

Reconfigurable Distributed Control (Time Delays Disturbances)

Dr. Héctor Benítez Pérez
IIMAS UNAM



Objectives

- To model time delays in order to integrate this representation into control law design.
- To study the computer network behaviour in terms of processes management and scheduling policies.
- To study external factors such as fault diagnosis for time delay modelling.
- To design Control law strategies that accomplish external factors like those mention before.

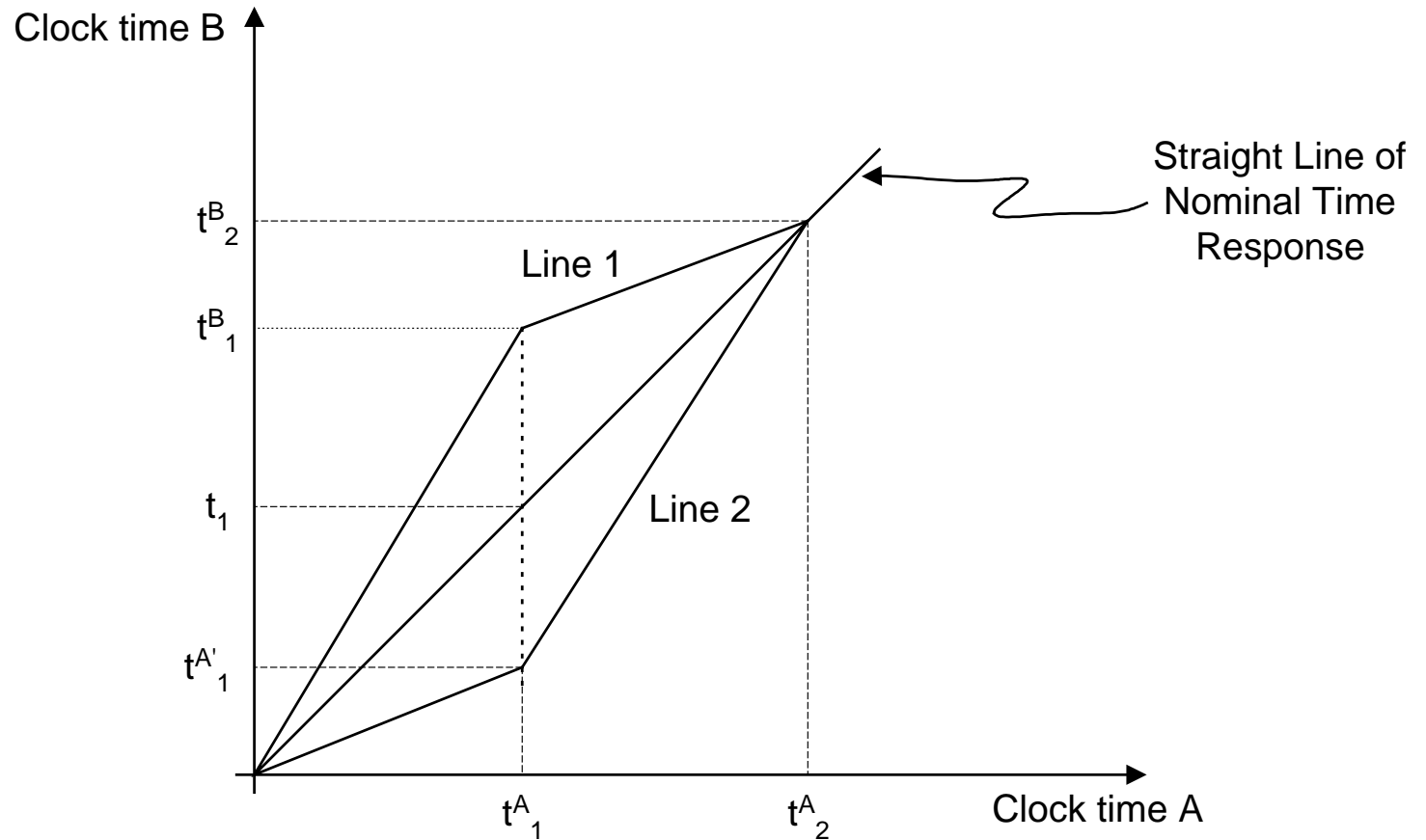


Previous Work

- The study of time delays has been widely spread from fault tolerance areas, computer network modelling, distributed systems design, control laws designs and others.
- Several implementations have been performed in order to understand the behaviour of processes.
- Different approaches have been followed like time graphs as shown next.

