



Eidgenössische Technische Hochschule Zürich  
Swiss Federal Institute of Technology Zurich



Computer Engineering and  
Networks Laboratory

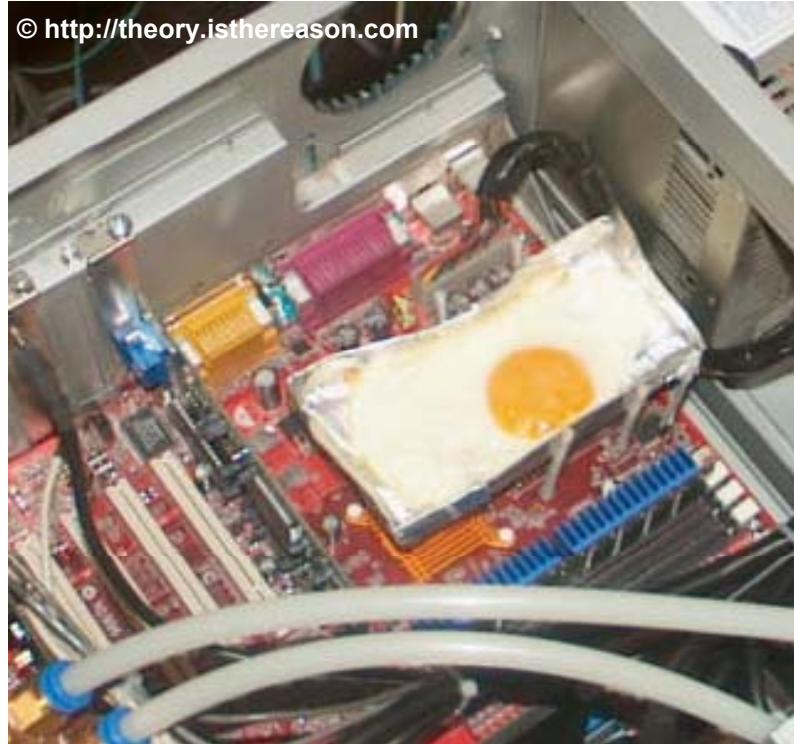
# Thermal-Aware Design of Real-Time Multi-Core Embedded Systems

Iuliana Bacivarov, Lars Schor,  
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ETH Zurich, Switzerland



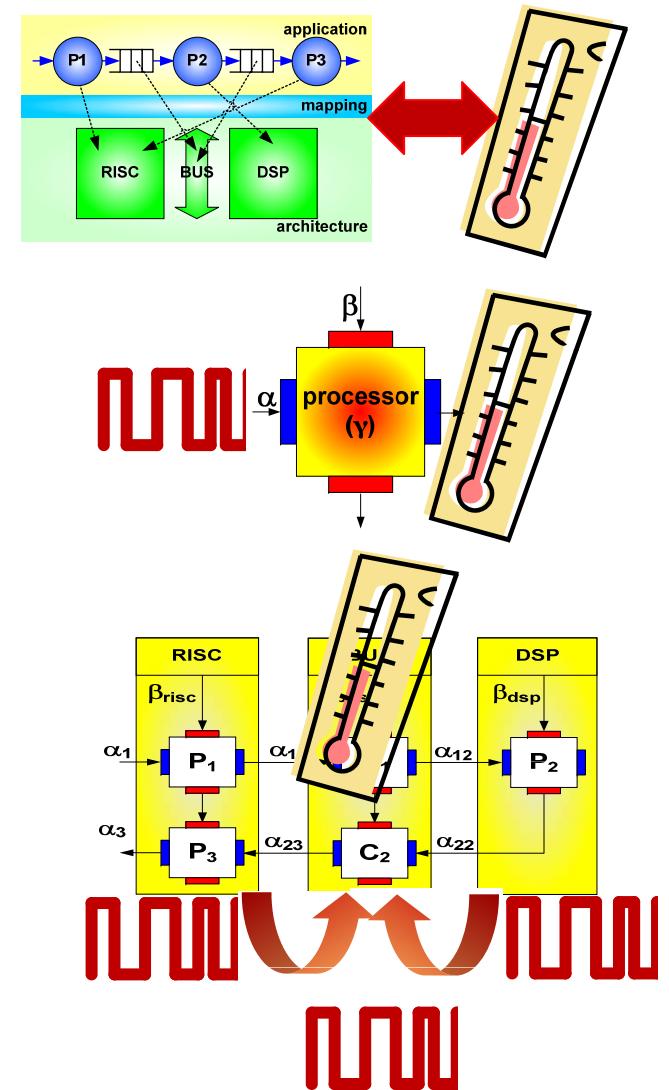
# How Hot Can It Get?



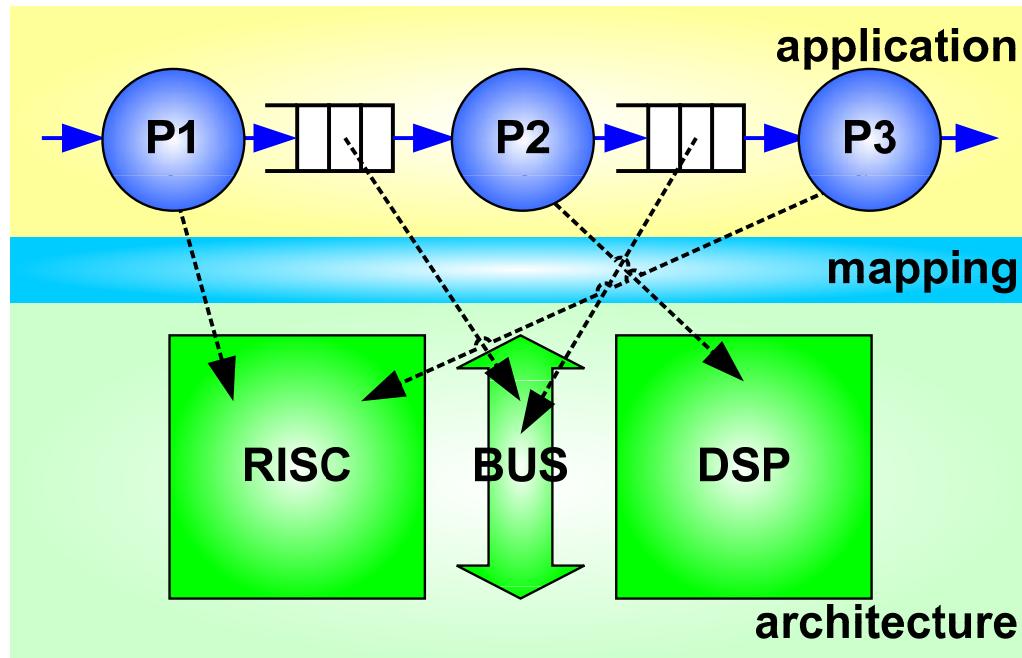
**CAN WE PREDICT WORST CASE  
(PEAK) TEMPERATURES OF AN  
EMBEDDED SYSTEM?**

# Outline

- **introduction**
  - system model
  - time, power, and temperature models
- **worst-case temperature analysis**
  - critical instance in terms of temperature
  - worst-case peak temperature
  - computational aspects
- **how about multi-cores?**
- **experiments & conclusions**

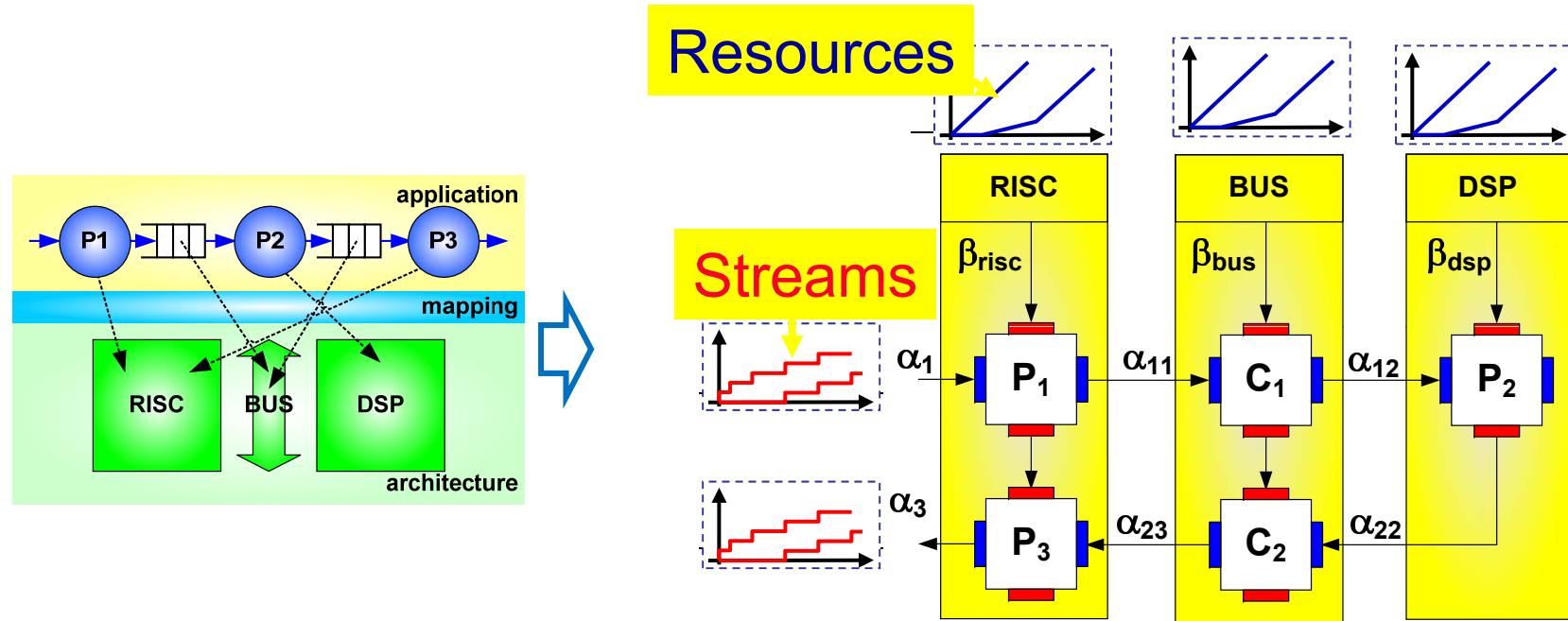


# System



- **embedded system specification**
  - process network – parallel applications
  - multi-core/3D architecture
  - mapping (binding, scheduling)

