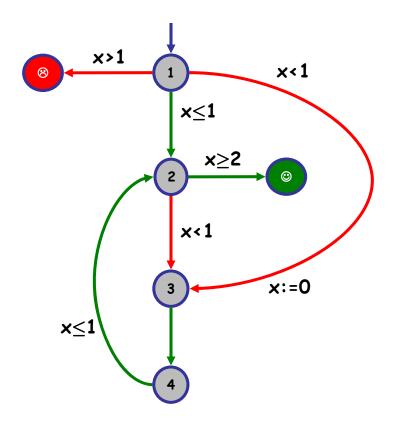


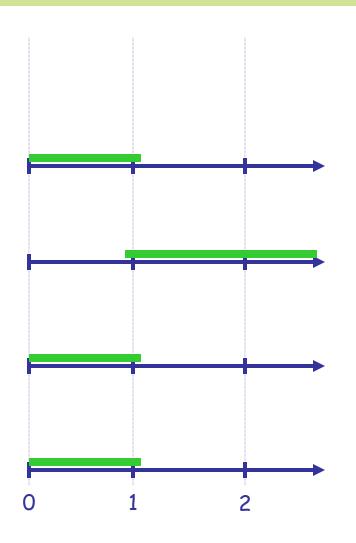


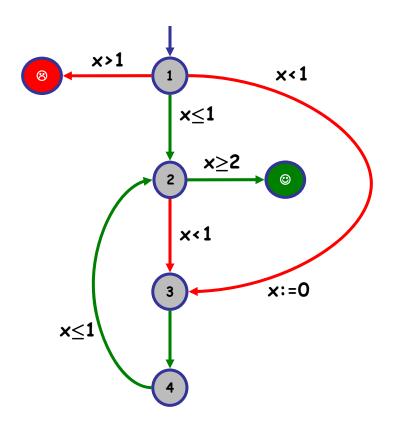




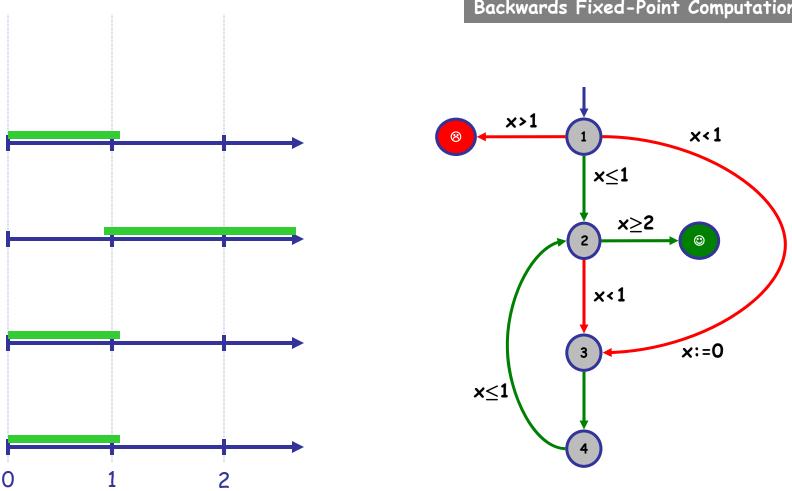








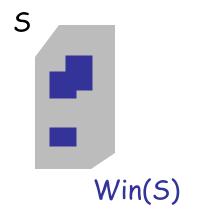




We want Forward and On-The-Fly Algorithm in order to avoid constructing all (backwards) reachable state-space and to allow for discrete variables (e.g. in UPPAAL)

## On-the-fly Algorithms for Timed Games

```
- S.S'...
are symbolic states, i.e. sets of concrete s
- G
is the set of (concrete) goal states;
- E = \{S \xrightarrow{c} S', S \xrightarrow{u} S'\}
the (finite) set of symbolic transitions (co
- Waiting \subseteq E
is the list of symbolic transitions waiting
- Passed
is the list of the passed symbolic states;
- Win[S] \subseteq S
is the subset of S currently known to be
- Depend[S] \subseteq E
indicates the edges (predecessors) of S wh information about S is obtained.