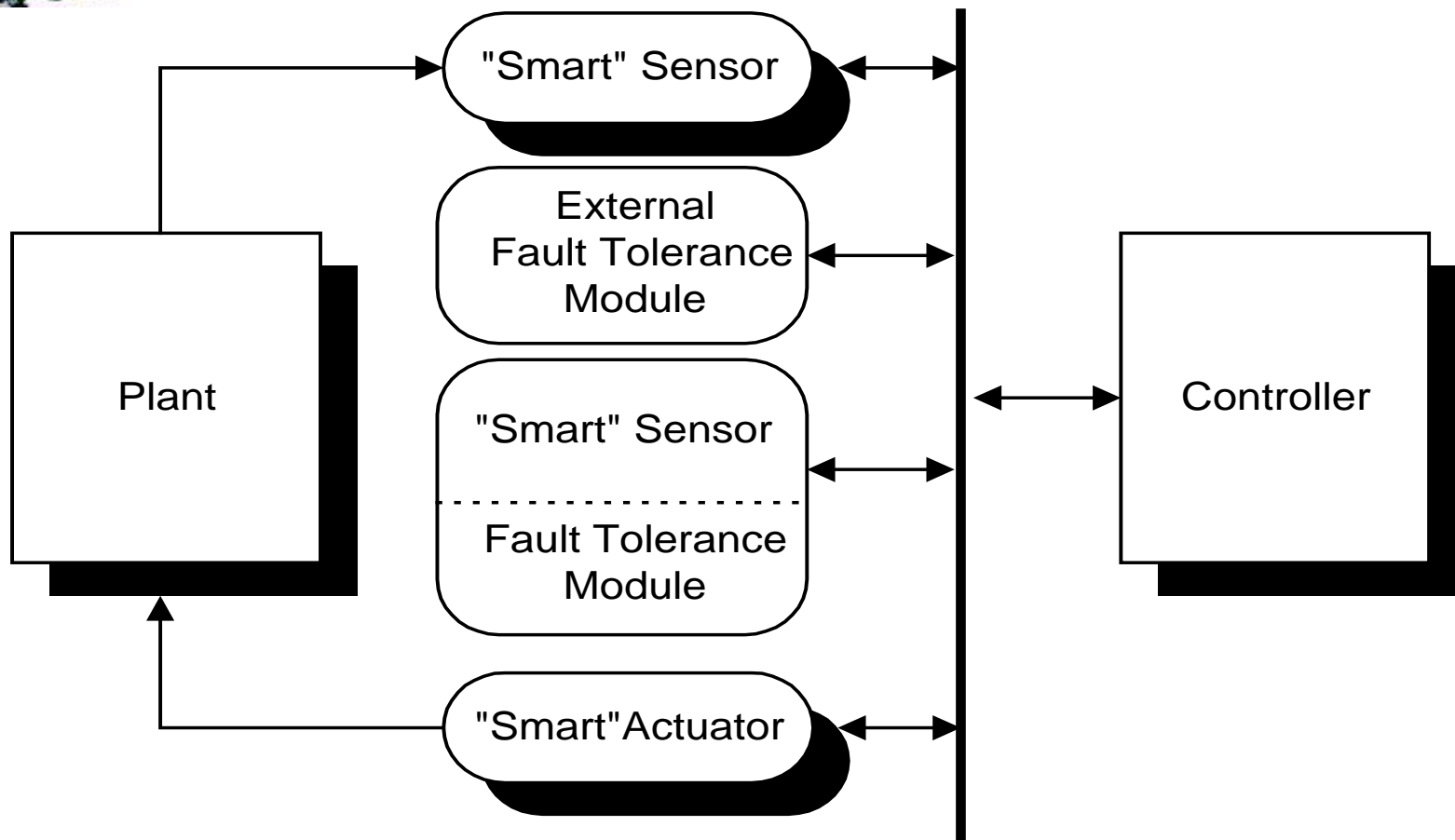


Clock Management



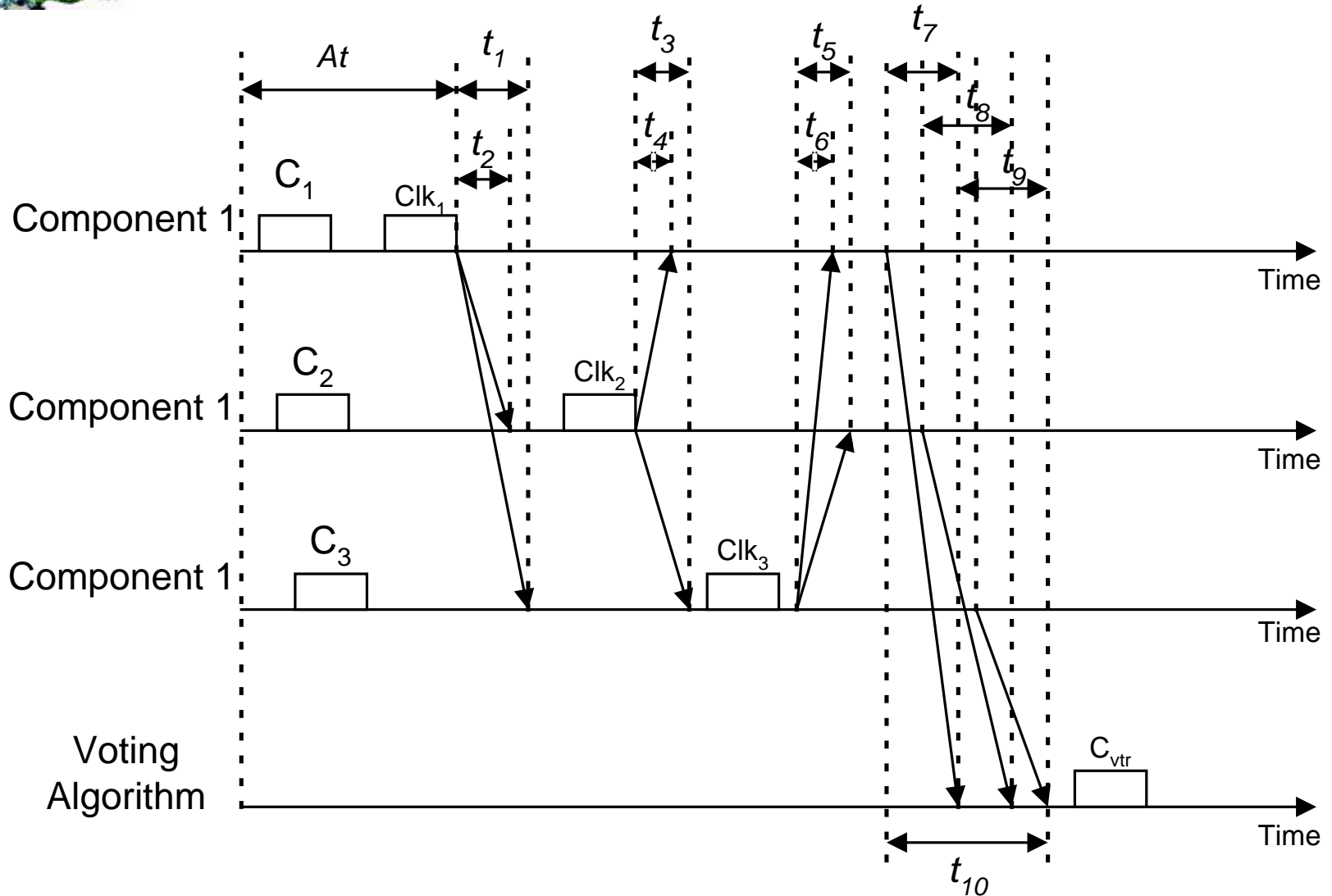


Basic Configuration