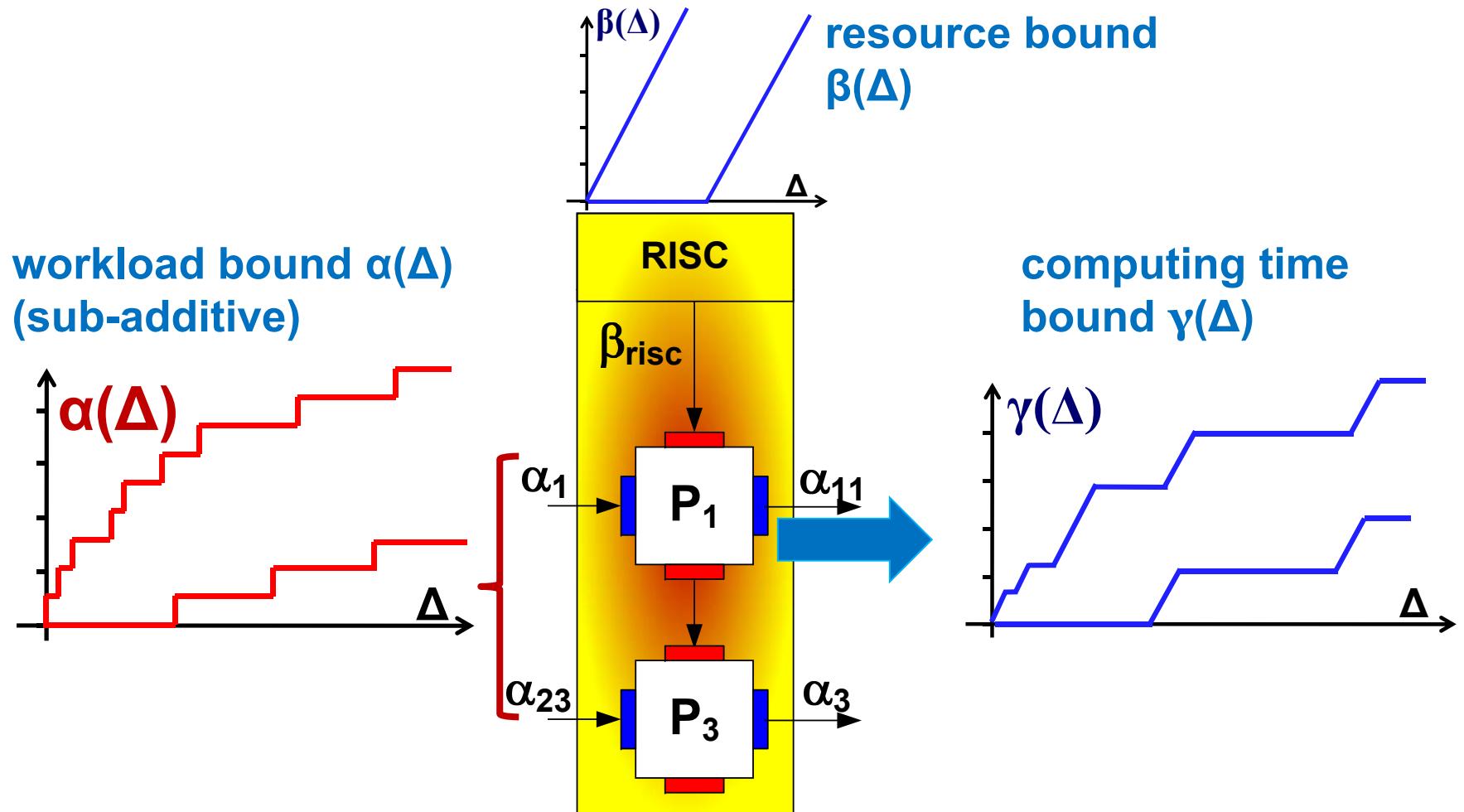
# System and Analysis Model



- real-time analysis via Modular Performance Analysis (MPA)\*
  - streams and resources represented by *arrival/service curves*
  - output: *worst-case bounds* on system timing properties

\*Modular Performance Analysis (MPA) <http://www.mpa.ethz.ch>

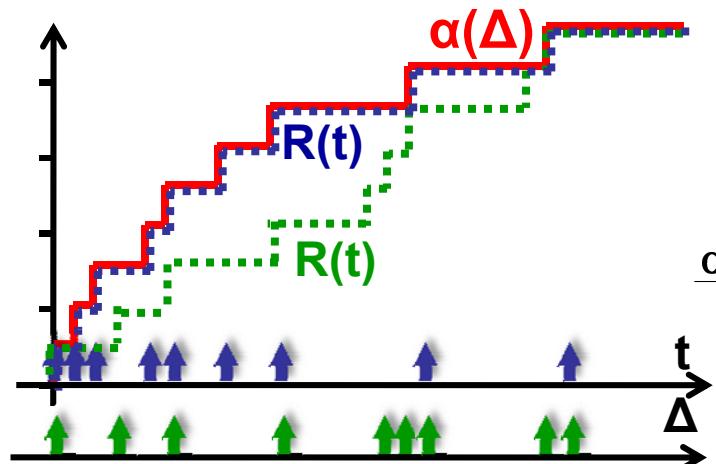
# MPA Component



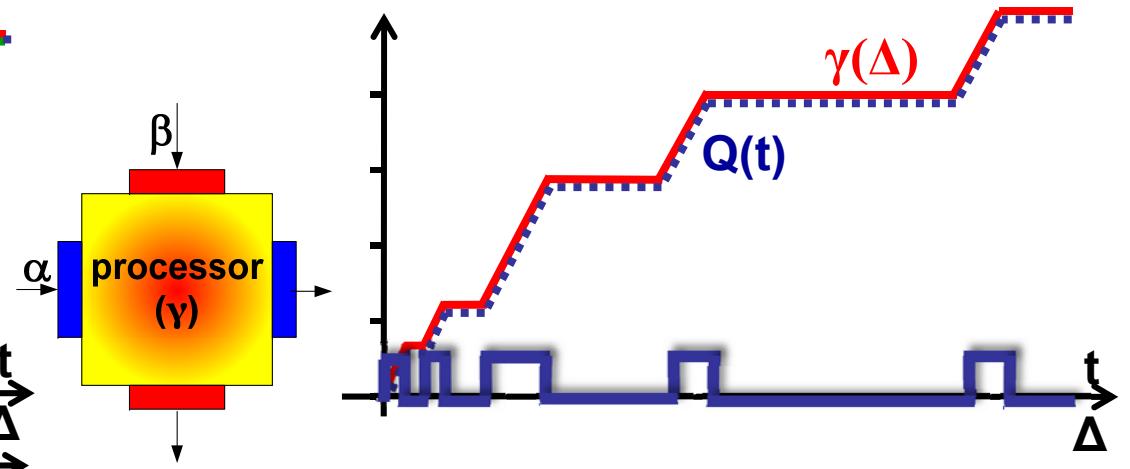
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# Workload/Computing Time Bounds

cumulative workload  
 $R(t)$  and bound  $\alpha(\Delta)$



accumulated computing  
time  $Q(t)$  and bound  $\gamma(\Delta)$

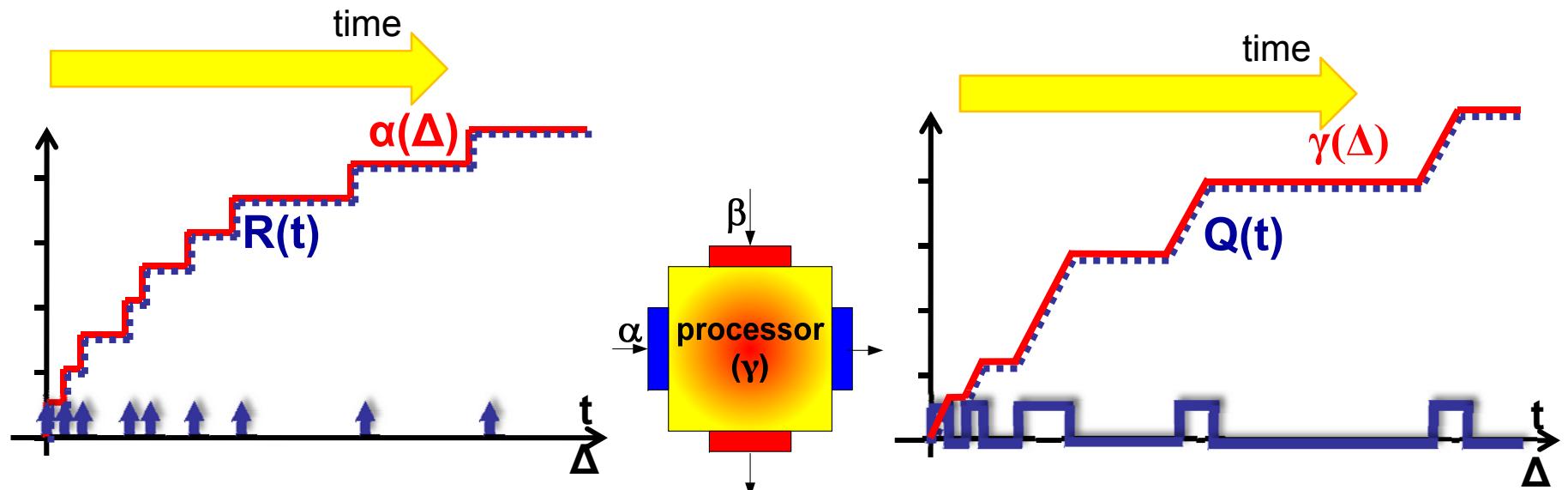


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# Workload/Computing Time Bounds

$\alpha(\Delta)$  corresponds to time-critical instance, leading to **worst-case execution time**

accumulated computing time  $Q(t)$  and bound  $\gamma(\Delta)$



\*Modular Performance Analysis (MPA) <http://www.mpa.ethz.ch>

# Power and Temperature Models

- **power model**

- **active** and **idle** task modes



$$P_a = \phi_a T + \psi_a \quad P_i = \phi_i T + \psi_i$$

temperature-dependent leakage

- **temperature model**

$$C \frac{dT}{dt} = P - G(T - T_{amb})$$

active/idle power  
params  $\phi_{a/i}, \psi_{a/i}$

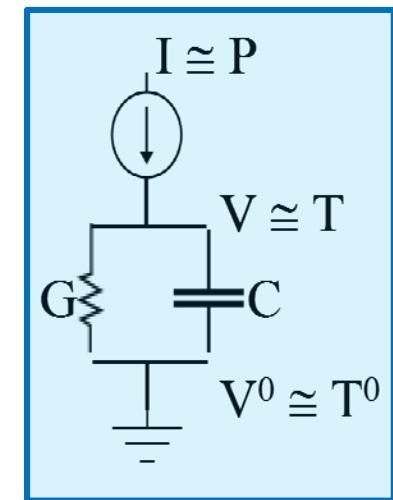
$$\frac{dT}{dt} = -gT + h \text{ with } g = \frac{G - \phi}{C}, \quad h = \frac{\psi + GT_{amb}}{C}$$

thermal  
conductance

thermal  
capacity

environment  
temperature

... in analogy with  
electrical circuits

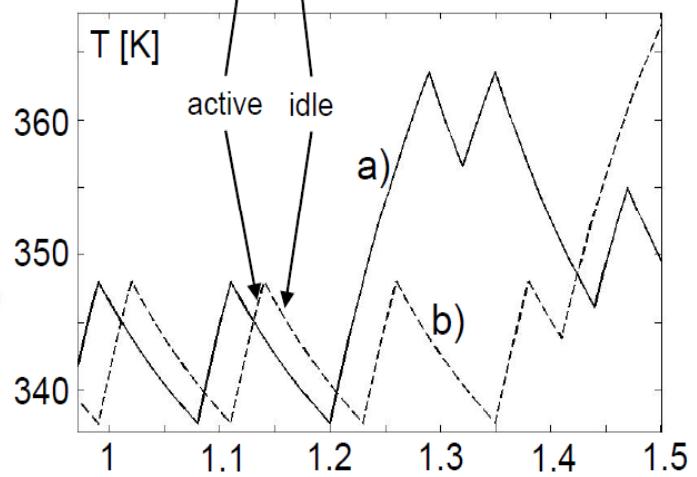
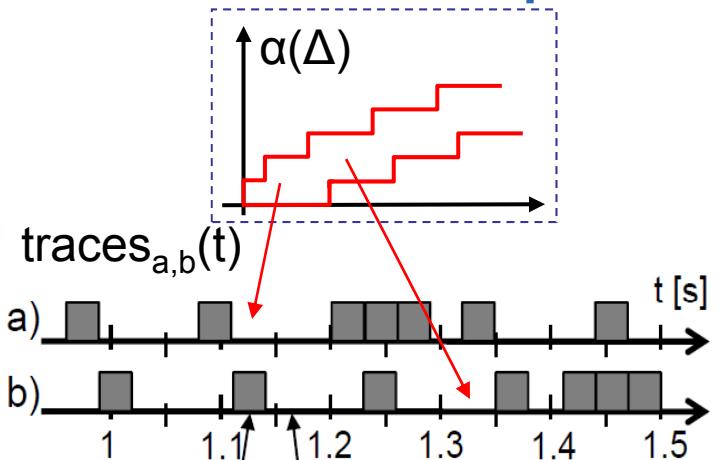


