

# Structuring Interaction in BIP

Workshop on

## Foundations of Component-based Design

Embedded Systems Week

Salzburg, September 28, 2007

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VERIMAG

# Motivation for BIP

Provide a **unified composition framework** for describing and analyzing interaction between components in terms of **tangible, well-founded and organized concepts** instead of using dispersed mechanisms including semaphores, monitors, message passing, remote call etc.

**Requirements:** The framework

- relies on a minimal set of constructs and principles
- treats interaction and system architecture as first class entities that can be composed and analyzed - independently of the behavior of individual components
- is expressive enough to directly encompass heterogeneity of synchronization (rendezvous and broadcast) and execution mechanisms (synchronous and asynchronous) – not just the usual product of automata
- provides automated support for component integration and generation of glue code meeting given requirements

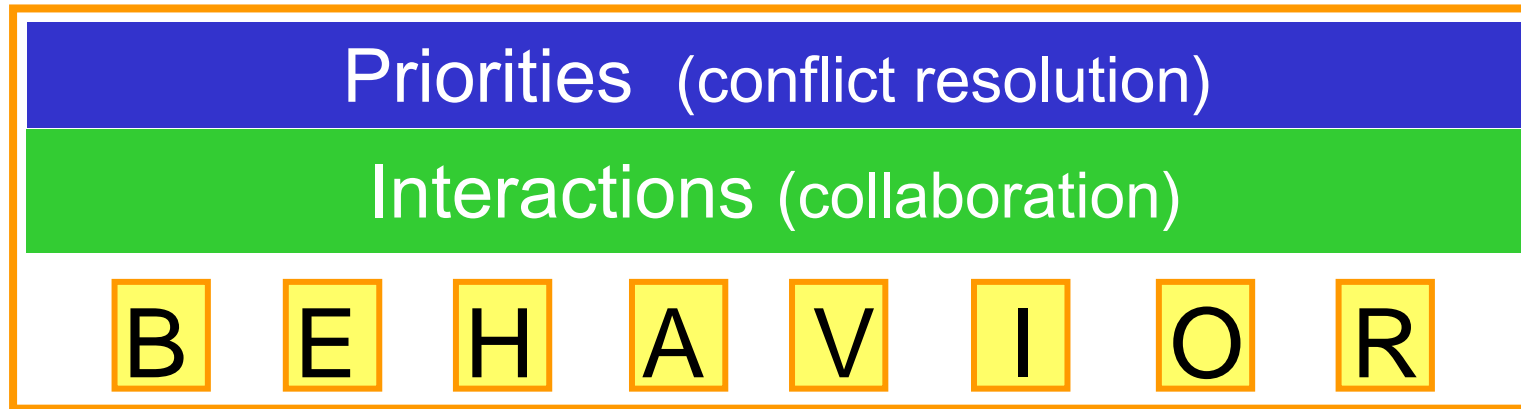
# Overview



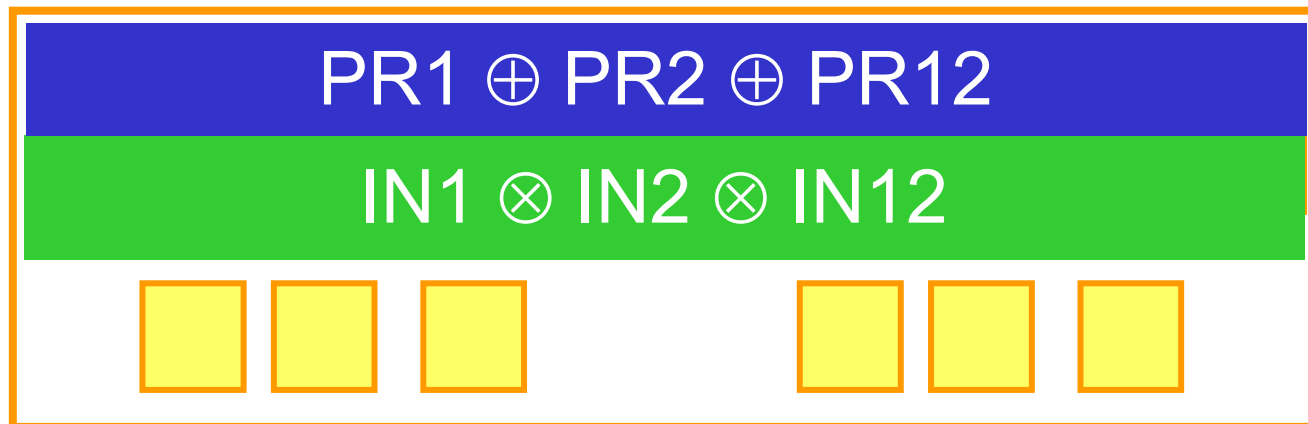
- BIP: Basic Concepts
- The Algebra of Connectors
- One-shot vs. Multi-shot semantics
- Discussion