Time Diagram considering Clock Synchronization and Voting Algorithm

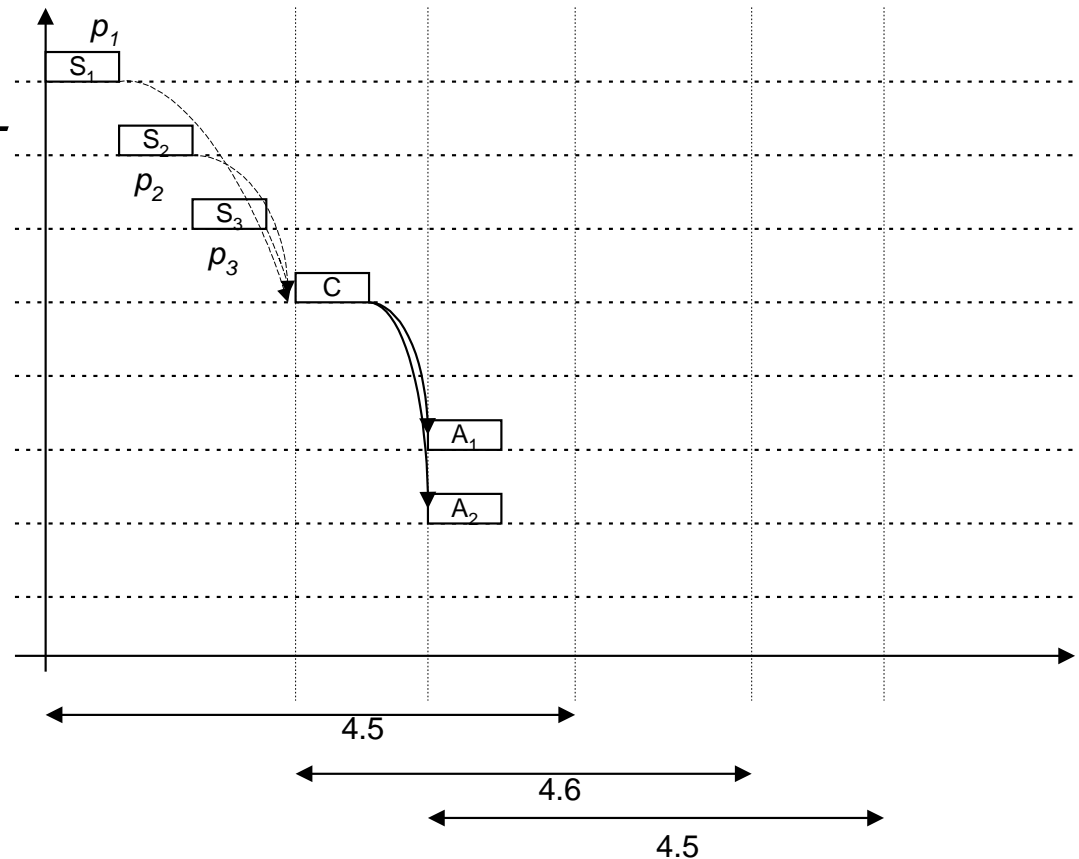




