

# Extending the Path Analysis Technique to Obtain a Soft WCET

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# Overview

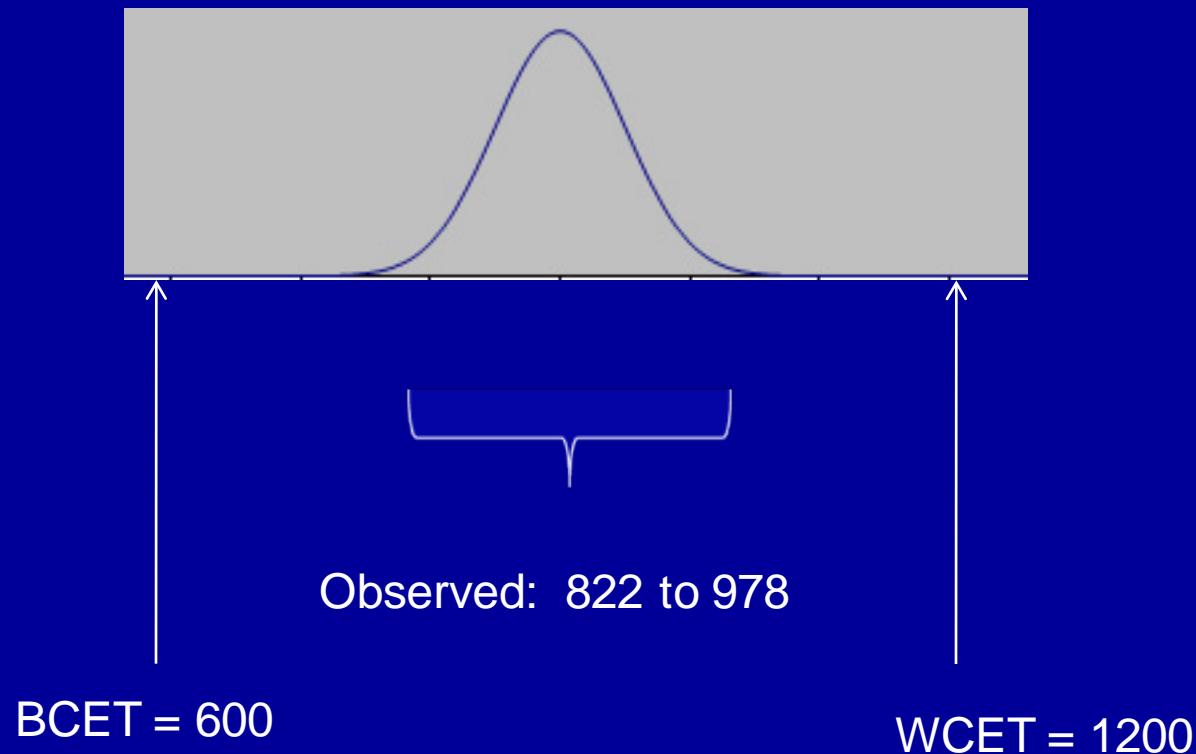
- **Hard** versus **soft** WCET
- Incorporating soft WCET in loop analysis algorithm
- Study of benchmarks
- Comparison of static timing analysis
- Ongoing & future work
- Conclusions

# Motivation

- Need to bound WCET of tasks.
  - Static timing analysis tools
- Can we tolerate an occasional missed deadline?
  - Hard RT system: **NO**. WCET is absolute
  - Soft RT system: **YES**. A WCET estimate that almost always bounds the actual WCET is acceptable.
- Traditional WCET analysis has been for hard RT
  - Estimates can be quite **loose** due to input data

# For example ...

- Consider a simple distribution of possible execution times, compared to “hard” WCET



# Goal

- We want to provide a tighter WCET bound, which may underestimate the actual execution time in rare cases ( $< 1\%$ ).
- Extend earlier work in timing analysis
  - Statically determine the **distribution** of execution times.
- Need to also update hardware simulator so it also produces time distributions: interesting case studies.

# Loop analysis

- In our “path analysis” approach, we do the analysis bottom up. Instruction → path → loop → function → task.
  - The loop’s execution time distribution depends on its paths.
  - Multiple paths result from conditional control flow.
  - Choice of path typically depends on input data, unknown at compile time.
  - 1 path : trivial
  - 2 paths : we use binomial probability technique
  - 3+ paths : repeated application of (2)

# 2 path case

Let A = longer path and B = shorter path

compute  $A_{\text{time}}$  and  $B_{\text{time}}$  as well as  $A_{\text{prob}}$  and  $B_{\text{prob}}$

total\_prob = 0.0

for i = 0 to n

p = probability that A is taken on i of the n iterations and  
B is taken on (n - i) iterations

for j = 100\*total\_prob to 100\*(total\_prob + p)

time\_dist[ j ] =  $A_{\text{time}} * i + B_{\text{time}} * (n - i)$

total\_prob += p

# More paths?

- Consider case of 4 paths (A,B,C,D) with equal probability of being taken.
  - Use 2 case model to find time distributions  $TD_{A+B}$  and  $TD_{C+D}$ .
  - Concatenate the two TD's. Sort the values, and remove every other element (because they were the same size) to normalize size of the TD.
- What if  $(A+B)_{\text{prob}} > (C+D)_{\text{prob}}$  ?
  - Before you concatenate, stretch  $TD_{A+B}$  by a factor of  $(A+B)_{\text{prob}} / (C+D)_{\text{prob}}$