# BIP: Basic Concepts

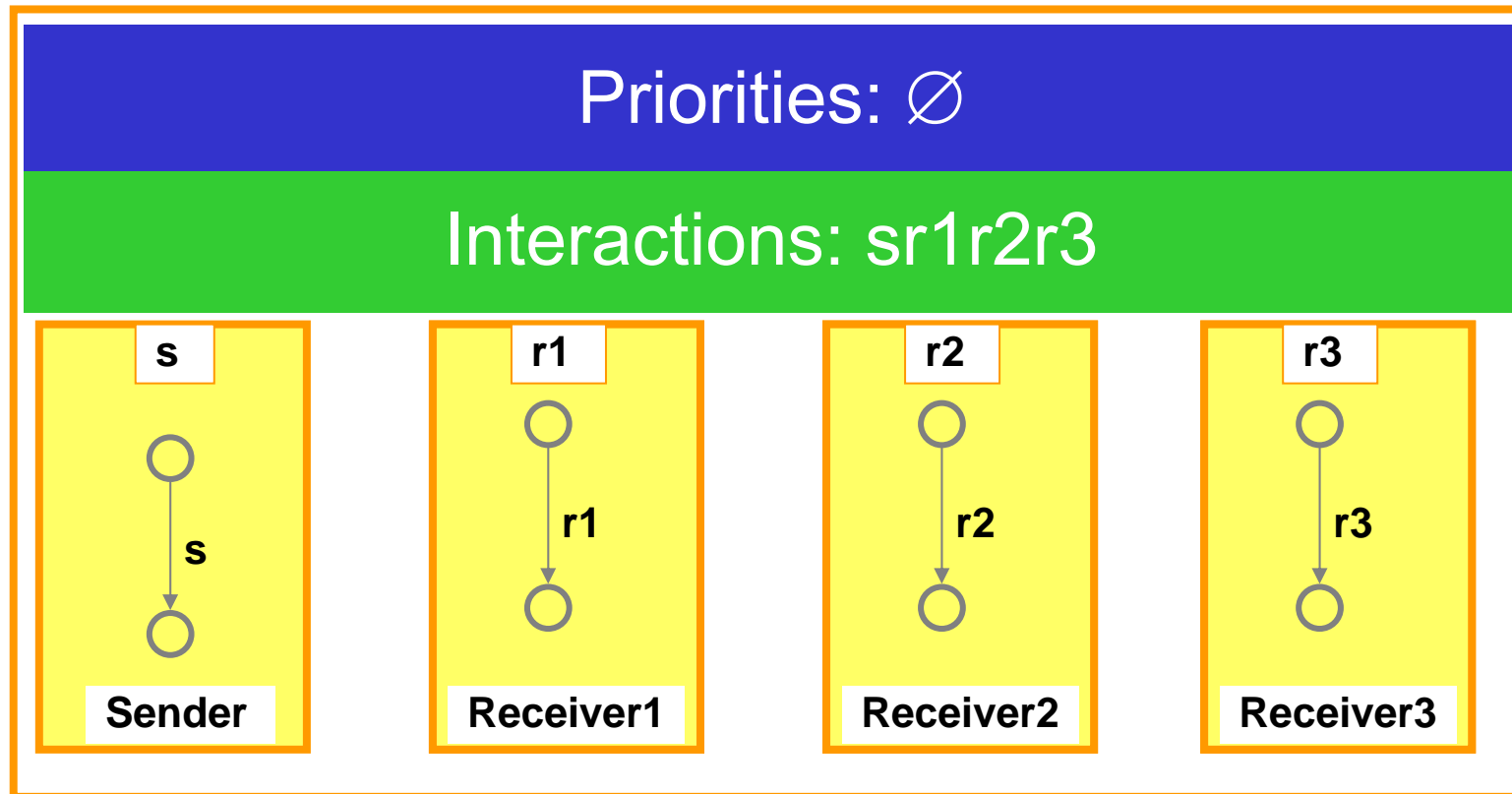
## Layered component model



## Composition (incremental description)



# BIP: Basic Concepts

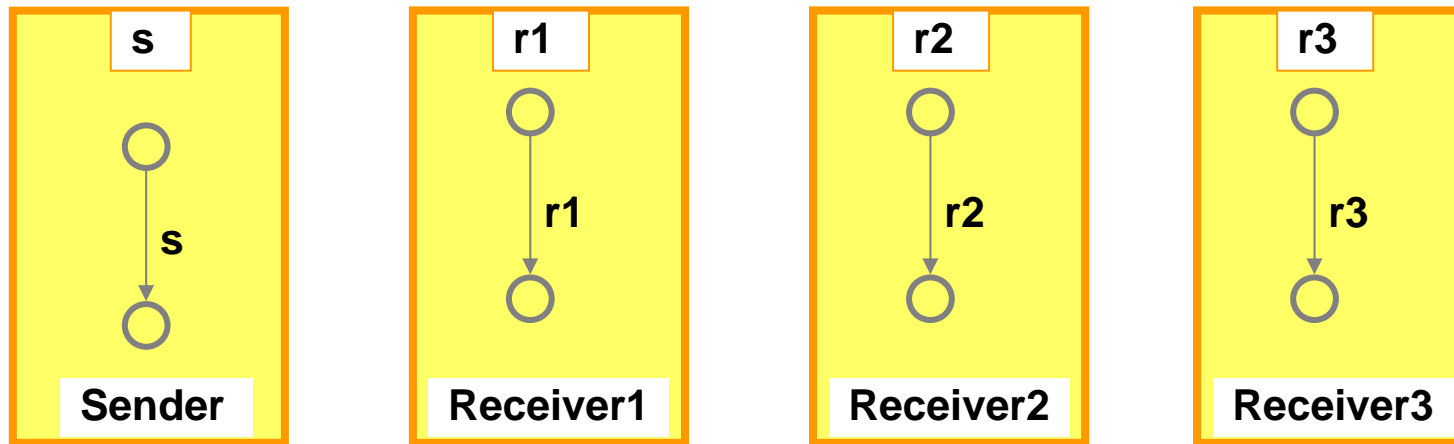


Rendezvous

# BIP: Basic Concepts

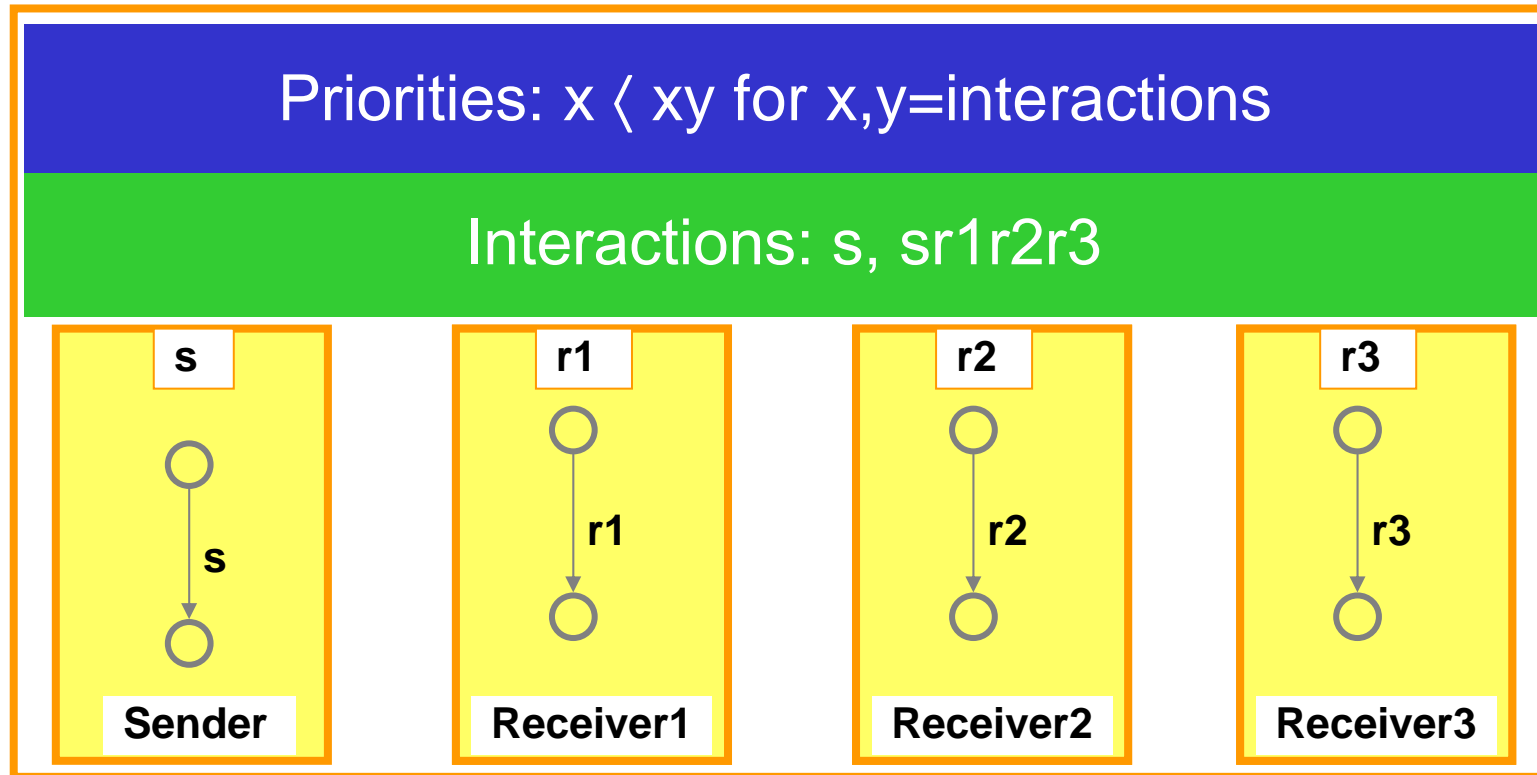
Priorities:  $x \prec xy$  for  $x, y = \text{interactions}$