Time Delays in the Dynamics of the Processes

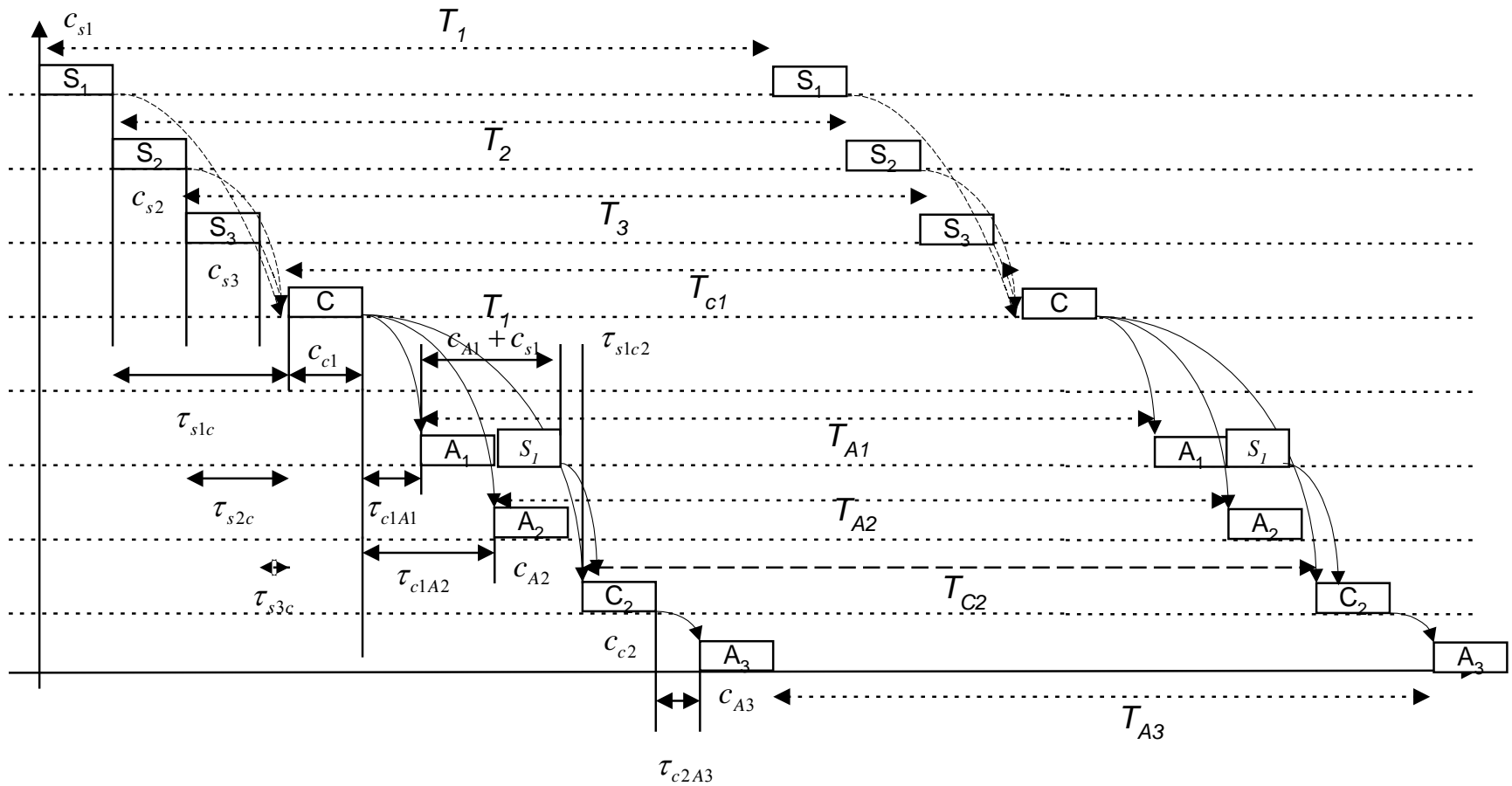
$$x(k+1) = Ax(k) + \sum_{i=0}^l B_i^k u(k-i)$$