```



#### Initialization:

```
Passed \leftarrow \{S_0\} \text{ where } S_0 = \{(\ell_0, \vec{0})\}^{\prime};
Waiting \leftarrow \{(S_0, \alpha, S') \mid S' = \mathsf{Post}_{\alpha}(S_0)^{\prime}\};
Win[S_0] \leftarrow S_0 \cap (\{\mathsf{Goal}\} \times \mathbb{R}^X_{\geq 0});
Depend[S_0] \leftarrow \emptyset;
```

#### Main:

```
while ((Waiting \neq \emptyset) \land (s_0 \not\in Win[S_0])) do
       e = (S, \alpha, S') \leftarrow pop(Waiting);
       if S' \not\in Passed then
           Passed \leftarrow Passed \cup \{S'\};
           Depend[S'] \leftarrow \{(S, \alpha, S')\};
           Win[S'] \leftarrow S' \cap (\{\mathsf{Goal}\} \times \mathbb{R}^{X}_{\geq 0});
           Waiting \leftarrow Waiting \cup \{(S', \alpha, S'') \mid S'' = \mathsf{Post}_{\alpha}(S')^{\nearrow}\};
           if Win[S'] \neq \emptyset then Waiting \leftarrow Waiting \cup \{e\};
       else (* reevaluate *)<sup>a</sup>
           Win^* \leftarrow \operatorname{Pred}_t(Win[S] \cup \bigcup_{S \xrightarrow{c} T} \operatorname{Pred}_c(Win[T]),
                                                   \bigcup_{S \xrightarrow{u} T} \mathsf{Pred}_u(T \setminus Win[T])) \cap S;
           if (Win[S] \subseteq Win^*) then
               Waiting \leftarrow Waiting \cup Depend[S]; Win[S] \leftarrow Win^*;
           Depend[S'] \leftarrow Depend[S'] \cup \{e\};
       endif
endwhile
```

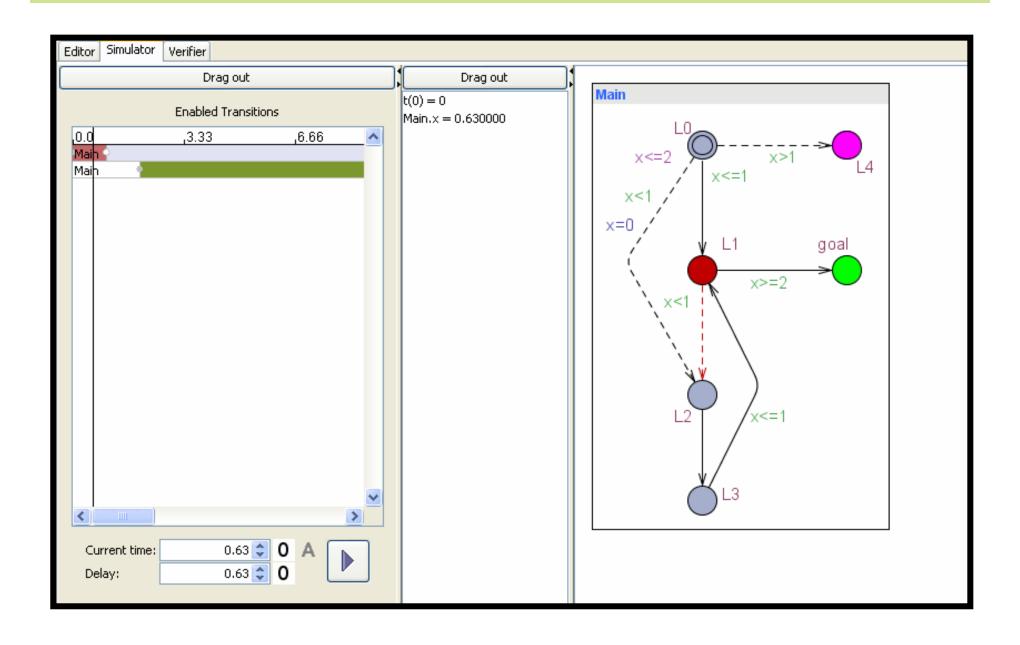