Interactions:  $s, sr_1, sr_2, sr_3, sr_1r_2, sr_2r_3, sr_1r_3, sr_1r_2r_3$



## Broadcast

# BIP: Basic Concepts

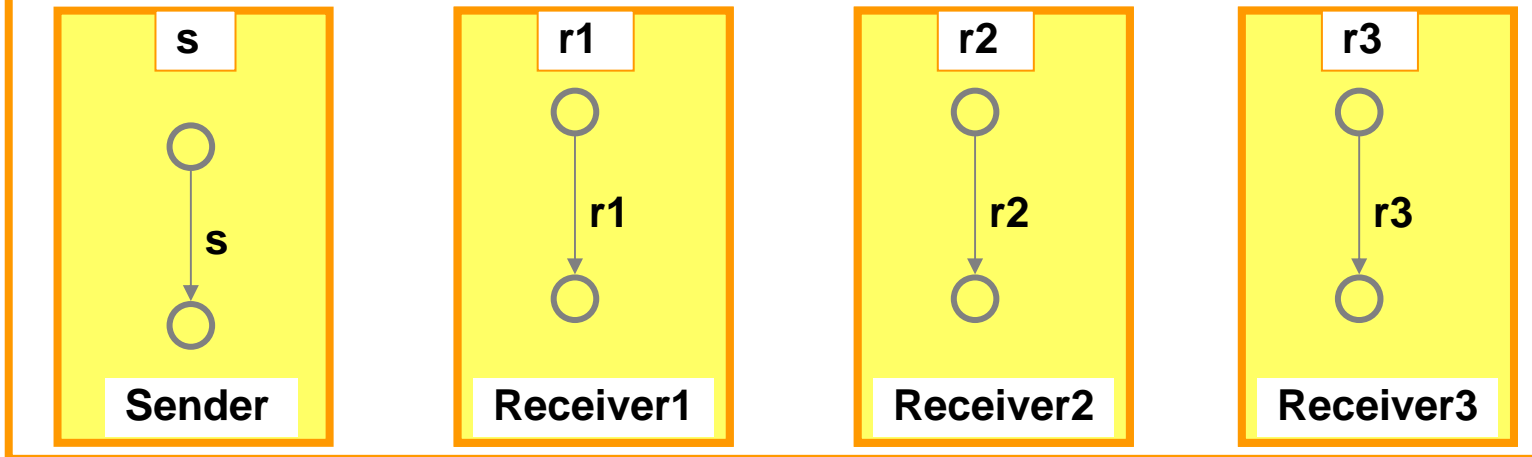


## Atomic Broadcast

# BIP: Basic Concepts

Priorities:  $x \prec xy$  for  $x, y = \text{interactions}$

Interactions:  $s, sr1, sr1r2, sr1r2r3$

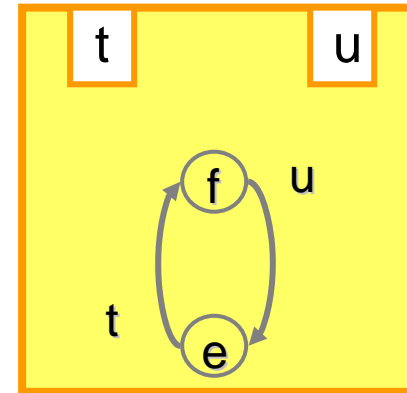
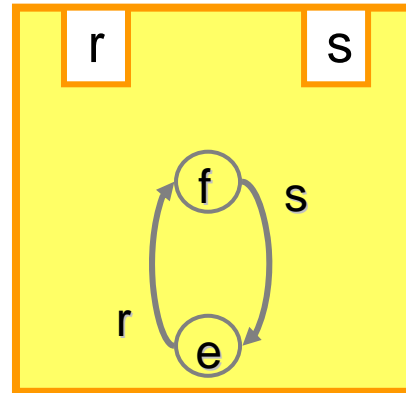
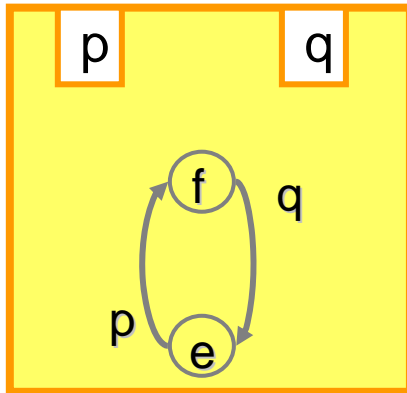


## Causal Chain

# BIP: Basic Concepts

Priorities:  $x \prec xy$  for  $x, y = \text{interactions}$

Interactions:  $p, qr, st, u$

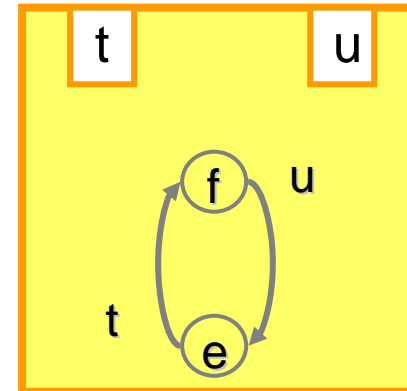
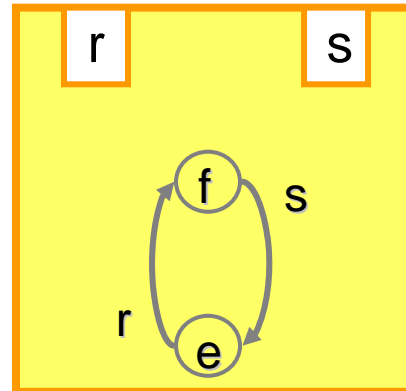
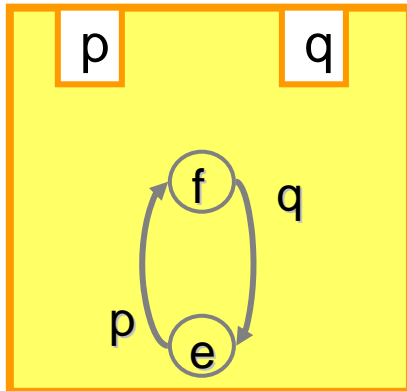