$$B_i^k = \int_{t_i^k}^{t_{i-1}^k} \exp(A(T-\tau)) B d\tau$$





Time Delays Definitions Considering Dynamic Processes





Time Delays Definition

| Elements | Consumption Time | Period (ms) | Communication Time Delay |
|-------------------------------|-------------------|-------------|---|
| S ₁ | c_{s1} | T_1 | τ_{s1c} |
| S ₂ | c_{s2} | T_2 | τ_{s2c} |
| S ₃ | c_{s3} | T_3 | τ_{s3c} |
| C ₁ | c_{c1} | T_{c1} | $\tau_{c1A1}, \tau_{c1A2}, \tau_{c1s1}$ |
| A ₁ S ₁ | $c_{A1} + c_{s1}$ | T_{A1} | τ_{s1c2} |
| A ₂ | c_{s1} | T_{A2} | |
| C ₂ | c_{c2} | T_{c2} | τ_{c2A3} |
| A ₃ | c_{A3} | T_{A3} | |



Fuzzy Approximation

R_j : if $x_1(k)$ is A_{j1} and x_2 is B_{j2} then $x(k+1) = A_j x(k) + B_j u(k) + \Delta B_j u(k)$

$$v_j(k) = \prod_{i=1}^n w_{ji}(k)$$

$$w_{ji} = A_{ij}(x_i(k))$$

$$x(k+1) = \frac{\sum_{j=1}^N v_j(k) (A_j x(k) + B_j u(k) + \Delta B_j u(k))}{\sum_{i=1}^N v_i(k)}$$



Stability approach for TSK

$$\Delta B^p = \sum_{i=1}^N \rho_i \Delta B_i \sum_{j=1}^M \int_{\tau_j^i}^{\tau_{j-1}^i} e^{-a^p(t-\tau)} d\tau$$

$$V(x(k)) = x(k)^T p x(k)$$

$$A^T P A + B^T P B - 2P + \Delta B^T P \Delta B < 0$$

$$\Delta V(x(k)) = v(x(k+1)) - v(x(k)) < 0$$



Where the controllers are local implementations as shown in last equation

The plant is expressed as

$$\dot{\mathbf{x}}_p^j = \mathbf{A}_p^j \mathbf{x}_p^j(\mathbf{k}) + \mathbf{B}_p^j \mathbf{x}(\mathbf{k}) u_p^j(\mathbf{k}) + \Delta \mathbf{B}_p^j \mathbf{e}(\mathbf{k})$$

$$\mathbf{y}_p^j = \mathbf{C}_p^j \mathbf{x}_p^j(\mathbf{k})$$

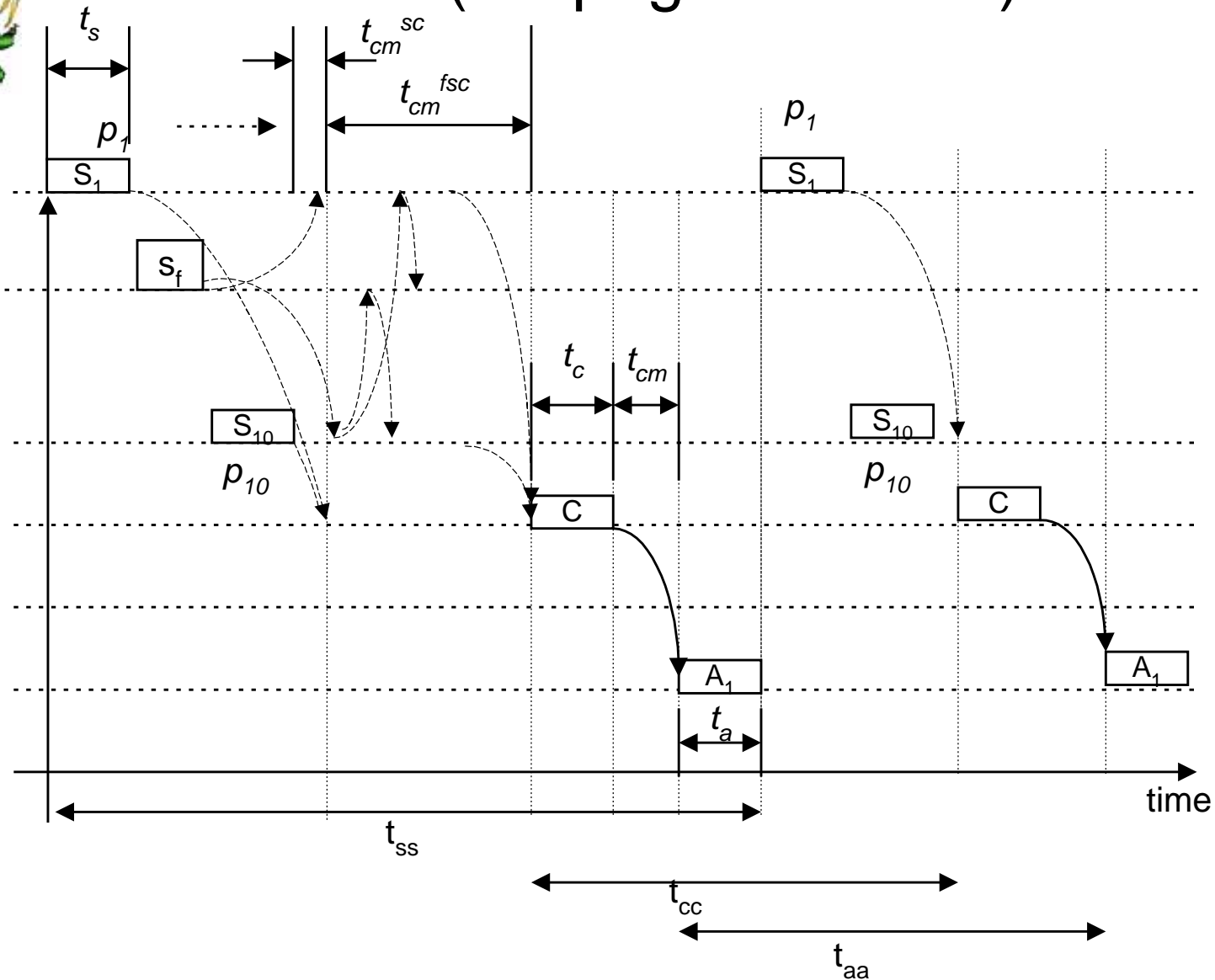
And the controller as:

$$\dot{\mathbf{x}}_c^j = \mathbf{A}_c^j \mathbf{x}_c^j(\mathbf{k}) + \mathbf{B}_c^j \mathbf{x} u_c^j(\mathbf{k})$$

$$\mathbf{y}_c^j = \mathbf{C}_c^j \mathbf{x}_c^j(\mathbf{k} - \tau_c^j) + \mathbf{D}_c^j u(\mathbf{k} - \tau_c^j)$$



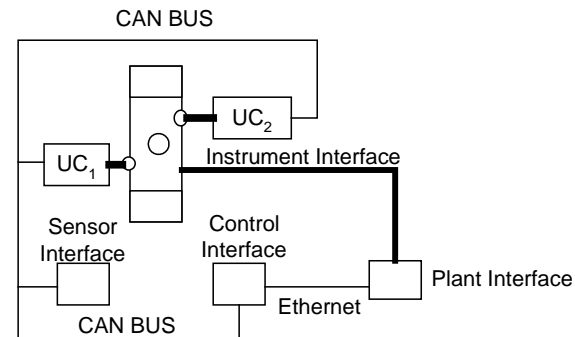
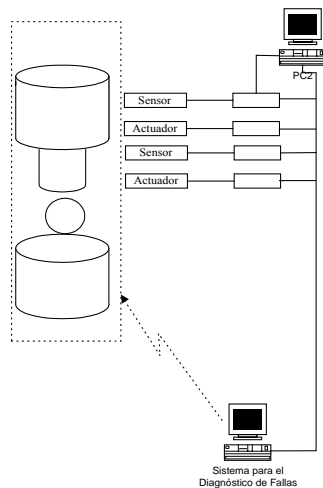
Case Study (Propagation Fault)