## On-the-fly Algorithms for Timed Games

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                                                 Depend[S_0] \leftarrow \emptyset:
  is the list of symbolic transitions waiting

    Passed

                                                UPPAAL Tiga
                                          Main:
  is the list of the passed symbolic states;
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  informatio
  5
                                                    if (Win[S] \subseteq Win^*) then
                                                       Waiting \leftarrow Waiting \cup Depend[S]; Win[S] \leftarrow Win^*;
                                                    Depend[S'] \leftarrow Depend[S'] \cup \{e\};
                                                 endif
              Win(S)
                                          endwhile
```

## UPPAAL Tiga: New Concrete Time Simulator

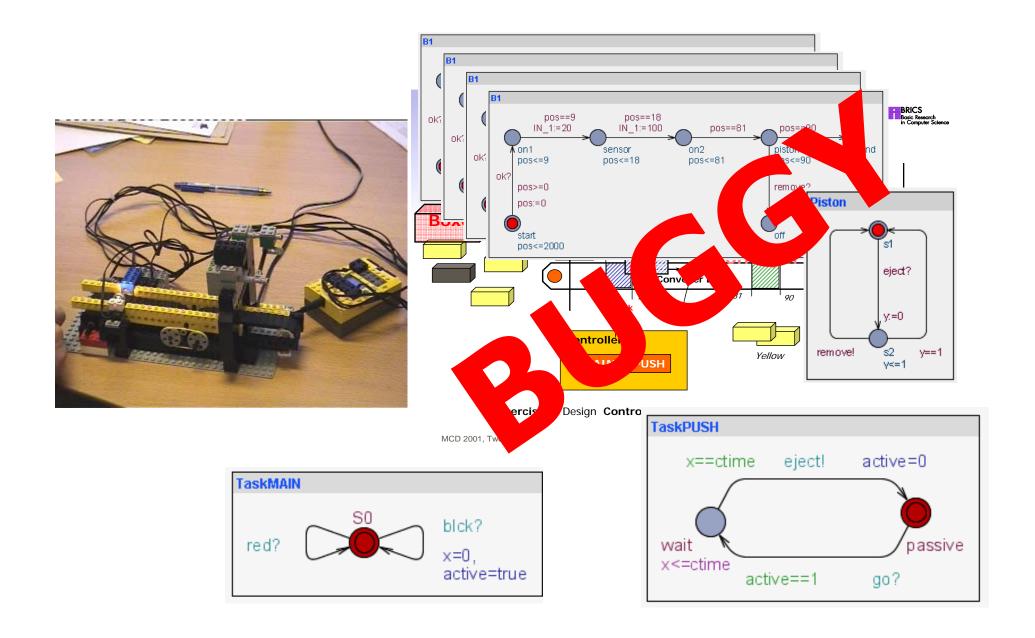


## UPPAAL Tiga: CTL Control Objectives

### Reachability properties:

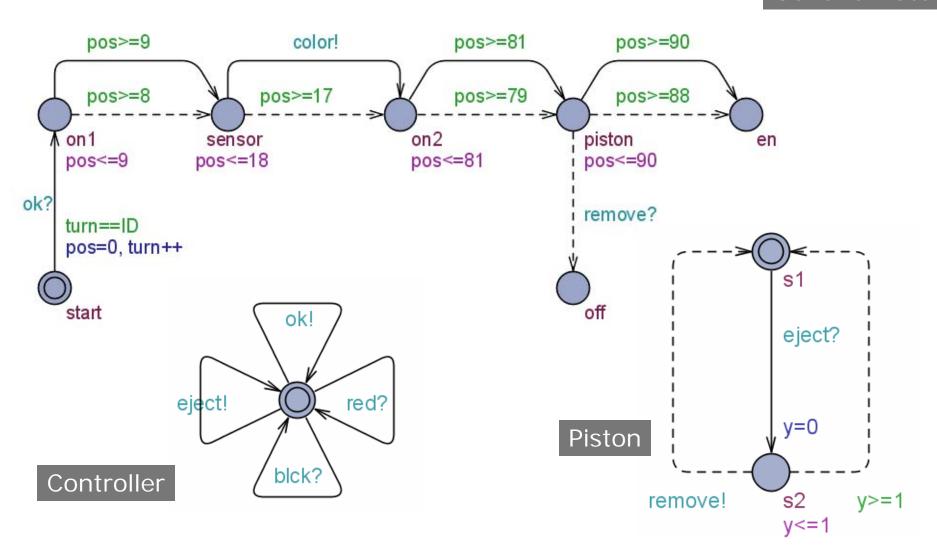
- control: A[p U q]
  until
- control:  $A \Leftrightarrow q \Leftrightarrow control$ : A[true U q]
- Safety properties:
  - control: A[p W q]
    weak until
  - control: A[] p ⇔ control: A[ p W false ]
- Time-optimality:
  - control\_t\*(u,g): A[ p U q ]
    - u is an upper-bound to prune the search, act like an invariant but on the path = expression on the current state.
    - g is the time to the goal from the current state (a lower-bound in fact), also used to prune the search.