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# BIP: Basic Concepts

Priorities:  $x \prec xy$  for  $x, y = \text{interactions}$

Interactions:  $p, qr, st, u, pst, pu, qru$

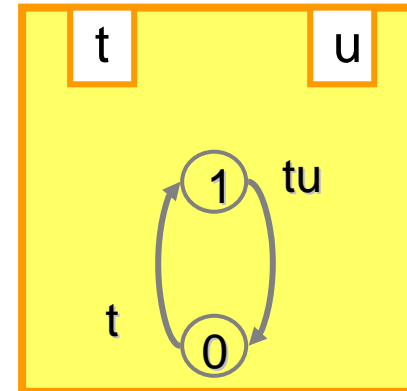
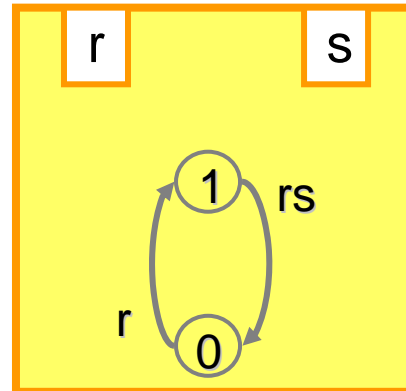
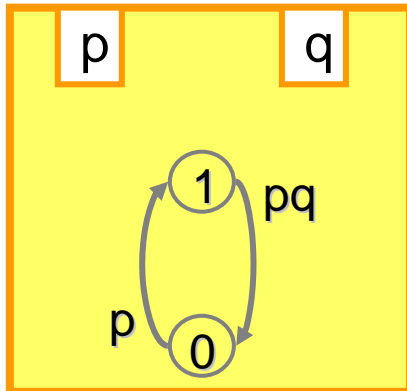


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# BIP: Basic Concepts

Priorities:  $x \prec xy$  for  $x,y$ =interactions

Interactions:  $p, pqr, pqrst, pqrstu$



## Mod8 Counter

## BIP: Basic Concepts - Semantics

- a set of atomic components  $\{B_i\}_{i=1..n}$   
where  $B_i = (Q_i, 2^{P_i}, \rightarrow_i)$
  - a set of interactions  $\gamma \in 2^P$  with  $P = \cup_{i=1..n} P_i$   
and  $P_i \cap P_j = \emptyset$   $P = \cup_{i=1..n} P_i$
  - a strict partial order  $\pi \subseteq 2^P \times 2^P$
- $\left. \vphantom{\begin{matrix} \bullet \\ \bullet \\ \bullet \end{matrix}} \right\} \pi \gamma (B_1, \dots, B_n)$

### Interactions

$$\frac{a \in \gamma \wedge \forall i \in [1, n] q_i - a \cap P_i \rightarrow_i q'_i}{(q_1, \dots, q_n) - a \rightarrow_\gamma (q'_1, \dots, q'_n) \text{ where } q'_i = q_i \text{ if } a \cap P_i = \emptyset}$$

### Priorities

$$\frac{q - a \rightarrow_\gamma q' \wedge \neg (\exists q - b \rightarrow_\gamma \wedge a \pi b)}{q - a \rightarrow_\pi q'}$$

*Other parallel composition operators (CCS, SCCS, CSP)  
can be expressed in BIP*

# Overview

- BIP: Basic Concepts



- The Algebra of Connectors
- One-shot vs. Multi-shot semantics
- Discussion

## The Algebra of Interactions $AI(P)$

Broadcast	$s+sr_1+sr_2+sr_1r_2 = s(1+r_1)(1+r_2)$
Causality Chain	$s+sr_1+sr_1r_2 = s(1+r_1(1+r_2))$

**Syntax:**  $x ::= 0 \mid 1 \mid p \in P \mid x.x \mid x + x$

where  $P$  is a set of ports, such that  $0, 1 \notin P$

$+$	<i>union</i>	idempotent, associative, commutative, identity 0
$\cdot$	<i>synchronization</i>	idempotent, associative, commutative, identity 1, absorbing 0, distributive wrt $+$