# Embedded System – Thermal Model

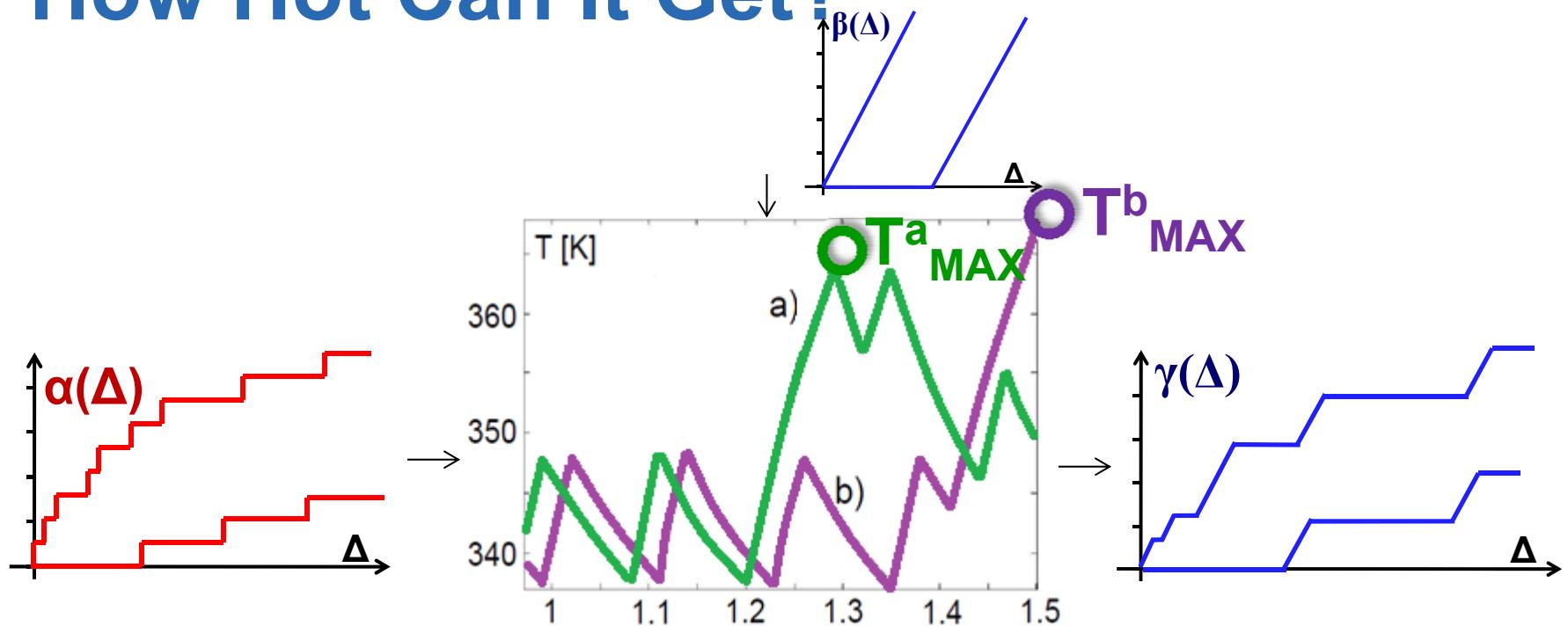
- **bounds on workload arrivals**
  - ...arrival curves  $\alpha(\Delta)$
- **computation model**
  - ...from arrival curves to task execution traces  $[\text{tr}_a(t), \text{tr}_b(t), \dots]$
- **power model**
  - ...from task executions to **active/idle power modes**
- **temperature model**
  - ...from power to temperature

$$C \frac{dT}{dt} = P - G(T - T_{amb})$$

from workload to temperature



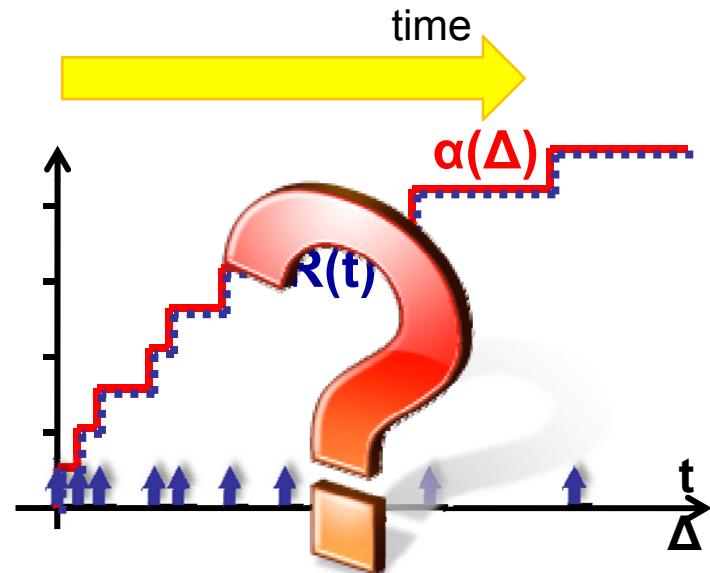
# How Hot Can It Get?



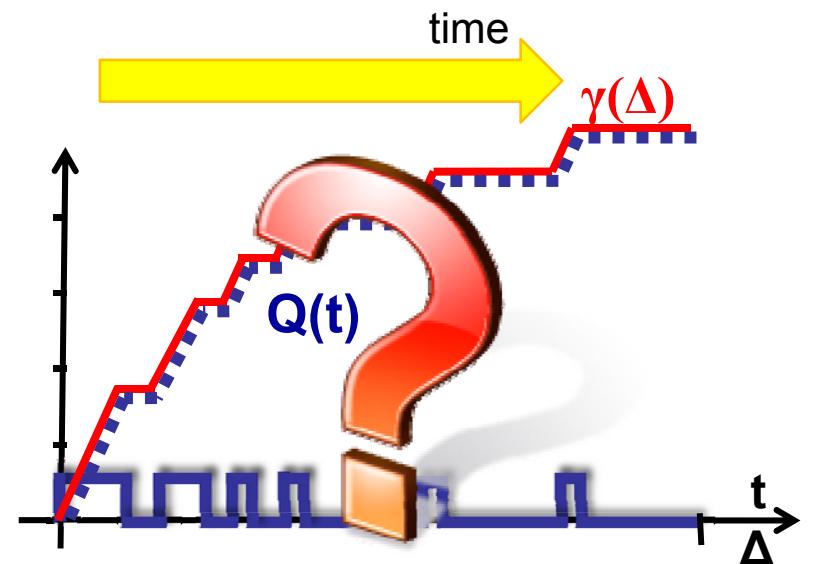
CAN WE DETERMINE  
*WORST CASE (PEAK) TEMPERATURES*  
IN MPA COMPOSITIONAL FRAMEWORK?  
(AT SYSTEM LEVEL – DESIGN TIME)

# Critical Instance for Temperature Analysis?

$\alpha(\Delta)$  corresponds to time-critical instance, leading to **worst-case execution time**

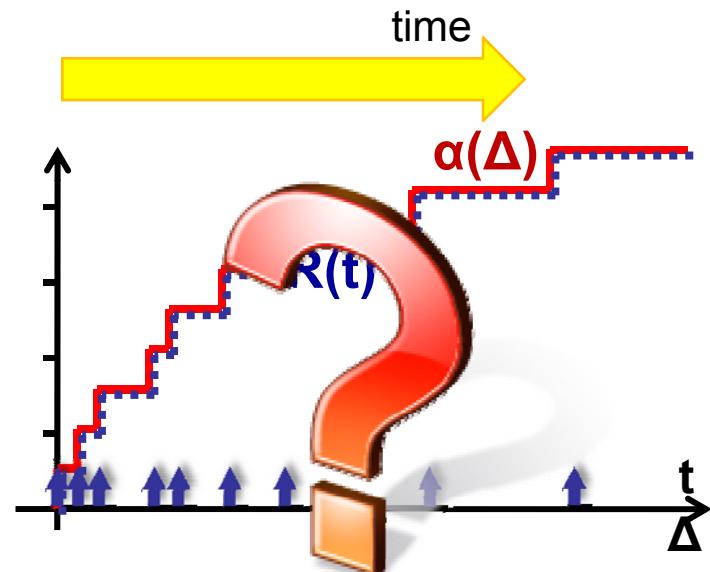


$\gamma(\Delta)$  is the upper bound on accumulated computing time, due to  $\alpha(\Delta)$