       States with are pruned

## A Buggy Brick Sorting Program

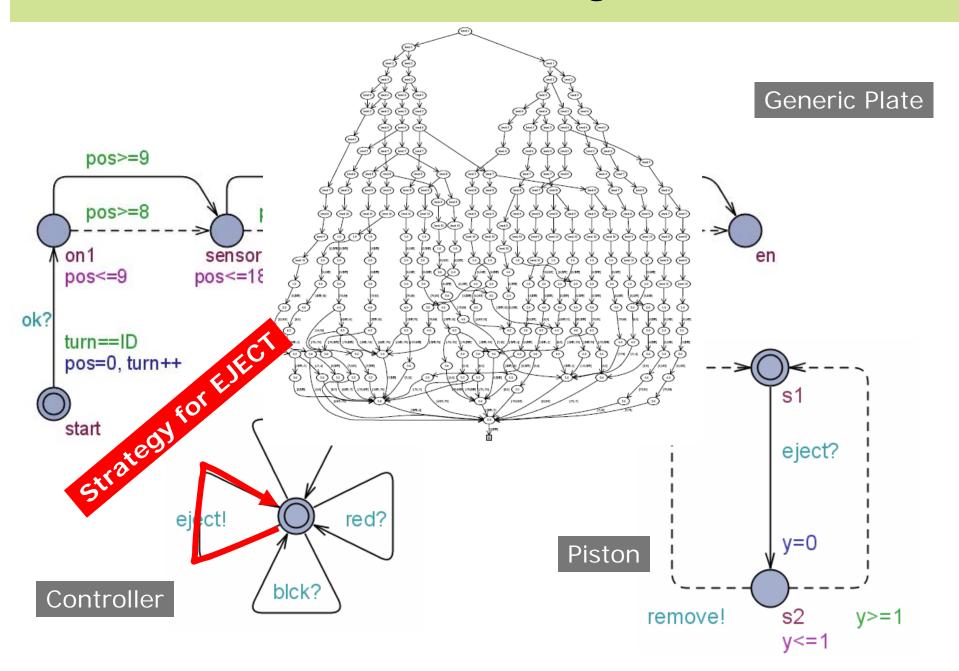


## **Brick Sorting**

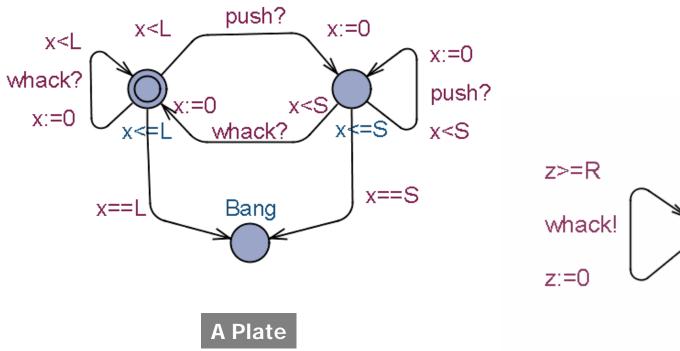
#### Generic Plate

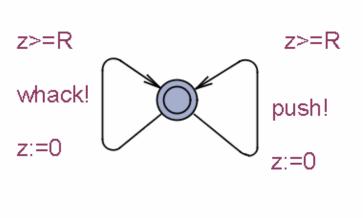


## **Brick Sorting**



### Balancing Plates / Timed Automata

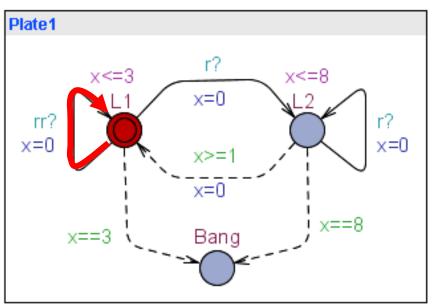


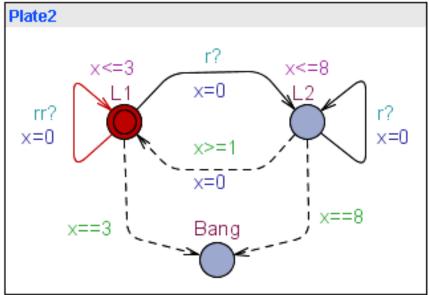


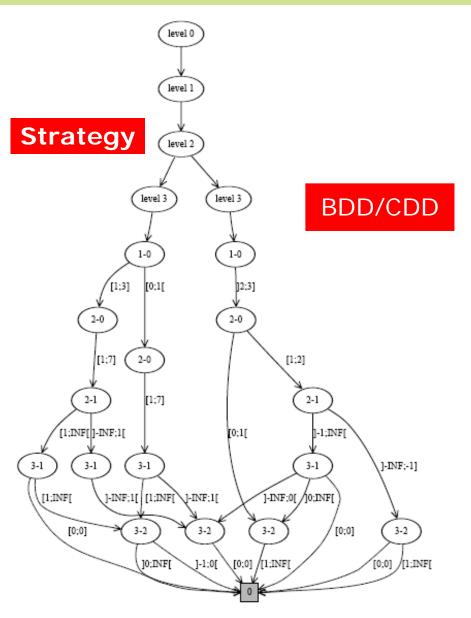
The Joggler