**Semantics:** defined by the function  $\| \cdot \|: AI(P) \rightarrow 2^{2^P}$

$$\|0\| = \emptyset$$

$$\|1\| = \{\emptyset\}$$

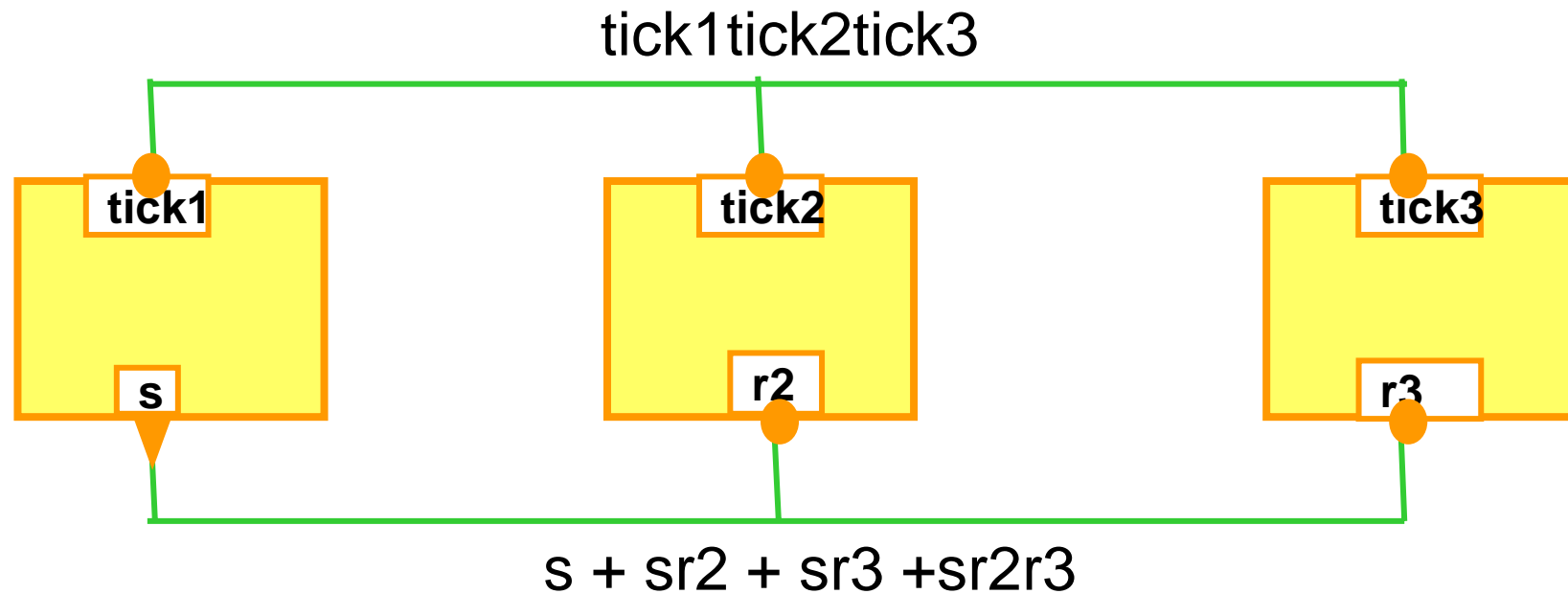
$$\|p\| = \{\{p\}\}$$

$$\|x_1 + x_2\| = \|x_1\| \cup \|x_2\|$$

$$\|x_1 \cdot x_2\| = \{a_1 \cup a_2 \mid a_1 \in \|x_1\| \ a_2 \in \|x_2\|\}$$

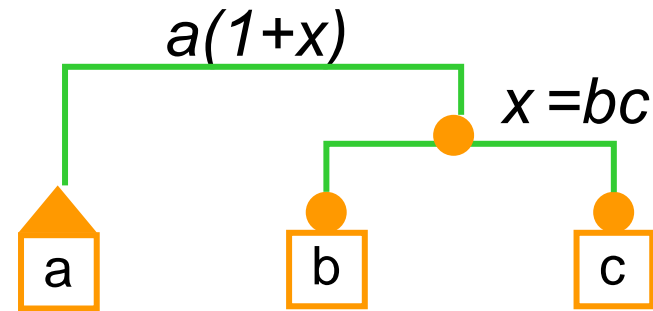
## Simple Connectors

- A **connector** is a set of ports which can be involved in an interaction
- Port attributes (**trigger** ▼, **synchron** ●) are used to model rendezvous and broadcast.
- An **interaction** of a connector is a set of ports such that: either it contains some trigger or it is maximal.

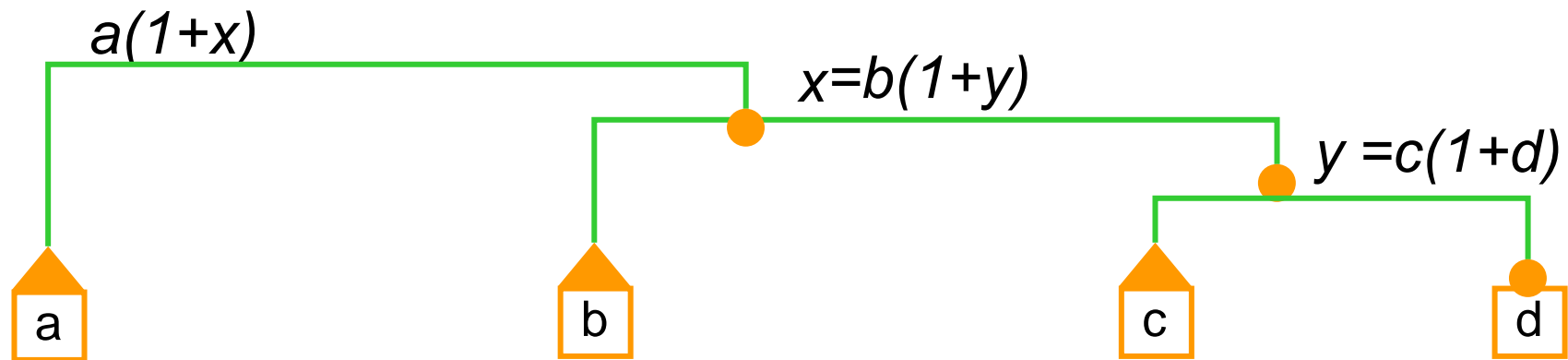


## Hierarchical Connectors

Atomic Broadcast:  
 $a+abc$



Causality chain:  $a+ab+abc+abcd$



# The Algebra of Connectors $AC(P)$

## Syntax:

$s ::= [0] \mid [1] \mid [p] \mid [x]$  (synchrons)

$t ::= [0]' \mid [1]' \mid [p]' \mid [x]'$  (triggers)

$x ::= s \mid t \mid x.x \mid x + x$

where  $P$  is a set of ports, such that  $0, 1 \notin P$

$+$	<i>union</i>	idempotent, associative, commutative, identity $[0]$
$\cdot$	<i>fusion</i>	idempotent, associative, commutative, identity $[1]$ , distributive wrt $+$ ( $[0]$ is not absorbing)
$[ ], [ ]'$	<i>typing</i>	unary operators

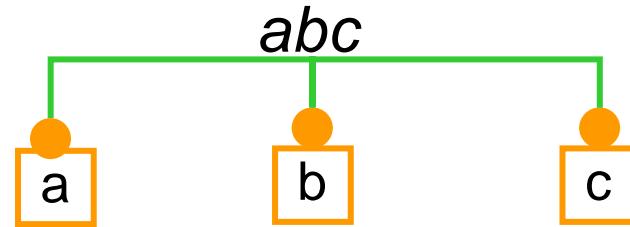
## Semantics:

The semantics of  $AC(P)$  is given by a function  $| \cdot | : AC(P) \rightarrow AI(P)$