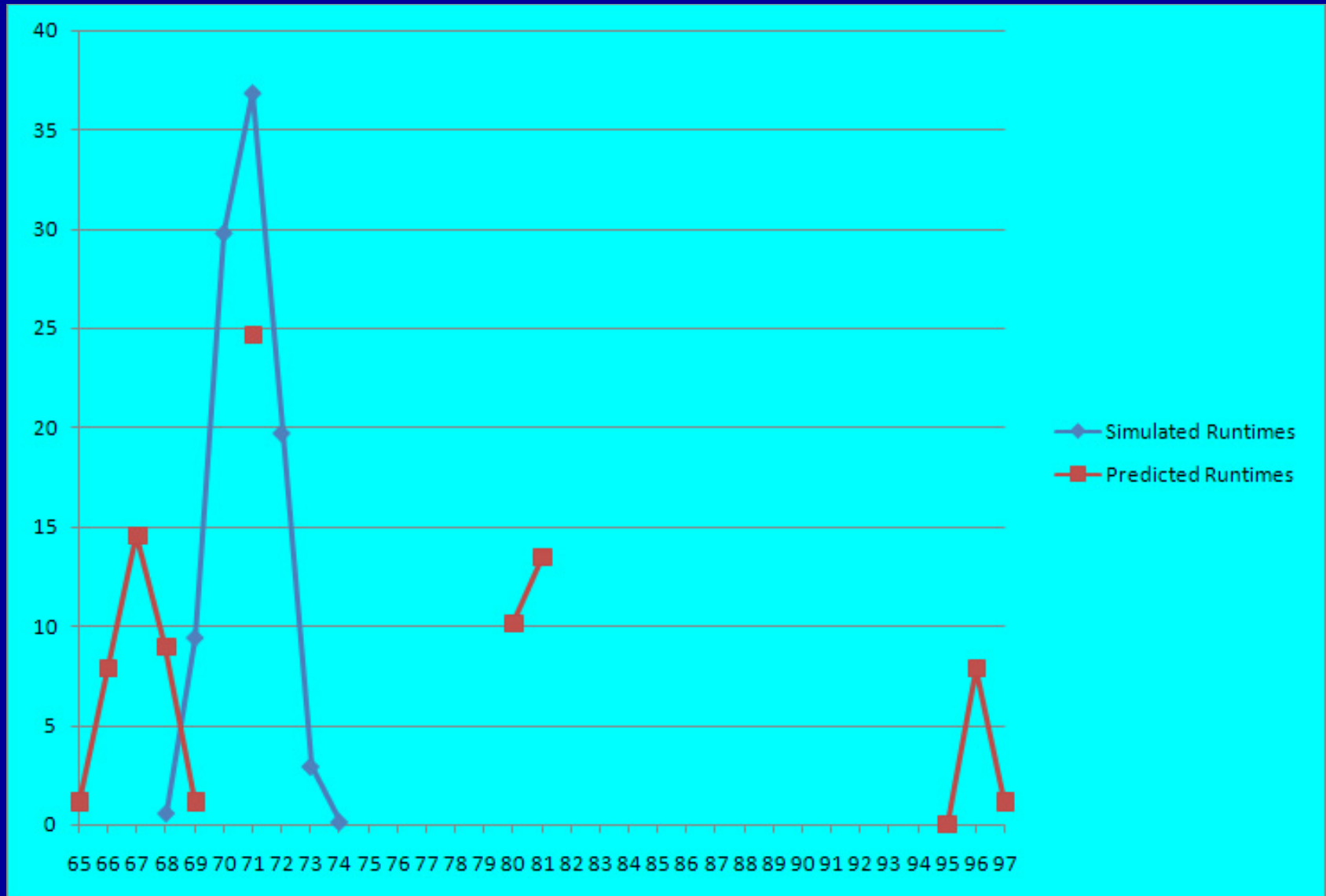
# Methodology

- Benchmark tasks with random input data
- Timing analyzer only needs to be run once, because it **ignores** the input data.
- Using hardware simulator
  - 1000 trials of benchmark program
  - Automatically generate next version of benchmark, compile and run.
  - Testing is easier for soft WCET than for hard WCET because we don't need to figure out the WC input data. 😊

# Simulated observations

- Each time we ran a randomized version of a benchmark, we computed: observed execution time / predicted WCET. (As a percent)
- We took note of:
  - Width of the observed distribution
  - Skewness
  - The **observed soft WCET**. In one case this was as low as 2%.
  - Different loops in the same function
  - **Effect of changing the distribution of input values.** (“fair” versus “unfair”)

# Result with 7 paths



# Ongoing & Future

- Combining multiple loops
  - More realistic estimate of probability of taking a branch
  - Open questions:
    - Consider other probability distributions?
    - How to measure “how close” static and dynamic distributions are?
- 
- GUI and Website [cs.furman.edu/~sparta](http://cs.furman.edu/~sparta)
  - Combine with work on parametric timing analysis to produce distribution of polynomial coefficients.

# Conclusion

- Extend our existing framework for bounding hard WCET to generate:
  - static prediction for **soft WCET**,
  - as well as entire execution time distribution.
- Incorporated into existing timing analyzer, giving rapid result for all loops in program.
- Scales well with  $\uparrow$  number of paths.
- Potential benefit for system developers if hard and soft WCET differ substantially.