**E**□ ¬(Plate1.Bang or Plate2.Bang or ...)

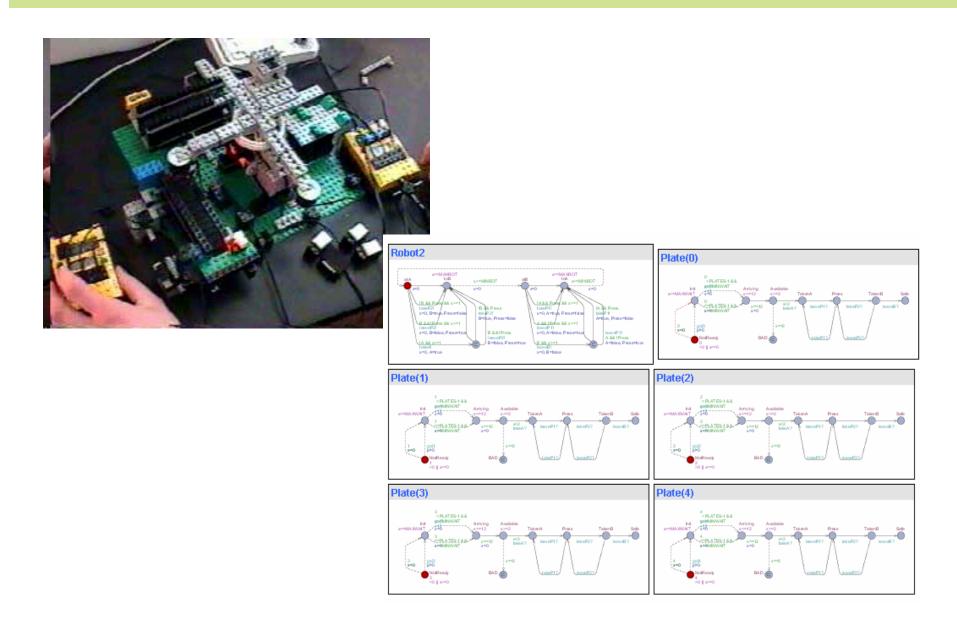
# Balancing Plates / Time Uncertainty







## Production Cell



# **Experimental** Results

Plates		Basic		Basic +inc		Basic +inc		Basic+lose +inc		Basic+lose +inc	
						+pruning		+pruning		+topt	
		time	mem	time	mem	time	mem	time	mem	time	mem
2	win	0.0s	1M	0.0s	1M	0.0s	1M	0.0s	1M	0.04s	1M
	lose	0.0s	1M	0.0s	1M	0.0s	1M	0.0s	1M	n/a	n/a
3	win	0.5s	19M	0.0s	1M	0.0s	1M	0.1s	1M	0.27s	4M
	lose	1.1s	45M	0.1s	1M	0.0s	1M	0.2s	3M	n/a	n/a
4	win	33.9s	1395M	0.2s	8M	0.1s	6M	0.4s	5M	1.88s	13M
	lose	-	-	0.5s	11M	0.4s	10M	0.9s	9M	n/a	n/a
5	win	-	-	3.0s	31M	1.5s	22M	2.0s	16M	13.35s	59M
	lose	-	-	11.1s	61M	5.9s	46M	7.0s	41M	n/a	n/a
6	win	-	-	89.1s	179M	38.9s	121M	12.0s	63M	220.3s	369M