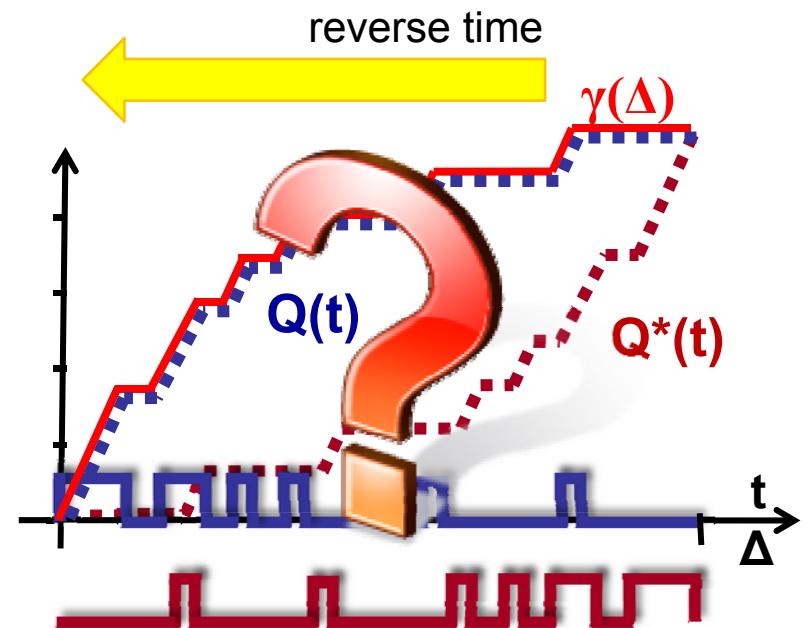


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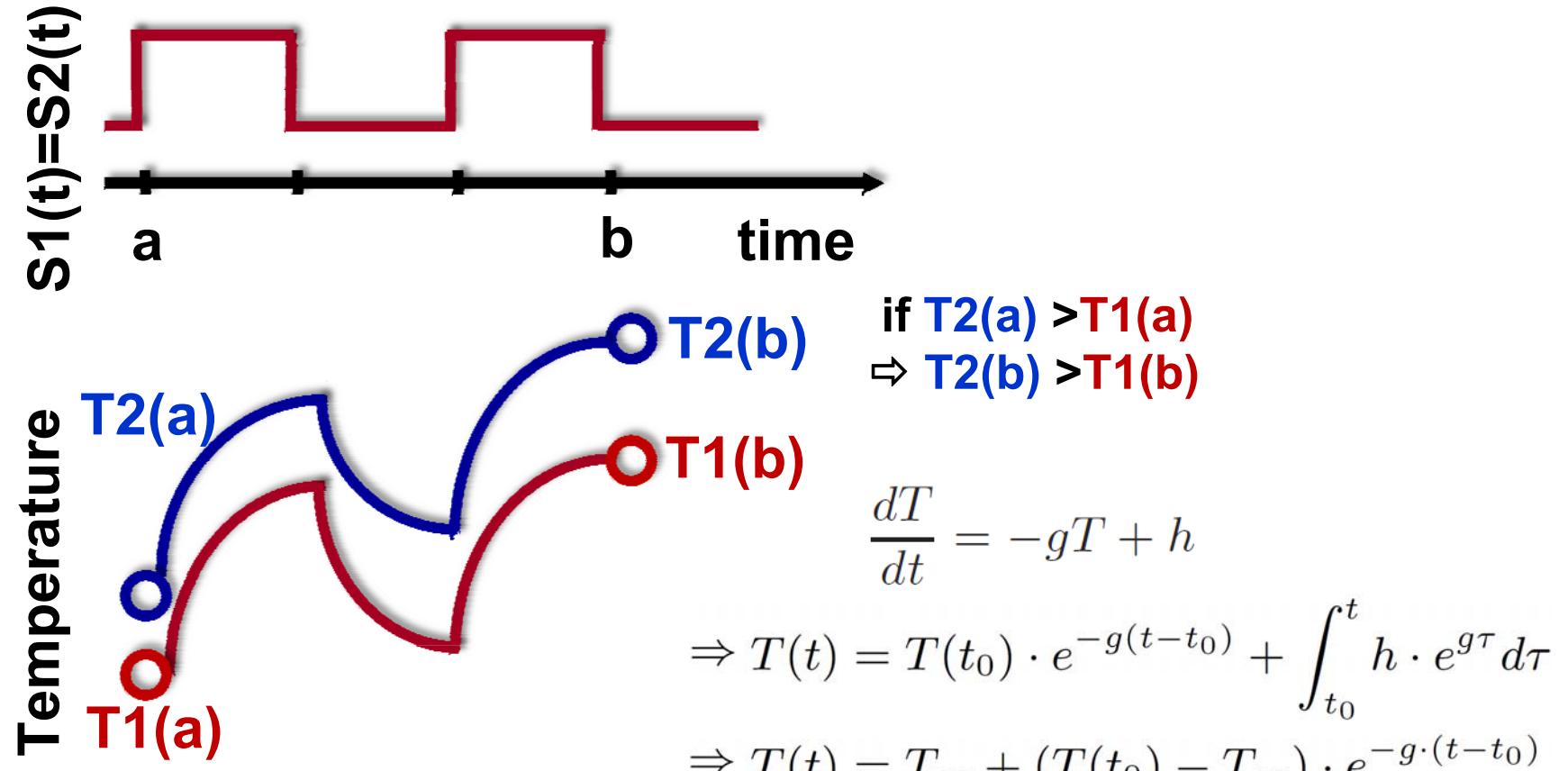


$Q^*(t)$  leads to MAX  $T^*(t)$ !  
(see DATE2011 paper)



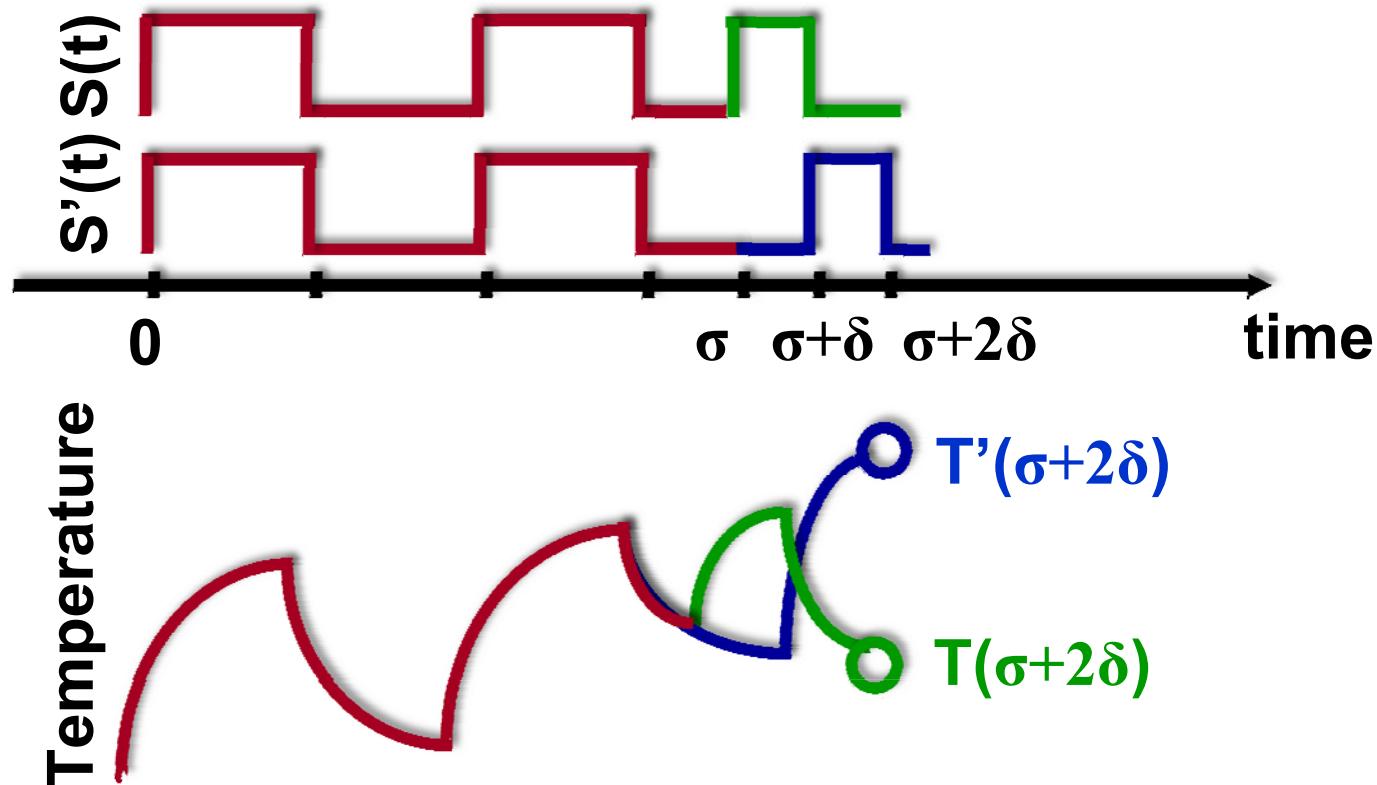
# Basics: Thermal Monotonicity

- For 2 equal *idle/active* sequences in  $[a,b]$ ,  
the sequence with higher initial temperature  $T_2(a) > T_1(a)$ ,  
leads to a higher final temperature  $T_2(b) > T_1(b)$ .



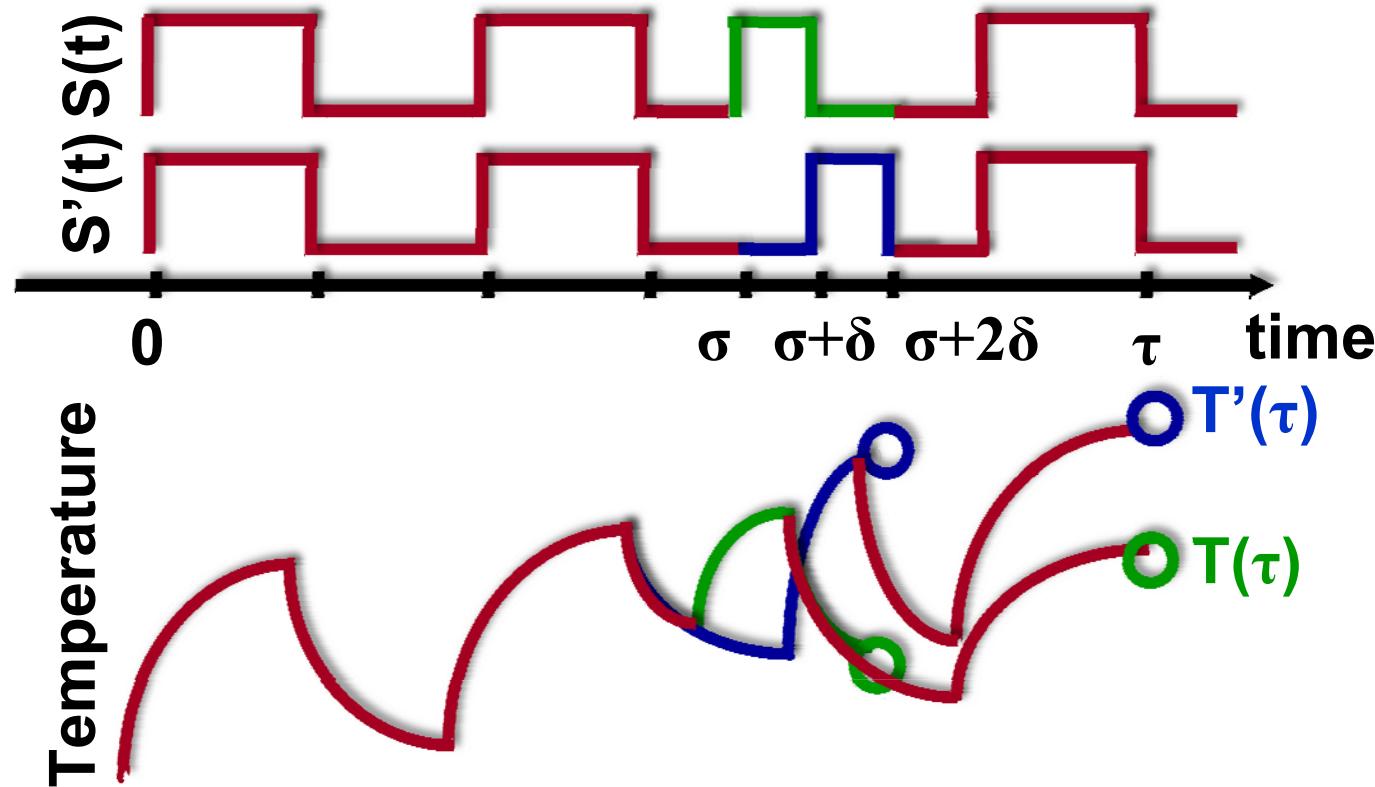
## Basics: Exchange Theorem

- Given sequences  $S(t)$  and  $S'(t)$ , differing in  $[\sigma, \sigma+2\delta]$ ,  
s.t.,  $S(t)=[\text{active}, \text{idle}]$  and  $S'(t)=[\text{idle}, \text{active}]$ ,  
for the same initial temperature  $\Rightarrow T(\tau) \leq T'(\tau)$