# The Algebra of Connectors $AC(P)$ : Examples

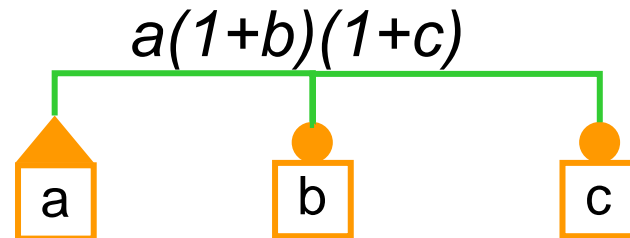
Rendezvous

$abc$



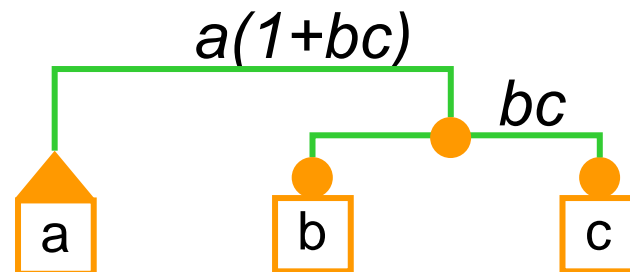
Broadcast

$a'bc$



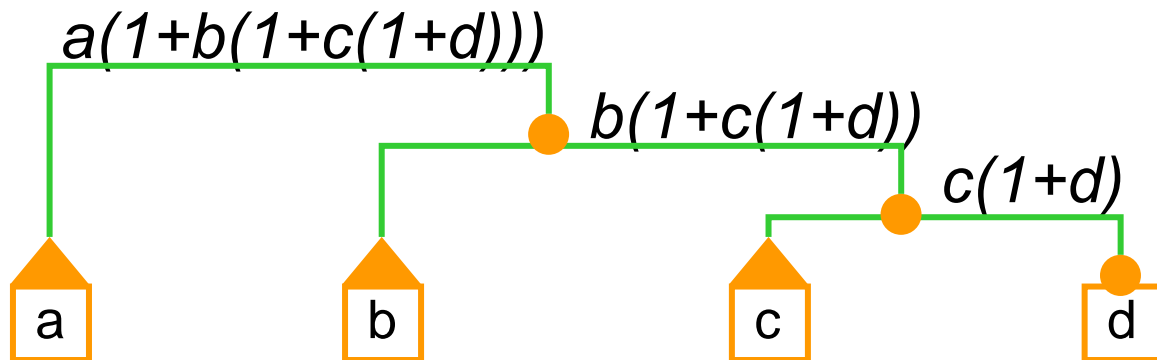
Atomic Broadcast

$a'[bc]$



Causality chain

$a'[b'[c'd]]$

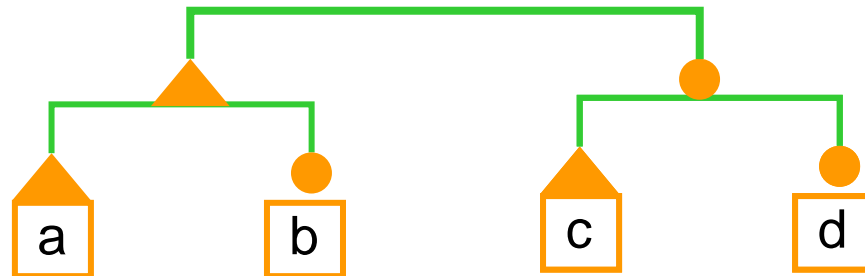


## The Algebra of Connectors: Fusion vs. Typing

For two connectors  $x=a'.b$  and  $y=c'.d$



$$xy=a'bc'd = a'bcd + abc'd = (a+b+ab)(1+c)(1+d)$$



$$[x]'[y]=[a'b]'[c'd] = a(1+b)(1+c(1+d))$$

## The Algebra of Connectors: Axioms for typing

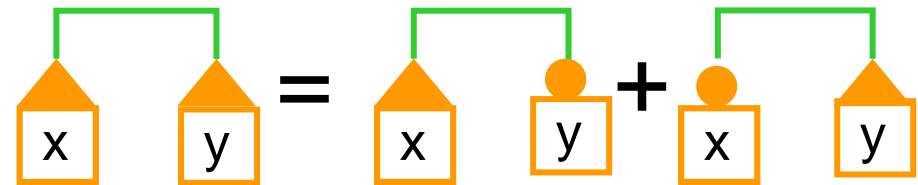
$$[0]' = [0]$$

$$[[x]^\alpha]^\beta = [x]^\beta$$



$$[x+y]^\alpha = [x]^\alpha + [y]^\alpha$$

$$[x]'[y]' = [x]'[y] + [x][y]'$$



*Fusion for typed connectors is not associative, e.g.*  
 $x[yz] \neq [xy]z$

## The Algebra of Connectors: Equivalence vs. Congruence

$x \sim y$  if  $|x| = |y|$  i.e. they represent the same set of interactions

- The axiomatization of AC(P) is semantically sound, i.e.

$$x=y \Rightarrow x \sim y$$

- $\sim$  is not a congruence (not preserved by fusion)

$$a'b \sim a+ab \text{ but } a'bc \sim a+ab+ac+abc \not\sim ac+abc$$

$\approx$  is the largest congruence contained in  $\sim$

- $x \sim y \Rightarrow [x]^\alpha \approx [y]^\alpha$
- Results for inferring congruence from equivalence
- Causal semantics not reducing triggers to rendezvous - the equivalence is a congruence

## The Algebra of Connectors: Boolean representation

$\beta: AC(P) \rightarrow B(P)$  where  $B(P)$  the boolean calculus on  $P$

For  $P = \{p, q, r, s, t\}$

$$\beta(pq) = p \wedge q \wedge \neg r \wedge \neg s \wedge \neg t$$

$$\beta(p'qr) = p \wedge \neg s \wedge \neg t$$

$$\beta(p+q) = (p \wedge \neg q \vee \neg p \wedge q) \wedge \neg r \wedge \neg s \wedge \neg t$$


$$\beta(0) = \text{false}$$

$$\beta(1) = \neg p \wedge \neg q \wedge \neg r \wedge \neg s \wedge \neg t$$

$$\beta(1+p'q'r's't') = \text{true}$$

Boolean representation depends on the set of ports  $P$ , in particular the expression of *fusion* and *typing* in terms of boolean operations .

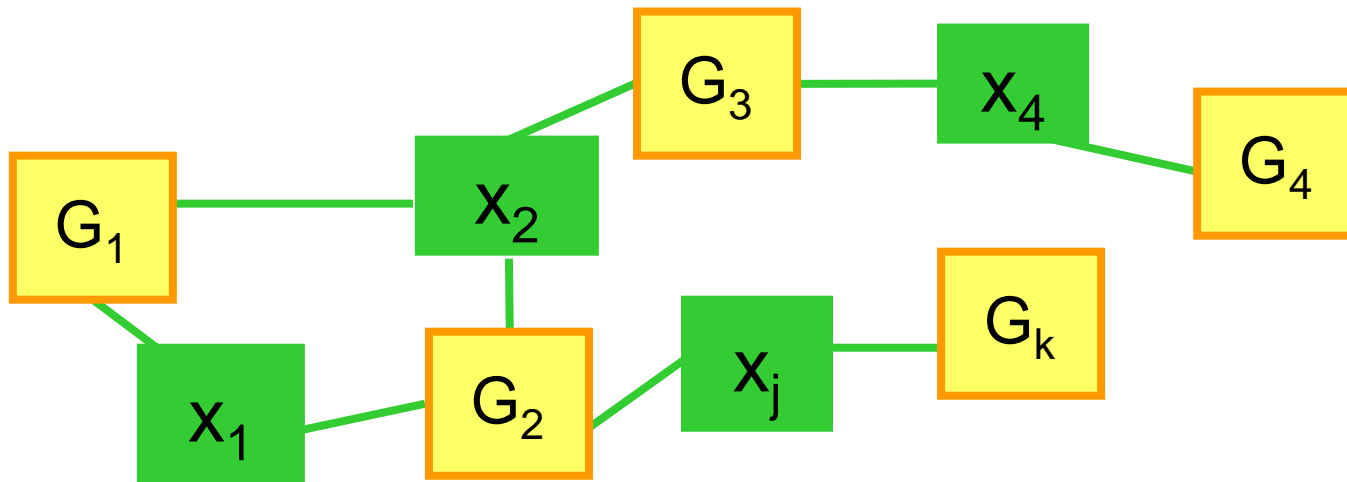
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## One-shot vs. Multi-shot Semantics