	lose	-	-	699s	480M	317s	346M	135.1s	273M	n/a	n/a
7	win	-	-	3256s	1183M	1181s	786M	124s	319M	6188s	2457M
	lose	-	-	-	-	16791s	2981M	4075s	2090M	n/a	n/a

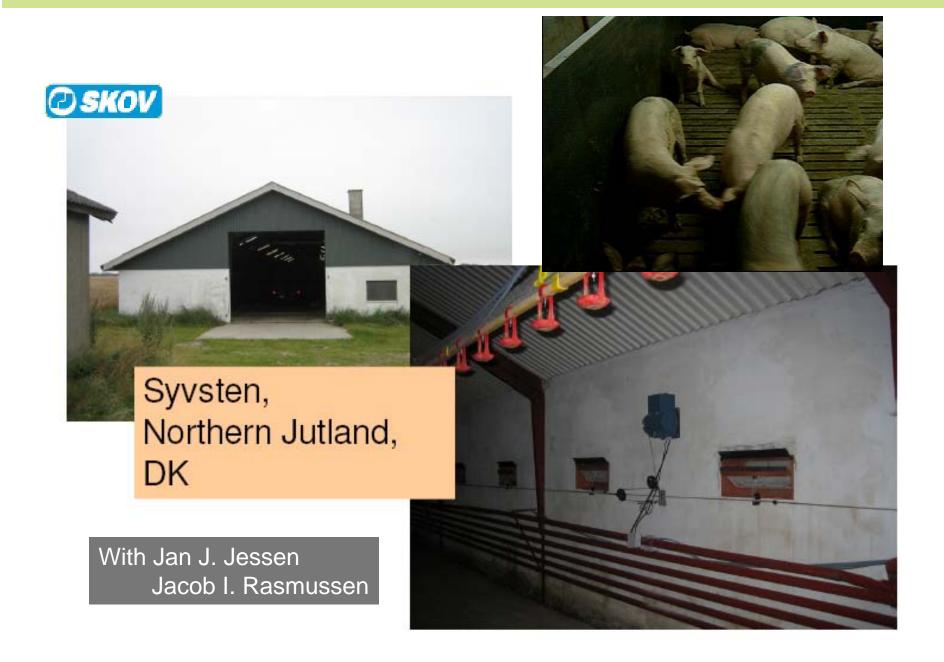
#### New Experimental Results Using UPPAAL 4.0 architecture

Model		3		6		12		50		100	
Old	С	0.1s	1M	12s	63M	-	-	-	-	-	-
	u	0.2s	3M	235s	273M	ı	ı	ı	ı	-	-
New	С	0.05s	3.5M	0.05s	3.5M	0.14s	55M	2.79s	104M	18.5s	426M
	u	0.02s	3.5M	0.04s	3.5M	0.12s	55M	2.32s	94M	15.6s	340M

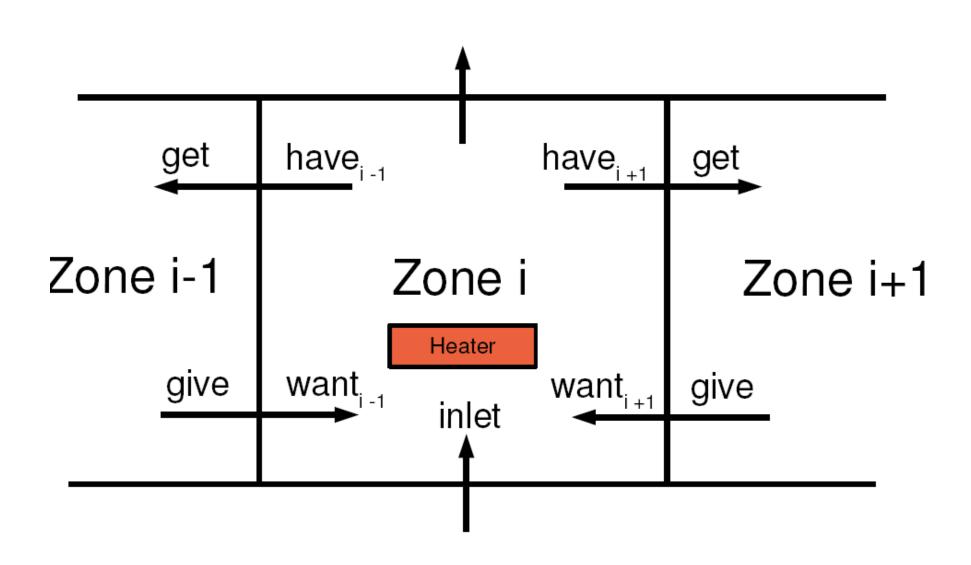
#### Tricks (Alexandre):

- UPPAAL pipeline architecture, which implies
  - \* active clock reduction
  - \* PW-list
  - \* UPPAAL optimizations (successor computation, postponed evaluation, reduced copies..)