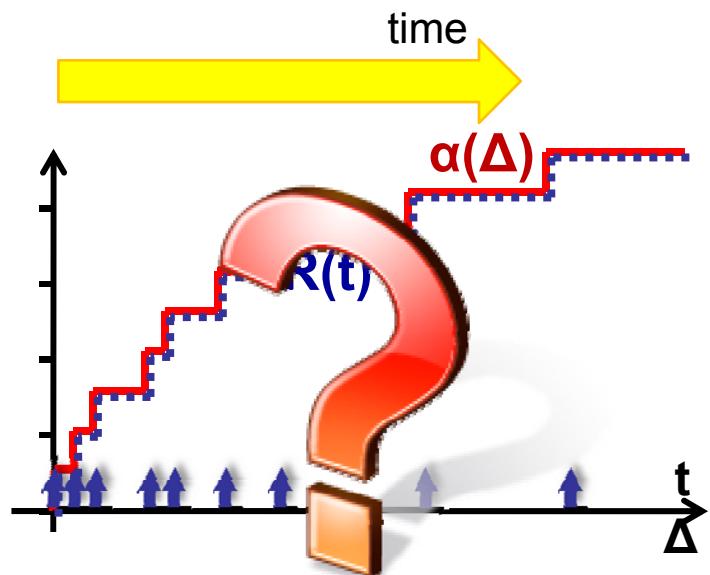
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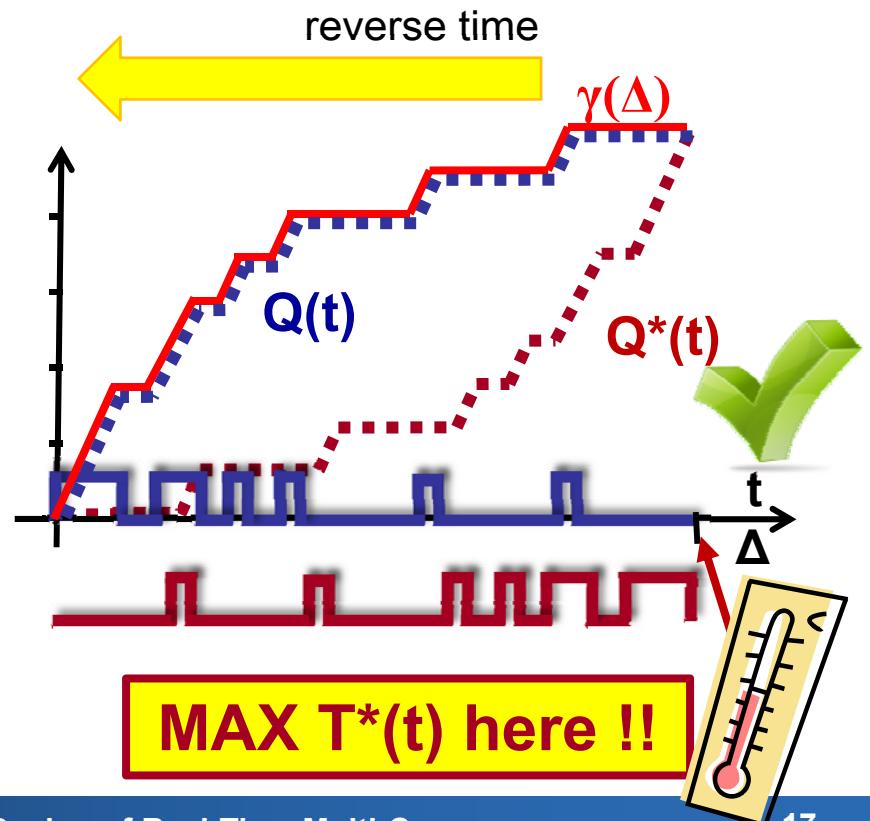


# Critical Instance for Temperature Analysis?

does there exist a  
*feasible input trace*  
that leads to MAX. peak  $T^\circ$ ?

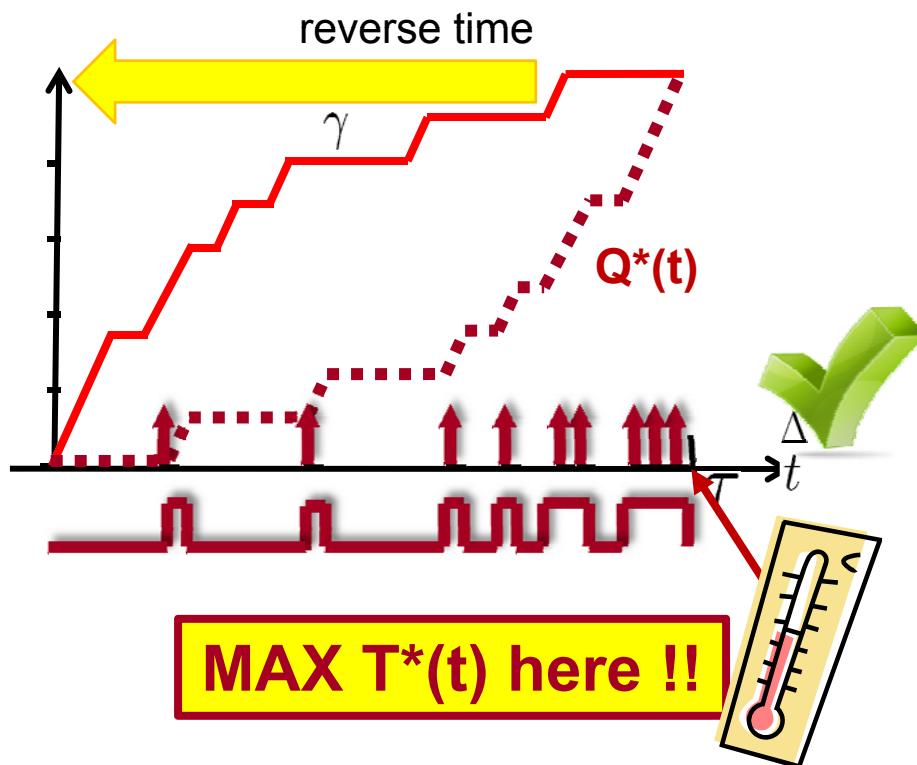


$Q^*(t)$  leads to MAX  $T^*(t)$ !  
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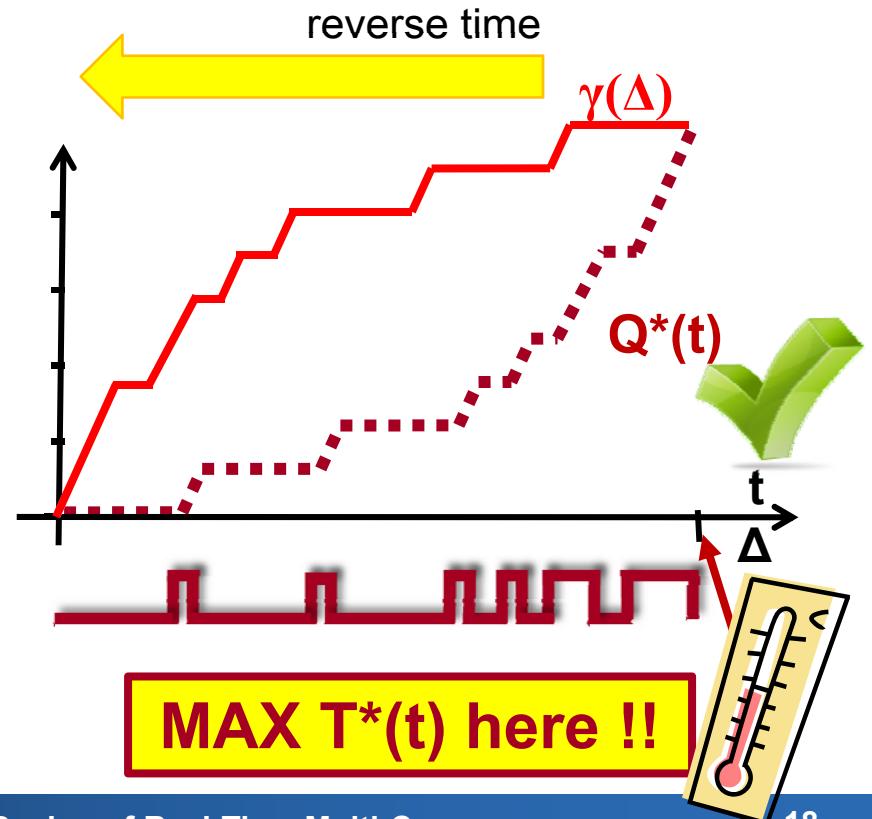


# Critical Instance for Temperature Analysis?

$R^*(t) = Q^*(t)$   
leads to MAX  $T^*(t)$ !



$Q^*(t)$  leads to MAX  $T^*(t)$ !  
(see DATE2011 paper)

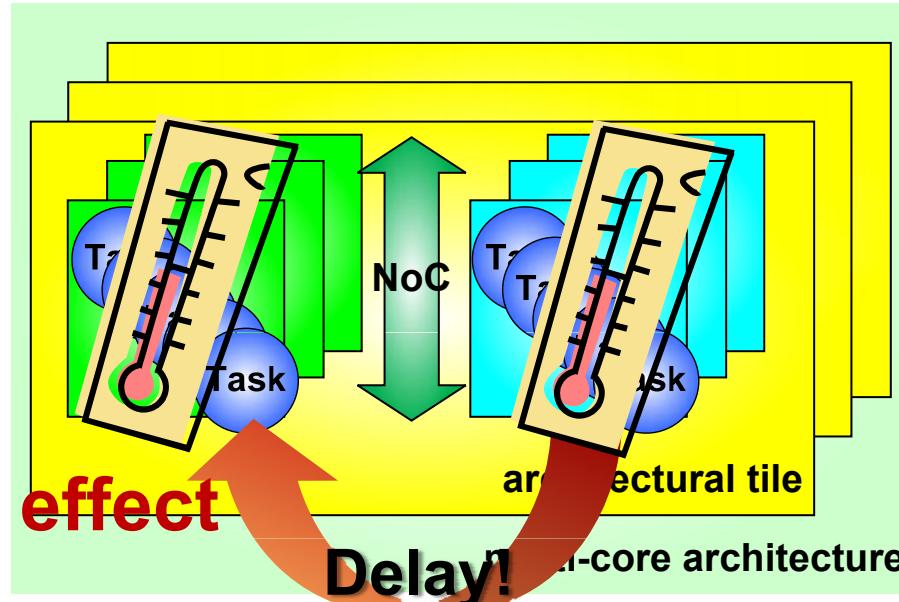


# How about Peak Temperature in Multi-Cores?

self-heating effect

Delay!

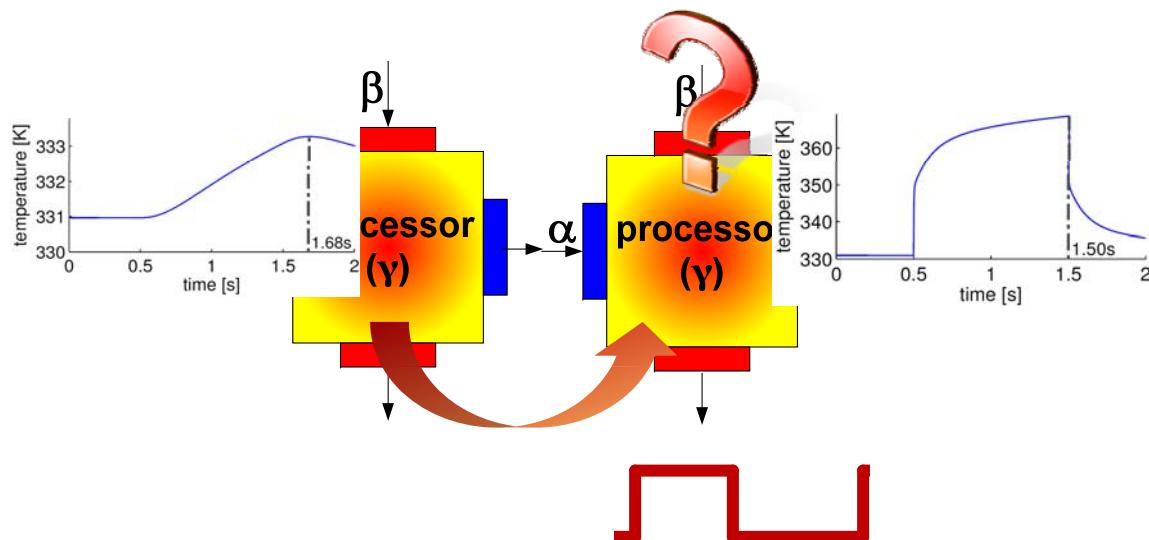
neighboring heating effect



- $T_{MAX}\{\text{SYSTEM}\} = \max \{T_{MAX}\{\text{SYSTEM}_{\{\text{COMPONENT}_i\}}\}\}$
- $T_{MAX}\{\text{SYSTEM}_{\{\text{COMPONENT}_i\}}\} = T_{self\_heating}_{\{\text{COMPONENT}_i\}} + \sum [T_{neighboring\_heating}_{\{\text{COMPONENT}_k\}}]$

# How about Temperature Critical Instances of Multi-Cores?

1. Reduction to One Input – One Output relation
2.  $T_{\text{MAX}}\{\text{SYSTEM}\} = \max \{T_{\text{MAX}}\{\text{SYSTEM}_{\{\text{COMPONENT}_i\}}\}\}$