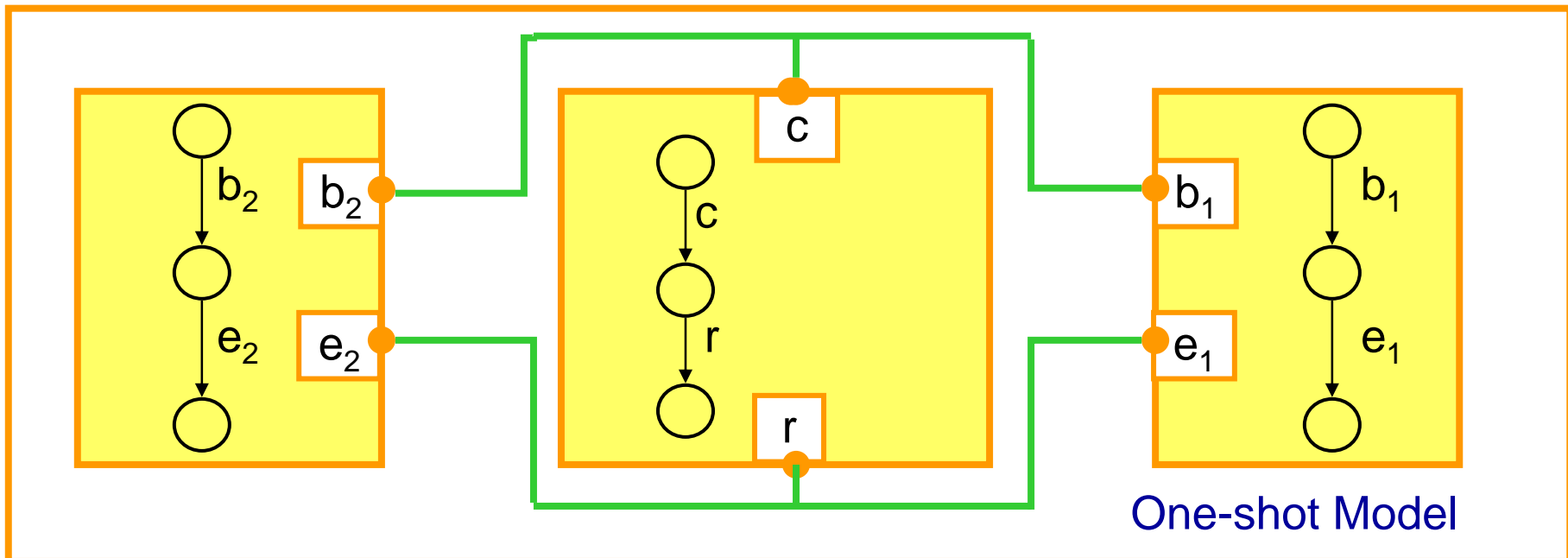
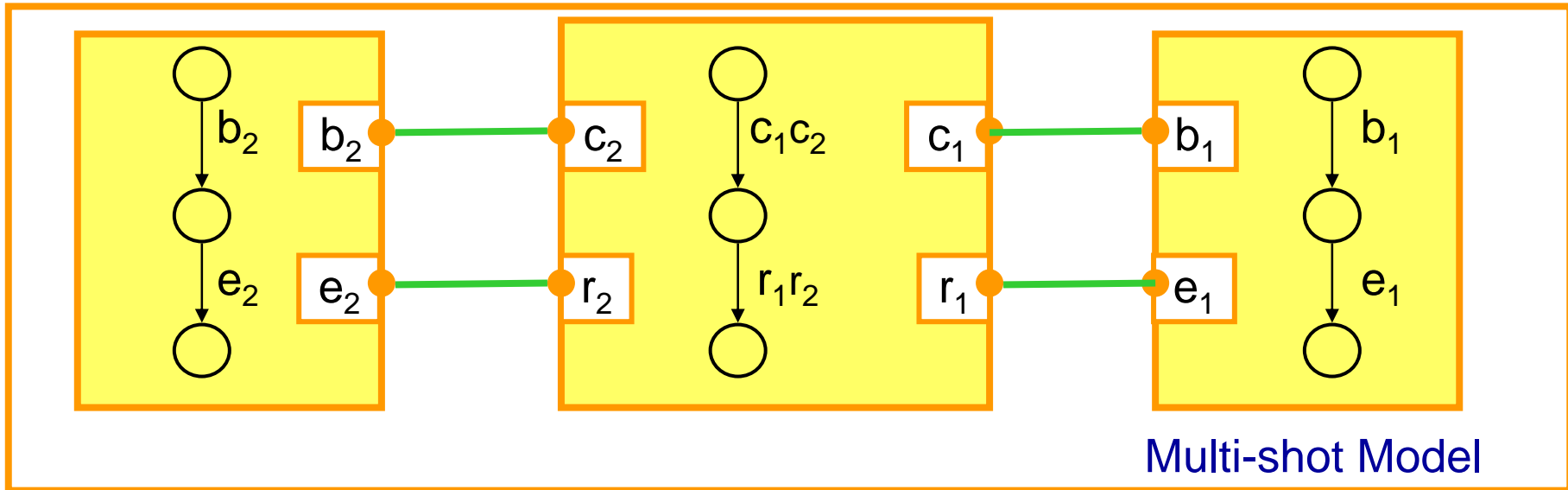
**Interactions**

$$\frac{a \in \gamma \wedge \forall i \in [1, n] q_i - a \cap P_j \rightarrow_i q'_i}{(q_1, \dots, q_n) - a \rightarrow_\gamma (q'_1, \dots, q'_n) \text{ where } q'_i = q_i \text{ if } i \notin I}$$

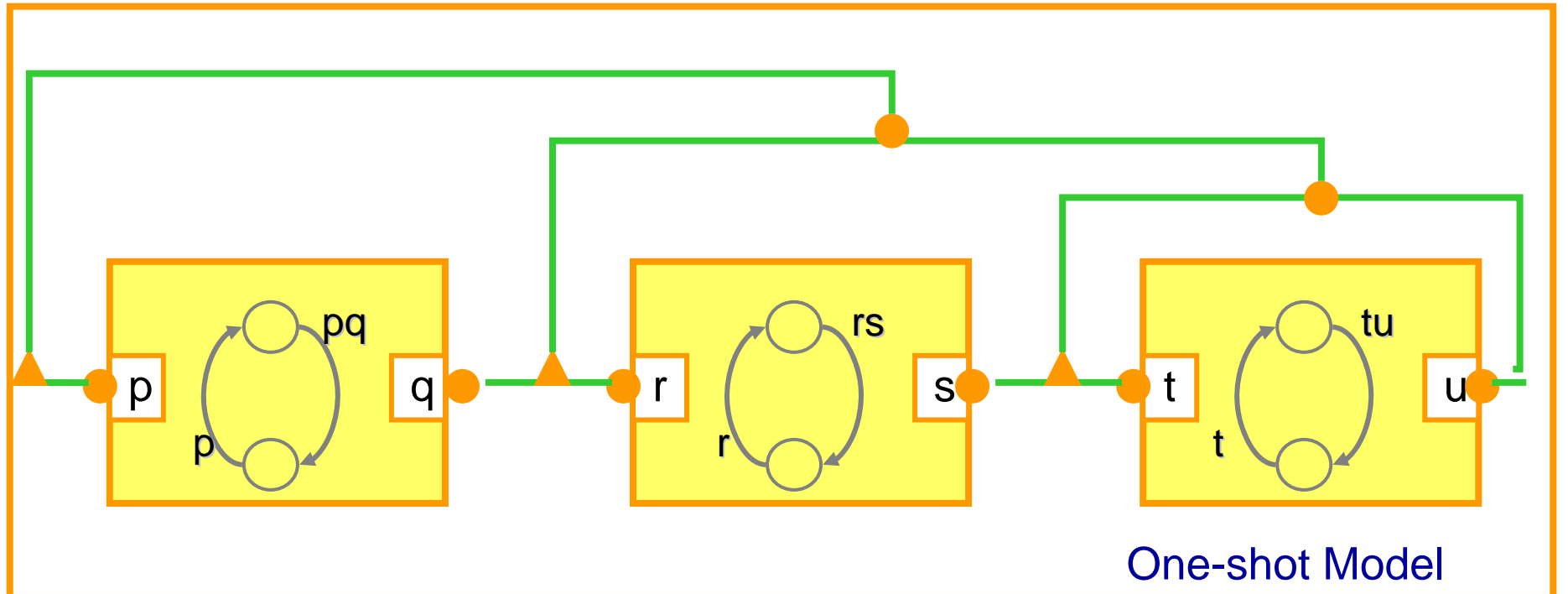
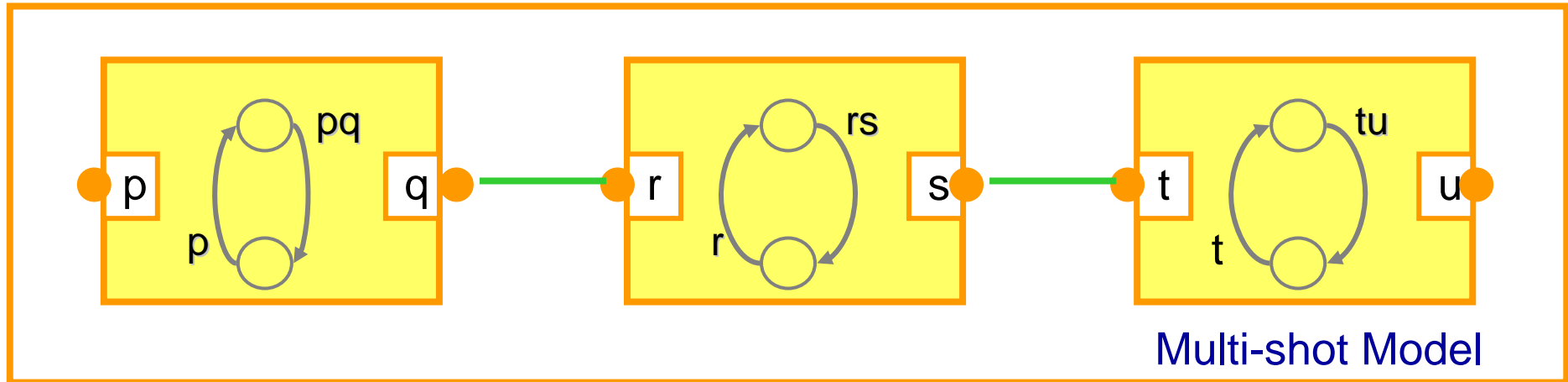