  - \* improved DBM library
  - \* improved copy-on-write implementations
  - \* improved subtraction (vital)
  - \* enormously improved merge (between DBMs) (vital)

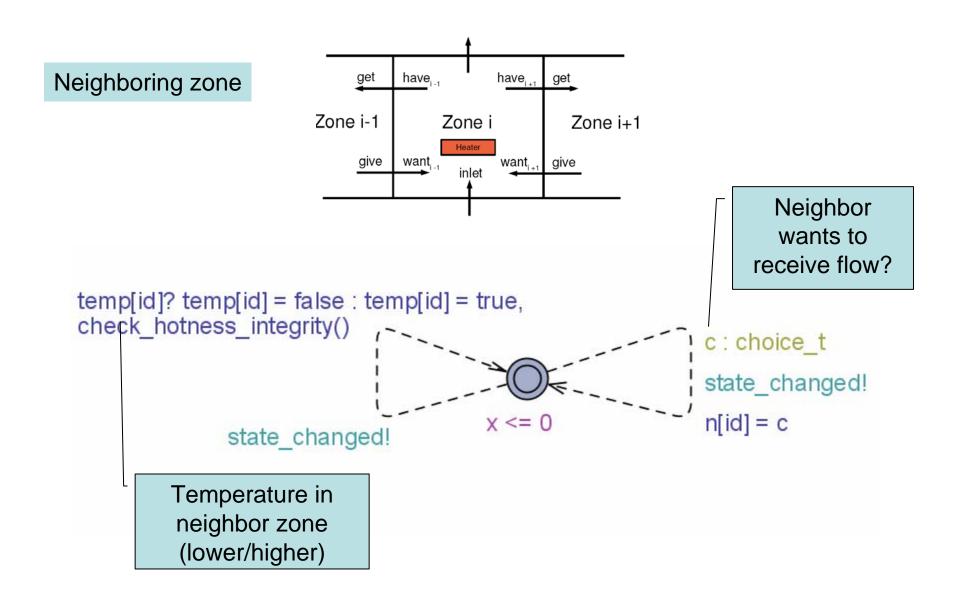
### Climate Control



#### Climate Control



### Climate Control / Neighbor



#### Climate Control / Controller

```
Zone Controller
                      bool flow balance (const choice t n0, const choice t n1, bool in, bool out)
                        bool o = out || (n[0] == WANT & and == HAVE) || (n[1] == WANT & and == HAVE);
                        bool i = in \mid \mid (n[0] == HAVE \quad \&\& n0 == WANT) \mid \mid (n[1] == HAVE \&\& n1 == WANT);
                        return o == i;
                   Decision
                               c0: choice t,
                               c1: choice t,
                               in: intbool t.
                               out : intbool t
                              flow_balance(c0,c1,in,out)
state_changed?
                               c[0] = c0,
                               c[1] = c1
                              heater = heat,
                              inlet = in.
                               outlet = out,
                              temp_derivative = compute_temperature(c0,c1,in,out,heat)
```

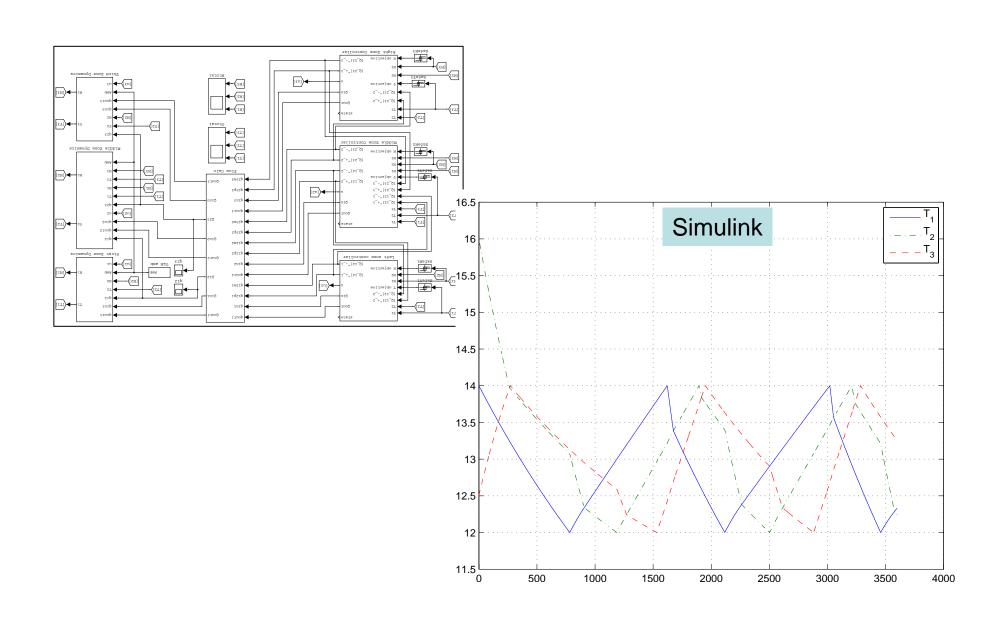
```
int compute temperature (const choice t c0, const choice t c1, const intbool t in, const intbool t out,
          int o,i,amp;
          //active out-flow
          o = out + (c0 == HAVE && n[0] == WANT) + (c1 == HAVE && n[1] == WANT);
          //active in-flow
          | i = in + (c0 == WANT & n[0] == HAVE) + (c1 == WANT & n[1] == HAVE);
          i = i >? 1;
          //Multiplier per incoming flow
          amp = (o * PER_OUT_CONTRIBUTION) / i;
Zone O
          if (objective) //heating
            return heat
                 + amp*(c0 == WANT && n[0] == HAVE ? (temp[0] ? (!hottest ? 3 : 1) : -1) : 0)
                 + amp^*(c1 == WANT & n[1] == HAVE ? (temp[1] ? (hottest ? 3 : 1) : -1) : 0)
                 + amp* (in ? -3 : 0)
                 + -(c0 == HAVE) //Motivation for participation, even when not neighbor doesn't want, og has air
                 + -(c1 == HAVE); //Motivation for participation, even when not neighbor doesn't want, og has ai.