$T_{2,2}^*$	304 K
$T_{2,1}^*$	41 K
$T_2^*$	345 K

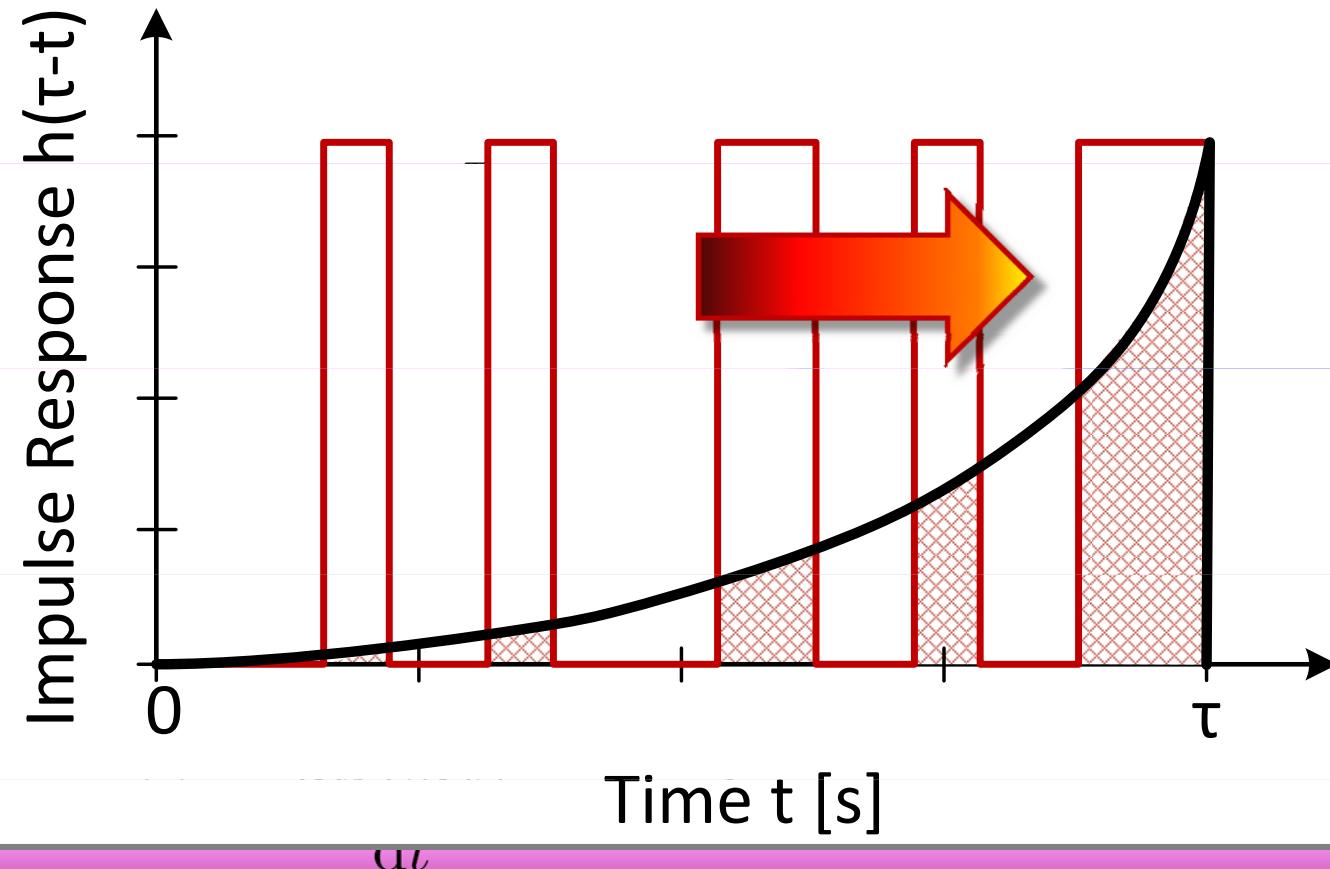
# Thermal Optimization Problem

Optimization Problem

Maximise

Subject to

Model



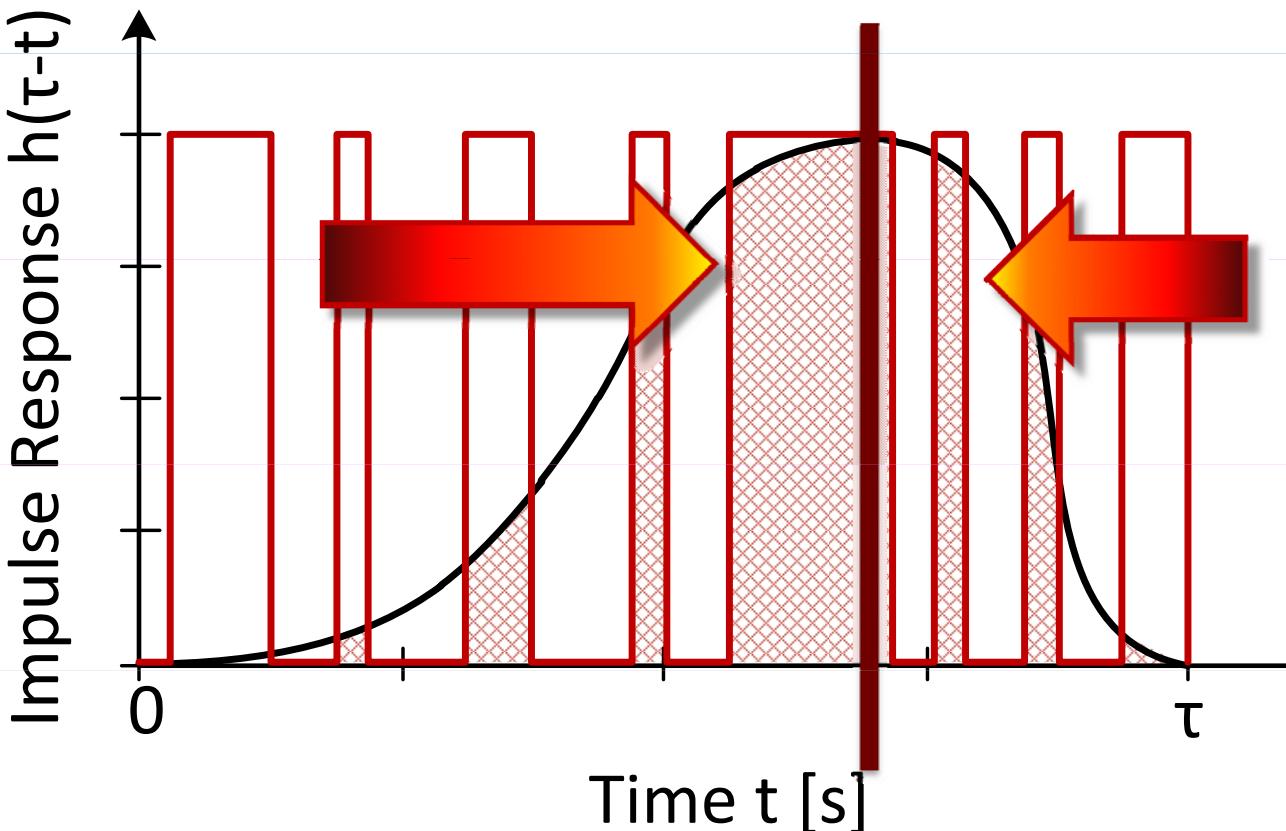
# Thermal Optimization Problem

Optim

Maxim

Subje

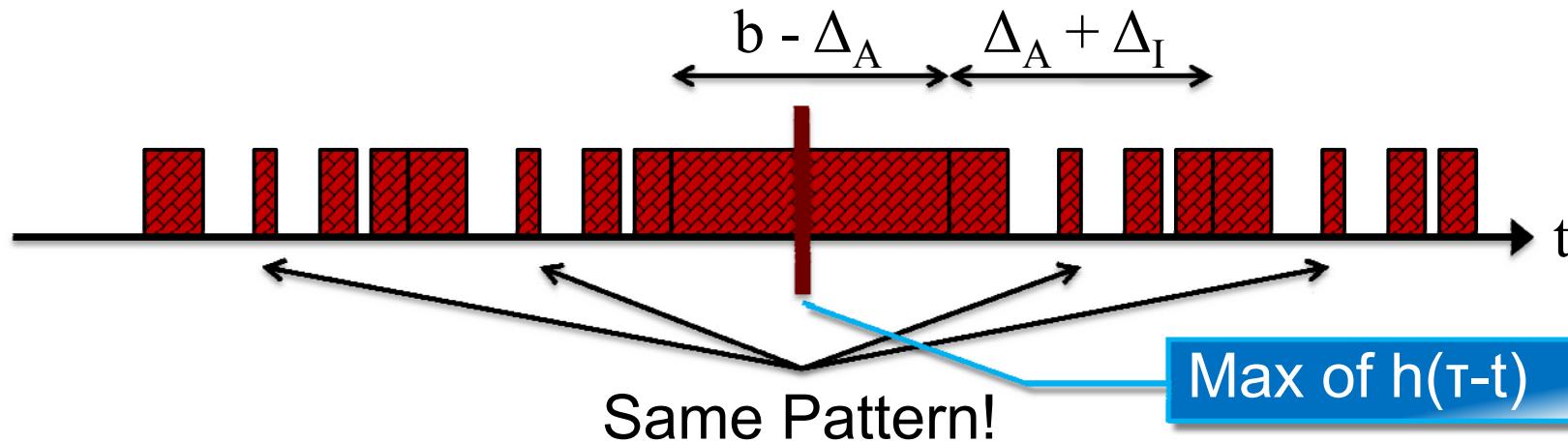
Model



$$S(t) = \frac{dQ(s, t)}{dt} \in \{0, 1\}$$

# Critical Instance for Multi-Cores – Exact Sol.

## Exact Solution



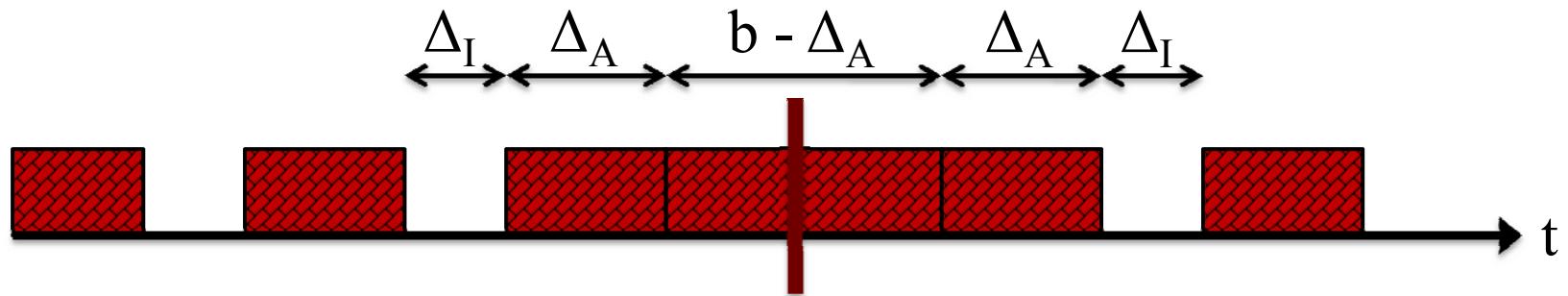
## Exhaustive search:

- Position of the first block?
- Pattern?

