

# Embedding Domain-Specific Modelling Languages into Maude Specifications

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# Outline

- 1 Introduction
- 2 Example
- 3 Results
- 4 Related Work

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# Domain Specific Modelling Languages (DSML)

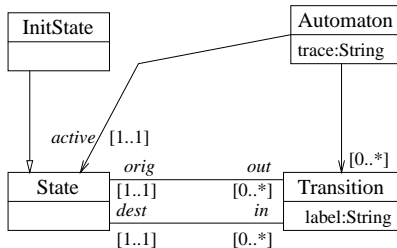
- What are they:
  - DSML are language for modelling specific domains
  - some DSML are *executable*
- Why are they needed:
  - the Unified Modelling Language (UML) is "too large"
  - people prefer smaller languages adapted to their *domain*
- How to define them:
  - based on *metamodels, models, and model transformations.*

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# Syntax of Finite Automata = Metamodel

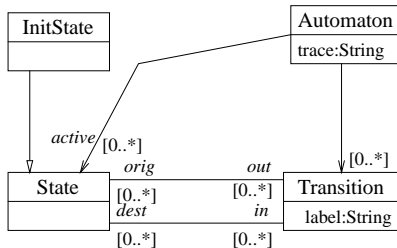
= UML Class Diagram + (optionally) OCL constraints



**Context State** :  $self.out \rightarrow \text{forAll}(t_1, t_2 | t_1 \neq t_2 \text{ implies } t_1.label \neq t_2.label)$   
**Context Transition** :  $self.label \neq ""$

# Syntax of Finite Automata = Metamodel

= UML Class Diagram + (optionally) OCL constraints



**Context** *Transition* : `self.dest.size() = 1`

**Context** *Automaton* : `self.active.size() = 1`

**Context** *Transition* : `self.orig.size() = 1`

**Context** *State* : `self.out → forAll( $t_1, t_2 | t_1 \neq t_2$  implies  $t_1.label \neq t_2.label$ )`

**Context** *Transition* : `self.label ≠ ""`

# Metamodel of Automata as Maude Specification

```
fth AUTOMATA-META-MODEL is
pr NAT .
pr STRING .

sorts Automaton State InitialState Transition .
subsort InitialState < State .

op trace : Automaton -> String . --- attributes
op label : Transition -> String .

op owned : Automaton -> Set{Transition} . --- associations
op orig : Transition -> Set{State} .
op dest : Transition -> Set{State} .
op incoming : State -> Set{Transition} .
op outgoing : State -> Set{Transition} .
op active : Automaton -> Set{State} .

eq card(active(X:Automaton)) = 1 -- "implicit" OCL invariant for cardinality ...
eq length(label(W:Transition)) > 0 = true --- "explicit" OCL invariant
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endfth
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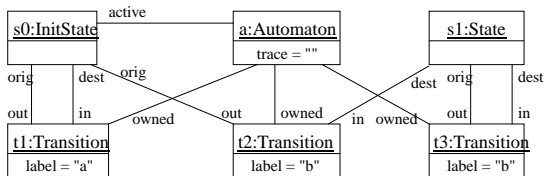
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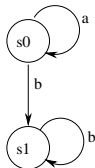
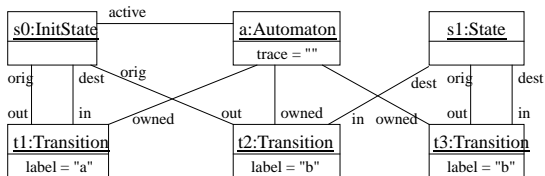
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= Object diagram of Class Diagram



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# Model of an Automaton as Maude Specification

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fmod AUTOMATON-MODEL is
...includes AUTOMATA-META-MODEL except equations for OCL invariants

op a : -> Automaton .
op s0 : -> InitialState .
op s1 : -> State .
ops t1 t2 t3 : -> Transition .

eq trace(a) = "" .
eq label(t1) = "a" .
eq label(t2) = "b" .
eq label(t3) = "b" .
eq owned(a) = t1, t2, t3 .
eq active(a) = s0 .
eq orig(t1) = s0 .
eq dest(t1) = s0 .
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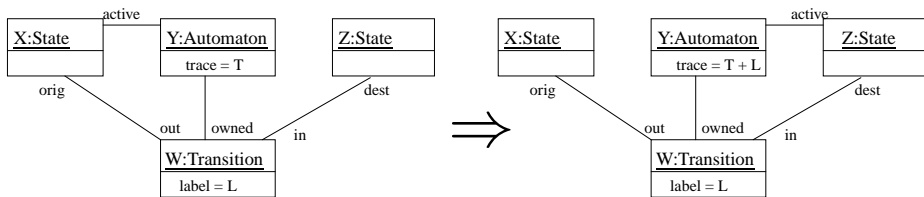
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# Operational Semantics = Model Transformation

## = Graph Rewriting



# Automata Semantics as Rewriting over Maude Specs

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rl
(eq 'active[Y] = X [none] .)
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search [1,10] upModule('AUTOMATON-MODEL,false) =>* M such that
getTrace(M) = '"aaabbb".String
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metamodel  $MM \rightsquigarrow$  Maude theory  $MM \rightsquigarrow \llbracket MM \rrbracket$ .

model  $M$  of  $MM \rightsquigarrow$  Maude module  $M_{MM} \rightsquigarrow \langle M_{MM} \rangle$ .

- *conformance*:  $\langle M_{MM} \rangle \in \llbracket MM \rrbracket$
- *operational semantics*: rec. function  $\llbracket MM \rrbracket \rightarrow \mathcal{P}(\llbracket MM \rrbracket)$

are *effectively decidable/computable* in Maude

Also in the paper: *semantics-preserving model transformations*.

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- Mova (Madrid): metamodels as *Maude specifications*
- Moment2 (Leicester) : metamodels as *Maude sorts*
- Maudeling (Málaga) : metamodels as *Full Maude specs.*

Other closely related approaches:

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