          else //cooling
            return (heat ? -3 : 0)
                 + amp*(in ? 5 : 0)
                 + amp*(c0 == WANT && n[0] == HAVE ? (!temp[0] ? ( hottest ? 3 : 1) : -1) : 0)
                 + amp^*(c1 == WANT & n[1] == HAVE ? (!temp[1] ? (!hottest ? 3 : 1) : -1) : 0)
                 + (c0 == HAVE) //Motivation for participation, even when not neighbor doesn't want, og has air
state ch
                 + (c1 == HAVE); //Motivation for participation, even when not neighbor doesn't want, og has air
                              ппет – пт.
                               outlet = out,
                               temp_derivative = compute_temperature(c0,c1,in,out,heat)
```

## Obtaining executable code

```
Strategy for state:
                                                                BDD 289 nodes
   Zone i-1: (Temp. lower/equal, wants flow)
   Zone i+1: (Temp. lower/equal, no interaction)
  Hottest neighbor: i-l
   Objective: heat
is:
   Wants flow from i-1
   Wants flow from i+1
   inlet closed
   outlet off
  heater on
Strategy for state:
   Zone i-1: (Temp. greater, offers flow)
   Zone i+1: (Temp. greater, offers flow)
  Hottest neighbor: i+l
   Objective: cool
is:
   Has flow for i-1
   Has flow for i+1
                         Stragegy
  inlet open
   outlet on
   heater off
                          1296 cases
Strategy for state:
   Zone i-1: (Temp. lower/equal, no interaction)
   Zone i+1: (Temp. greater, no interaction)
   Hottest neighbor: i+l
   Objective: cool
```

control : A[]
((ZC.Init && objective) imply temp\_derivative > 0) &&
((ZC.Init && !objective) imply temp\_derivative < 0)

# Obtaining executable code



#### Conclusion & Future Work

- More Applications we need you!
- Efficient Algorithms for Optimal Infinite Scheduling
- Multipriced Timed Automata
- Priced Timed Games
  - Optimal strategies undecidable in general [Raskin ao]
  - Decidability in setting of 1 clock or strong nonzenoness.
- Timed Games with Imperfect information.
- Distributed and parallel implementations (PC clusters, GRID, Shared Memory Machines)

## Reading material

#### UPPAAL Cora (Priced Timed Automata):

- Buhrmann, Larsen, Rasmussen: Optimal Scheduling using Priced Timed Automata, ACM SIGMETRICS Performance Evaluation Review, vol. 32, nb. 4, 2005, pp. 34-40, ACM Press.
- Priced Timed Automata: Algorithms, and Applications G. Behrmann, K. G. Larsen, J. I. Rasmussen. In proc. of FMCO'04, LNCS vol. 3657, pp. 162-186, Springer Verlag, 2005.
- Patricia Bouyer. Weighted Timed Automata: Model-Checking and Games. In Proceedings of the 22nd Conference on Mathematical Foundations of Programming Semantics (MFPS'06), Genova, Italy, May 2006, ENTCS 158, pages 3-17. Elsevier Science Publishers.

#### UPPAAL Tiga (Timed Games & Controller Synthesis):

- Franck Cassez, Alexandre David, Emmanuel Fleury, Kim G. Larsen, and Didier Lime. Efficient on-the-fly algorithms for the analysis of timed games. CONCUR05, volume 3653 of Lecture Notes in Computer Science.
- Patricia Bouyer and Fabrice Chevalier. On the Control of Timed and Hybrid Systems. EATCS Bulletin 89, pages 79-96, 2006.
- J.J. Jessen, J.I.Rasmussen, K.G.Larsen, A.David: <u>Guided Controller Synthesis for Climate Controller using UPPAAL TIGA</u>. Under Submission.