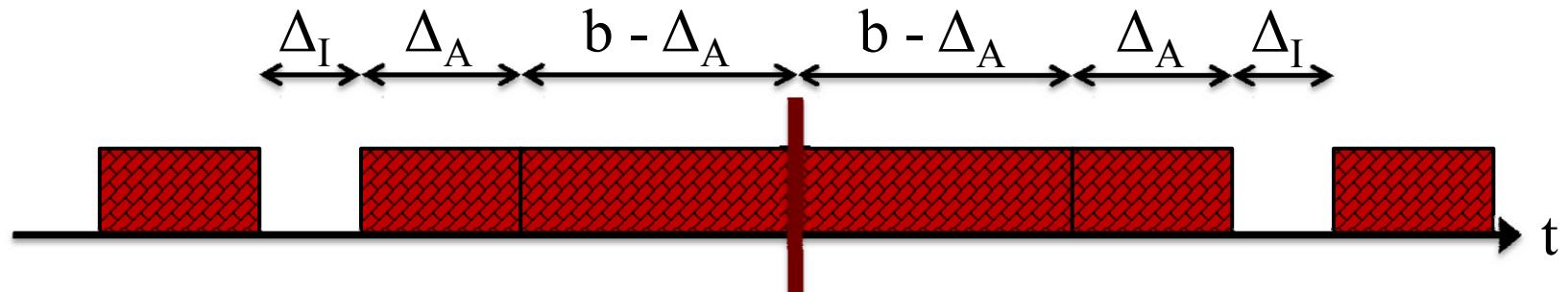


## Critical Instance for Multi-Cores – Approx.

### Approximation 1



### Approximation 2



# How large should $\tau$ be?

- All observation times  $t \leq \tau$  guarantee peak-temperature precision of  $T_a^*(\tau) - T_i^*(\tau)$  for estimating  $T^*$  with upper bound  $T_a^*(\tau)$

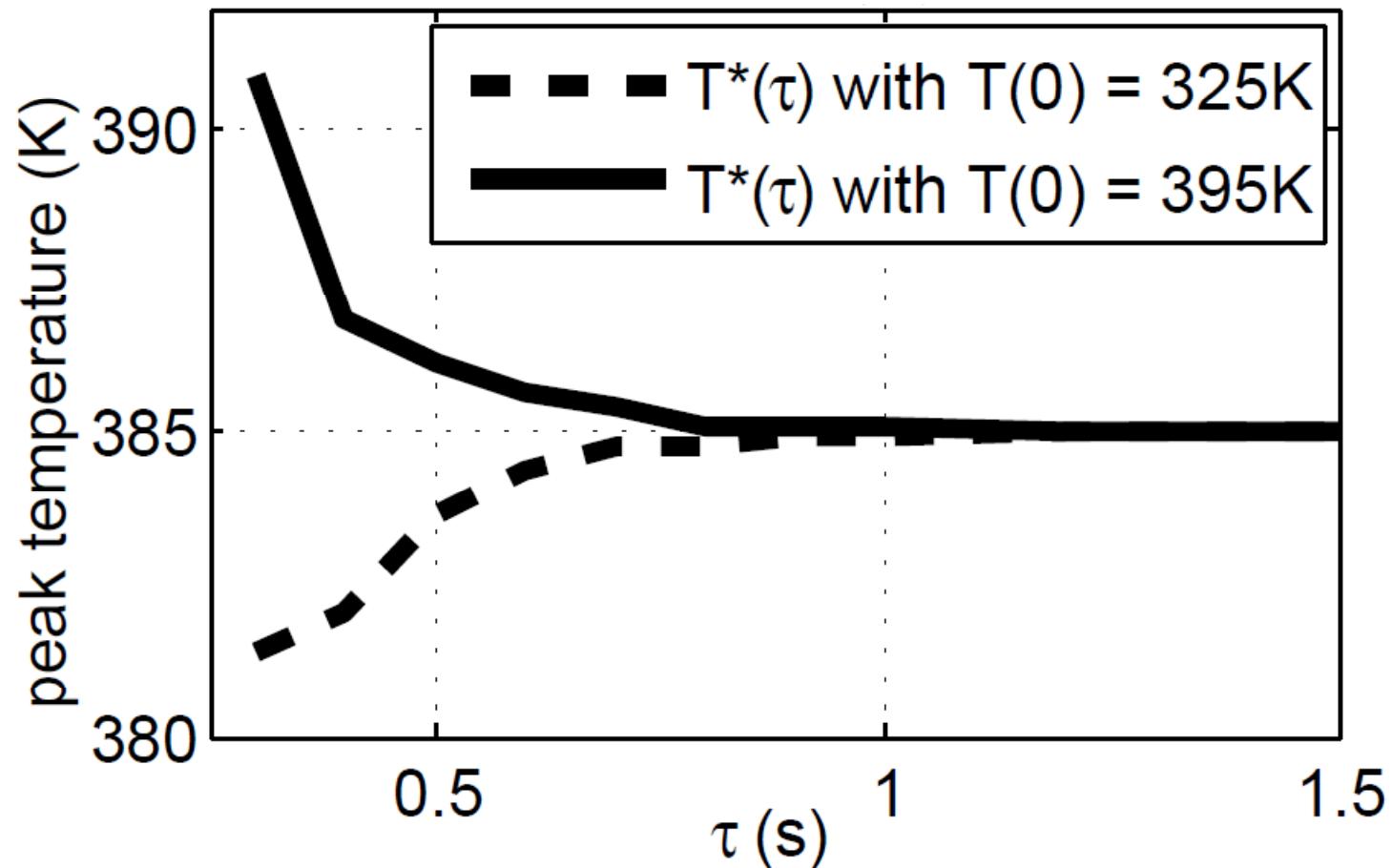
$$\tau \geq \frac{1}{\min\{g_i, g_a\}} \cdot \log \frac{(T_\infty)_a - (T_\infty)_i}{T_a^*(\tau) - T_i^*(\tau)}$$

thermal coefficients  
for *active/idle* power  
modes

steady-state  
temperatures  
for *active/idle*  
modes

temperatures for  
*active/idle*  
modes at  $\tau$ , with  
initial  $(T_\infty)_a / (T_\infty)_i$

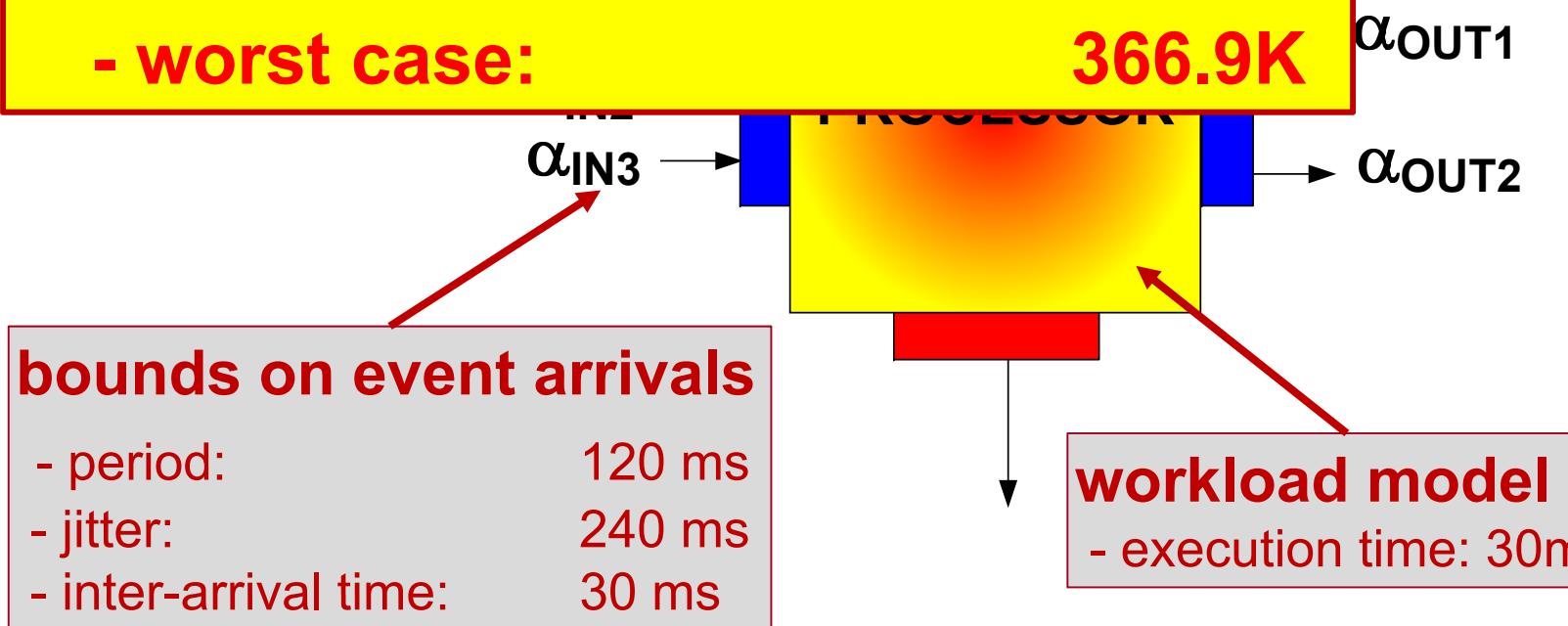
# How Large Should $\tau$ Be?



# Simple Example

## peak temperatures

- average workload (25%): **342.5K**
- random traces (500 s): **362.2K**
- reasonable heuristic: **363.5K**
- worst case:** **366.9K**



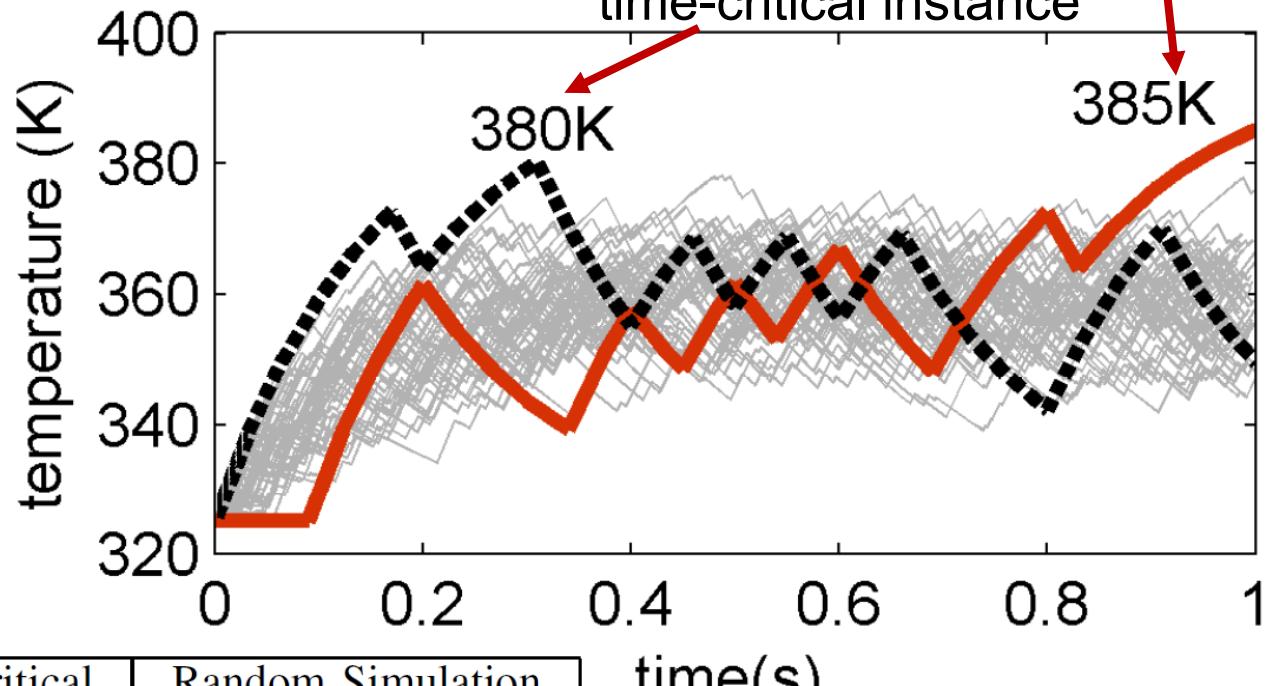
## Example 2: 3-Multi-Media Applications