- A set of components  $I$  offering interactions  $G_i$  for  $i \in I$
- A set of connectors  $X_j$  for  $j \in J$
- one-shot:  $\gamma = \prod_{i \in I} G_i' \cap \sum_{j \in J} X_j$       multi-shot:  $\gamma = \prod_{i \in I} G_i' \cap \prod_{j \in J} X_j'$

# One-shot vs. Multi-shot Semantics: Joint Function Call



# One-shot vs. Multi-shot Semantics: mod8 Counter

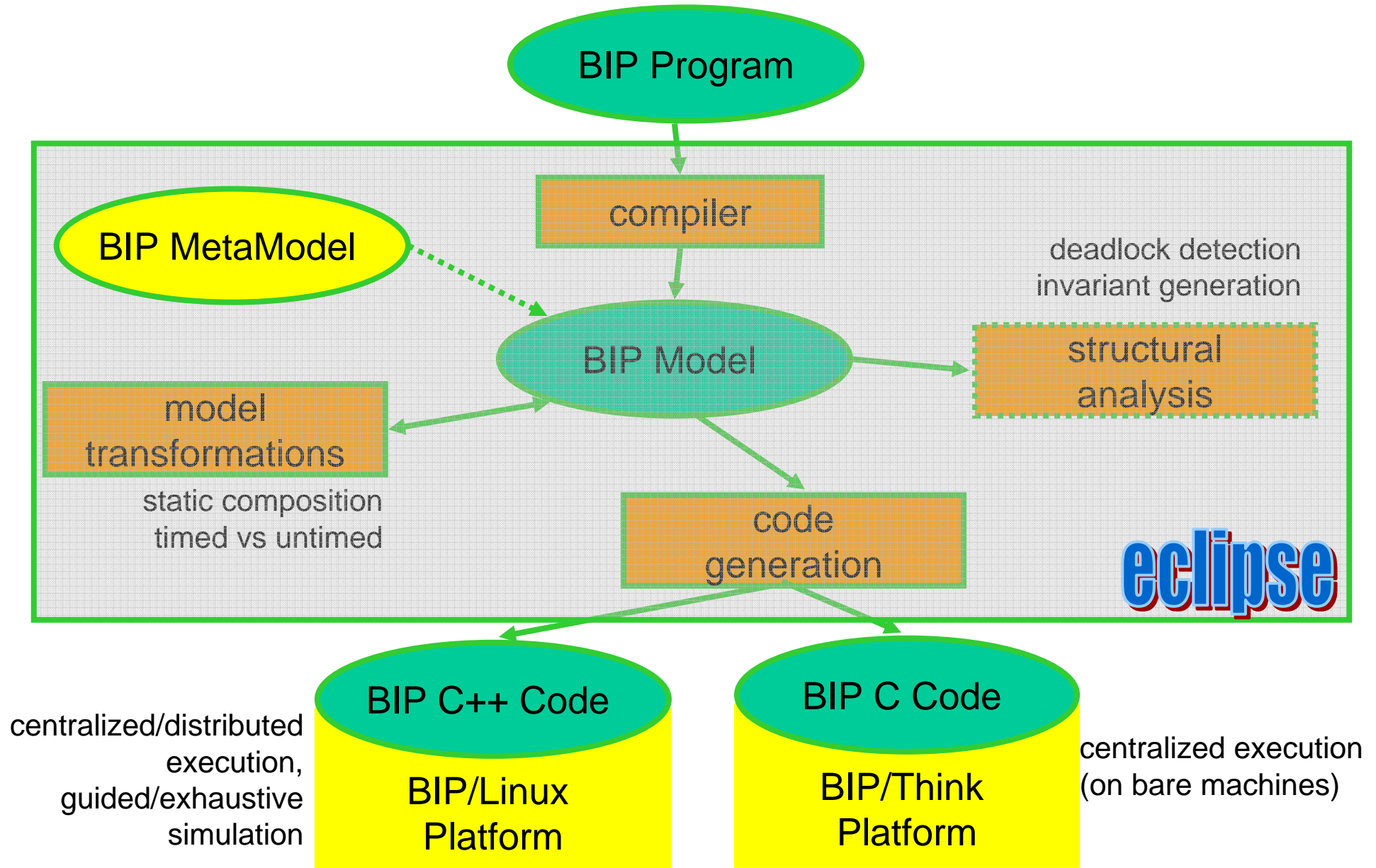


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# Discussion : Implementation



## Discussion: the Algebra of Conectors

- Allows compact and structured description of interactions as the structured composition of rendezvous and broadcast by using two operators : typing and fusion.
- Clear separation between behavior and interaction – NOT a process algebra!!
- Framework for studying composability in heterogeneous systems
- Boolean representation allows powerful manipulation, implementation and synthesis - Application for efficient execution of BIP