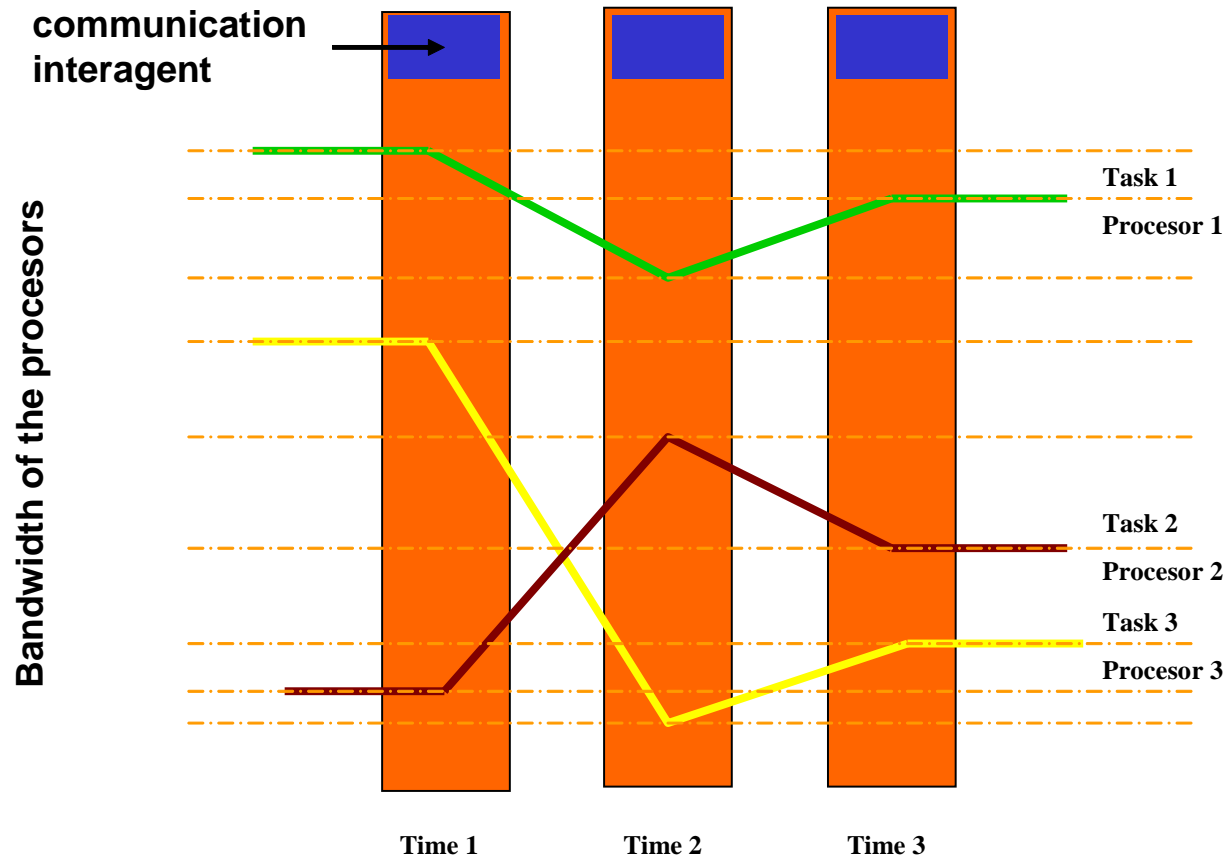
Magnetic Levitation System

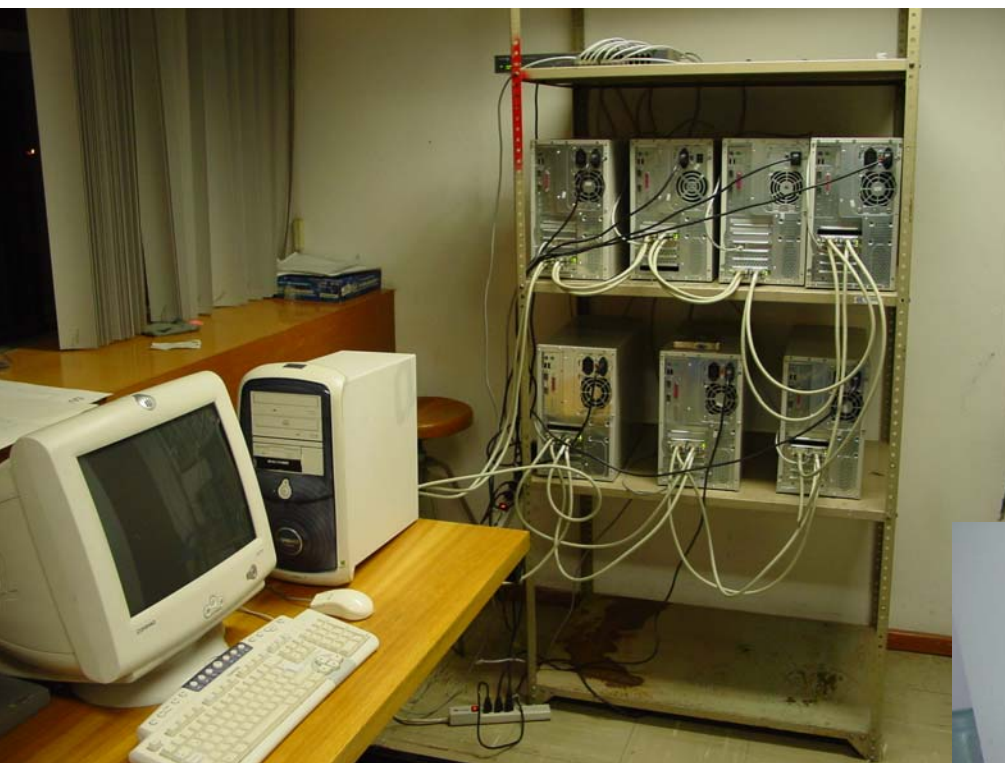
- Magnetic Levitator
 - Cooperative Agents by using FTT
 - Fuzzy control as TKS