	Video	Audio	Network
period (p)	[20, 90]ms	30ms	30ms
jitter	[20, 90]ms	10ms	10ms
min. inter-arrival	1ms	1ms	1ms
execution demand	6		
deadline	peri		

peak temperature for  
temperature-critical instance

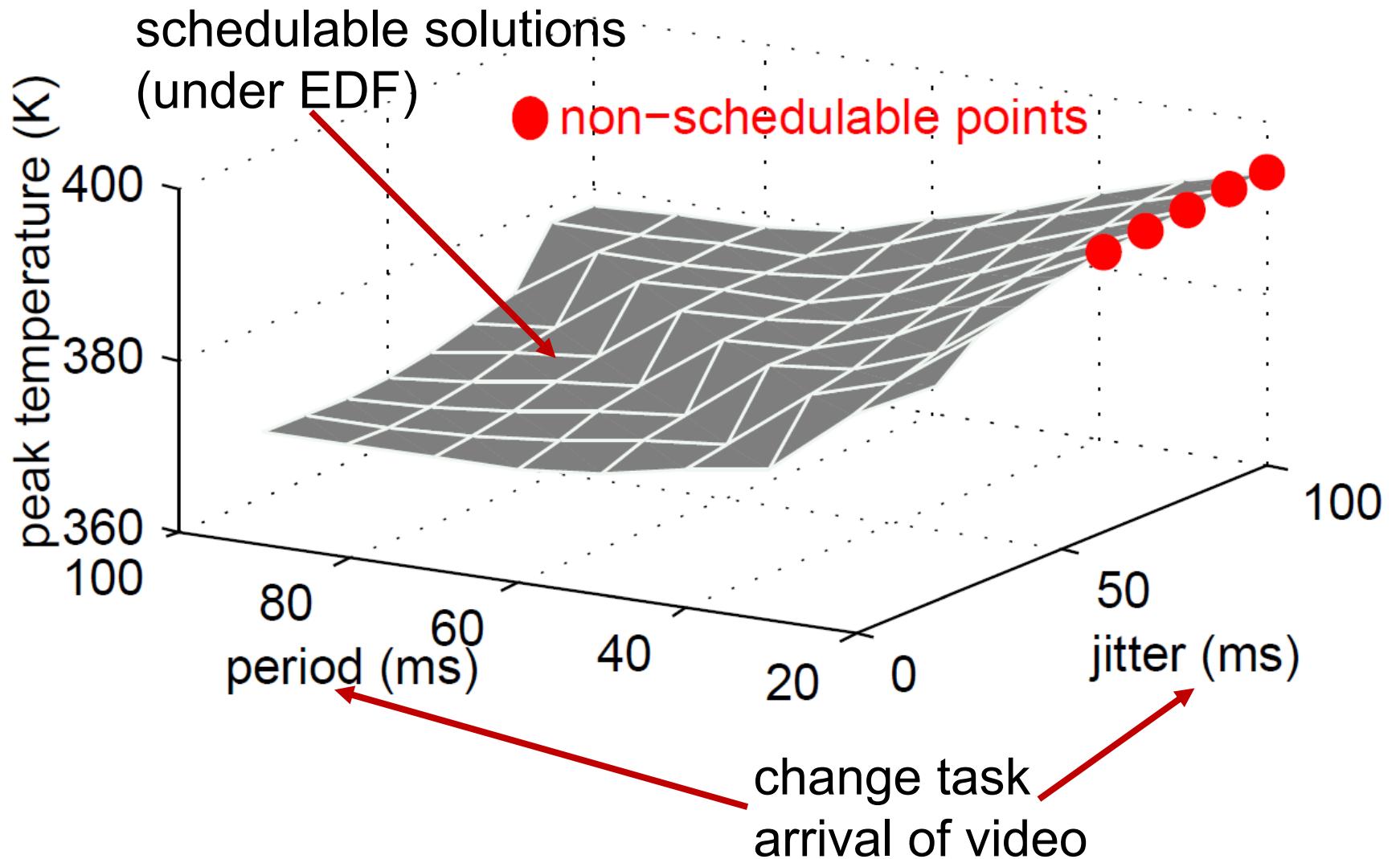
peak temperature for  
time-critical instance

$G$	$C$	$\phi_i =$
$0.3 \frac{W}{K}$	$0.03 \frac{J}{K}$	0.1



Thermal critical	Timing critical	Random Simulation
385.00K	380.00K	378.00K

## Example 2: Design Space Exploration



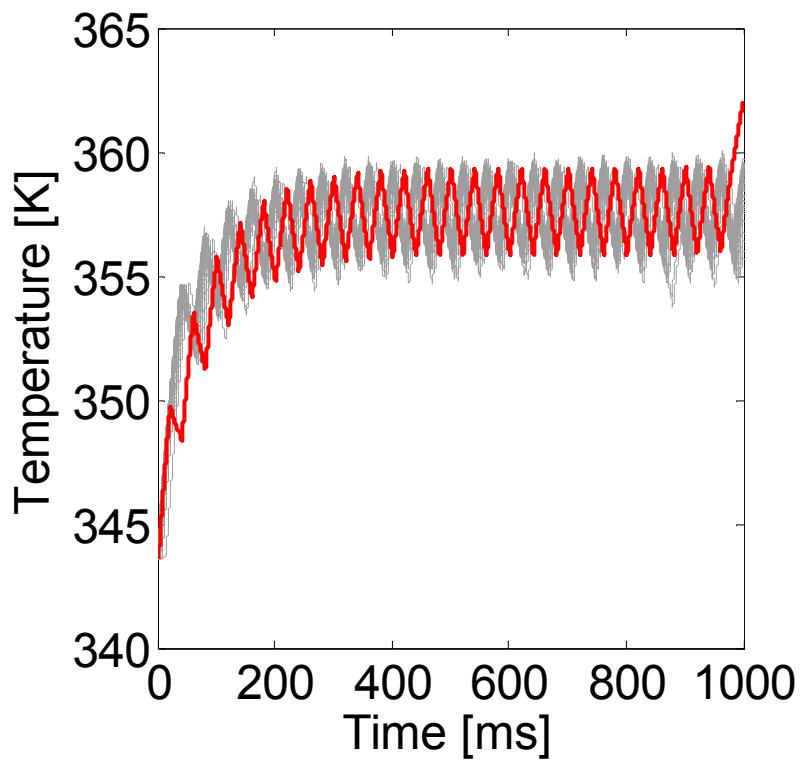


# Multi-Core Evaluation: Setup

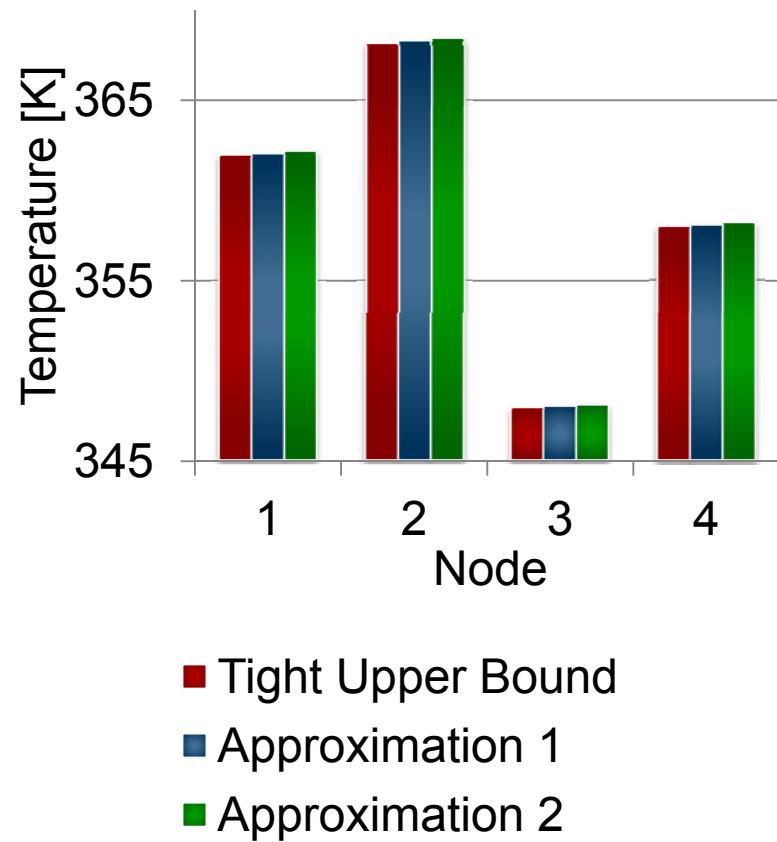
	Processing Component 1	Processing Component 2	Processing Component 3	Processing Component 4
<b><i>Period p</i></b>	40ms	44ms	24ms	36ms
<b><i>Jitter j</i></b>	20ms	22ms	48ms	36ms
<b><i>Min. inter-arrival a</i></b>	1ms	1ms	1ms	1ms
<b><i>Execution demand d</i></b>	20ms	22ms	12ms	18ms

# Multi-Core Evaluation: Result

Random Trace

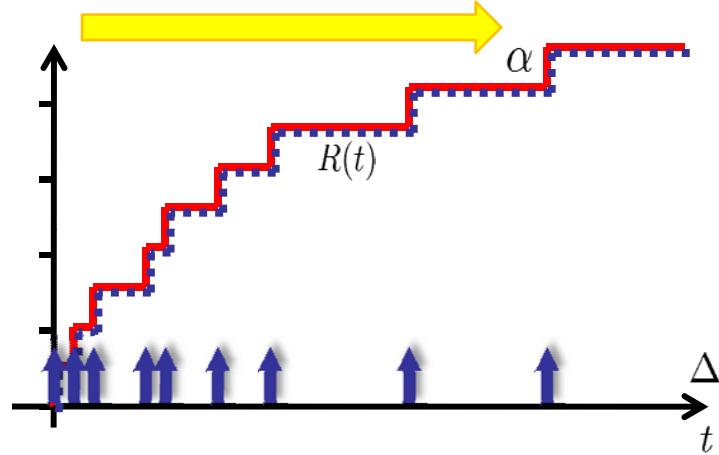


Approximation

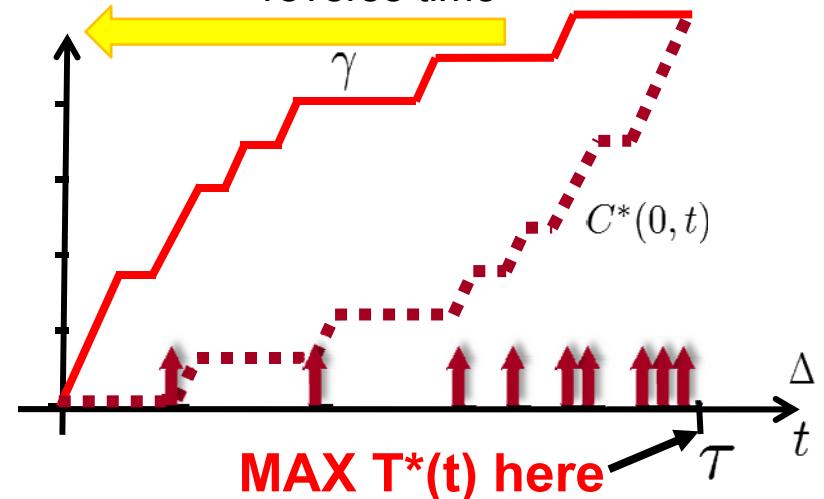


# In Conclusion: How Hot Can It Get?

critical instance for  
real-time analysis  
time



critical instance for  
temperature analysis  
reverse time



- Analytic framework **guaranteeing max temperature** on-chip, at system-level and at design time
- Optimize mappings w.r.t. **time AND temperature**
- Results integrated in **MPA toolbox** (<http://www.mpa.ethz.ch>)