Process Management





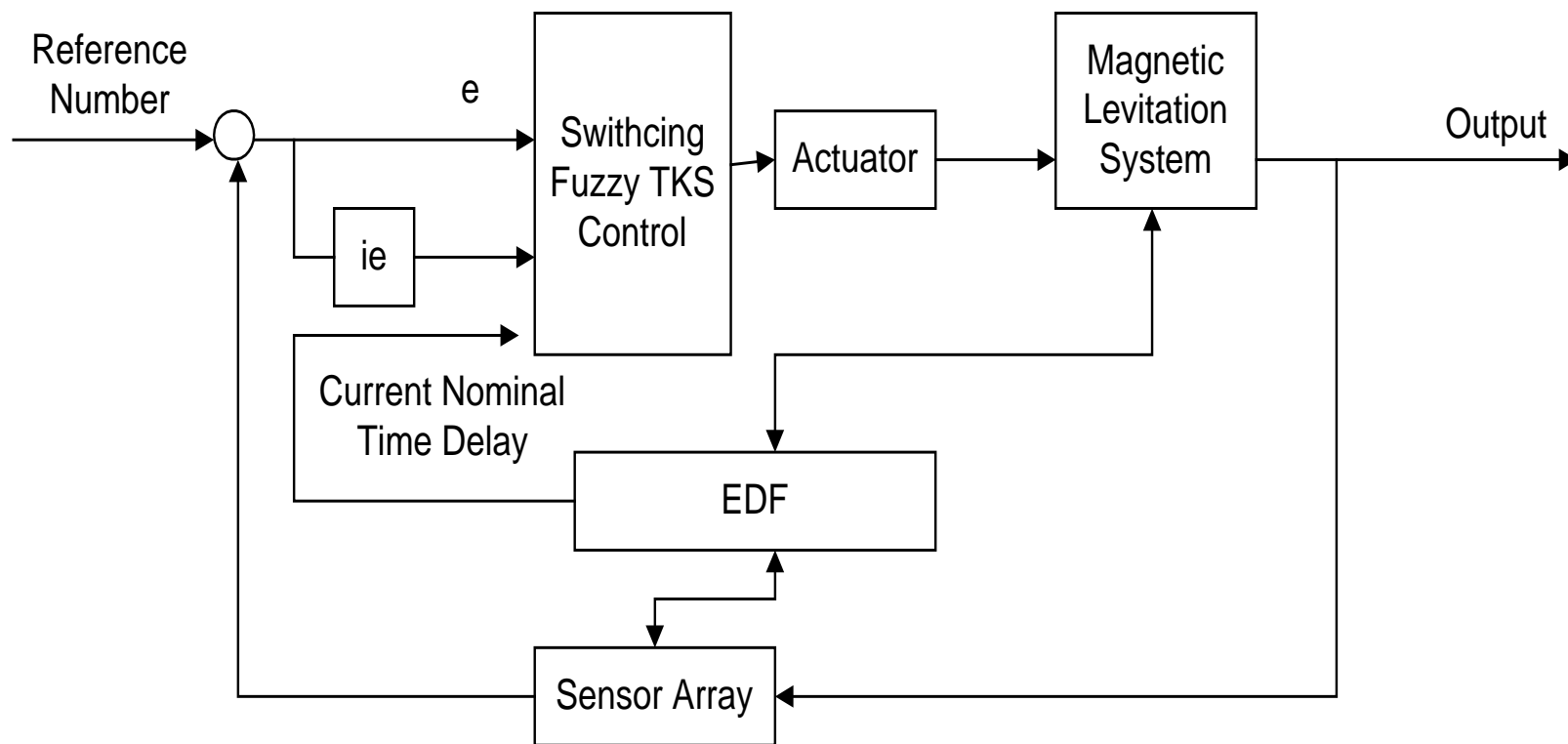


Process Management

- Scheduling of Distributed Processes using Neural Networks
- Scheduling of Processes based upon worst case scenario.
- Optimization of processes management on-line by using Genetic Algorithms



Current Approach





Conclusions

- Time Delays can be modelled in terms of stochastic procedure where switching control model becomes a feasible strategy to accomplish stability.
- Other strategies like time delays modelling are available but become difficult to implement due to the complexity of the source of these time delays. In this case a computer network system.
- Control law modelling can be approximated as a robust approximation but mainly in a hybrid manner.



Process Management (Future Work)

- Real-Time Modelling of Distributed Scheduling
- Metric Characterizations like Load Distribution, Timming Analysis and others.
- Dynamic Load Balancing
- Dynamic Process Migration
- Congestion Control
- Cooperative Control



Future Work

- To study the source of time delays in terms of Differential Equations, from the point of view of processes management.
- To implement TSK Control strategy based upon Helicopter case study.